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## Proceedings of the Second International Conference on The Theory of Groups

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## PREFACE

This volume consists of papers presented to the Second International Conference on the Theory of Groups held in Canberra in August 1973 together with a report by the chairman of the Organizing Committee and a collection of problems.

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M.F. Newman

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