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Hodge Cycles, Motives, and Shimura Varieties

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PREFACE

This volume collects six related articles.

The first is the notes (written by J.S. Milne) of a major part of the seminar "Périodes des Intégrales Abéliennes" given by P. Deligne at I.H.E.S., 1978-79.

The second article was written for this volume (by P. Deligne and J.S. Milne) and is largely based on: N Saavedra Rivano, *Catégories tannakiennes*, Lecture Notes in Math. 265, Springer, Heidelberg 1972.

The third article is a slight expansion of part of: J.S. Milne and Kuang-yen Shih, *Shimura varieties: conjugates and the action of complex conjugation* 154 pp. (Unpublished manuscript, October 1979).

The fourth article is based on a letter from P. Deligne to R. Langlands, dated 10th April, 1979, and was revised and completed (by Deligne) in July, 1981.

The fifth article is a slight revision of another section of the manuscript of Milne and Shih referred to above.

The sixth article, by A. Ogus, dates from July, 1980.

P. Deligne
J.S. Milne
A. Ogus
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Note to the second printing 1989

For this printing an Addendum and Erratum were added (pp. 415, 416).

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