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Numerical Methods in Computational Electrodynamics

Linear Systems
in Practical Applications

With 173 Figures, 65 in Colour



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To my children
Jan and Viola

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² being able to take care of the children

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³ Deutsches Elektronen-Synchrotron

Overview

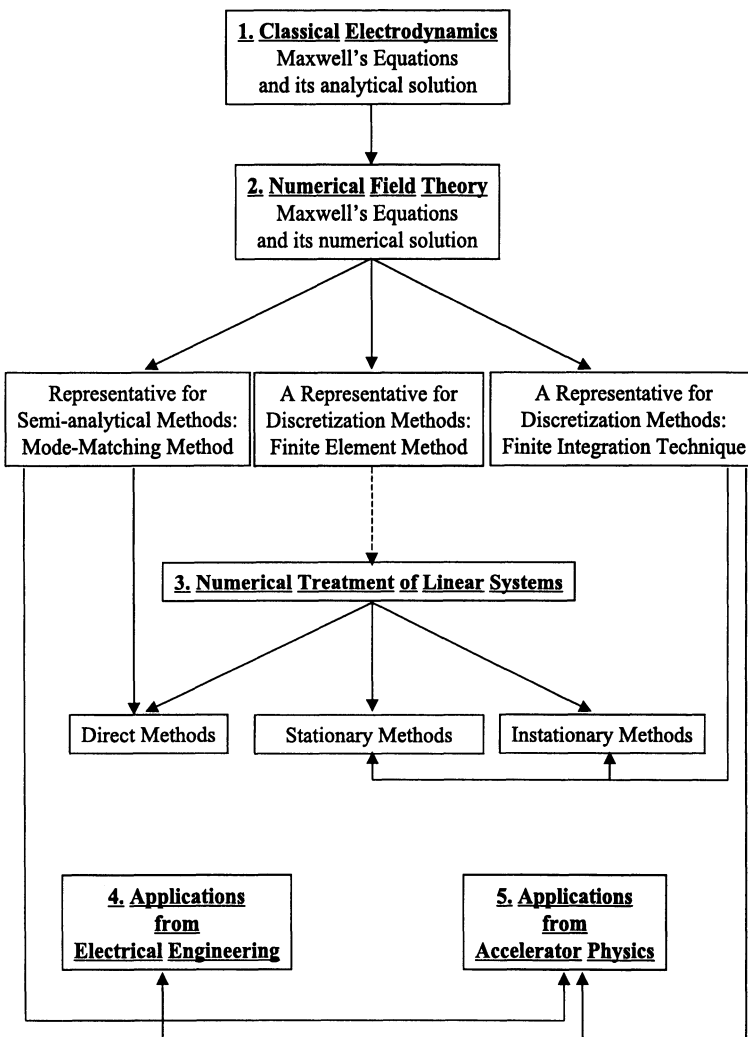


Figure 0.1. Organization of the book.