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Catherine Donati-Martin • Antoine Lejay  
Alain Rouault  
Editors

# Séminaire de Probabilités XLIV

*Editors*

Catherine Donati-Martin  
Université de Versailles-St-Quentin  
Versailles  
France

Alain Rouault  
Université de Versailles-St-Quentin  
Versailles  
France

Antoine Lejay  
Nancy-Université, INRIA  
Vandoeuvre-lès-Nancy  
France

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# Preface

As usual, some of the contributions to this 44th Séminaire de Probabilités were exposed during the Journées de Probabilités held in Dijon in June 2010. The other ones come from spontaneous submissions or were solicited by the editors. The traditional and historical themes of the Séminaire are present, such as stochastic calculus, local times and excursions and martingales. Some subjects already largely present in the previous volumes are still here: free probability, rough paths, limit theorems for general processes (here fractional Brownian motion and polymers) and large deviations. Finally, this volume explores new topics, including variable length Markov chains and peacocks. We hope that the whole volume is a good sample of the main streams of current research on probability and stochastic processes, in particular those active in France.

We remind that the web site of the Séminaire is

<http://portail.mathdoc.fr/SemProba/>

and that all the articles of the Séminaire from Volume I in 1967 to Volume XXXVI in 2002 are freely accessible from the web site

<http://www.numdam.org/numdam-bin/feuilleter?j=SPS>

We thank the Cellule Math Doc for hosting all these articles within the NUMDAM project.

*Catherine Donati-Martin  
Antoine Lejay  
Alain Rouault*



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