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Model Theory and Topoi

A Collection of Lectures by Various Authors

Edited by F. W. Lawvere, C. Maurer and G. C. Wraith



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Editors

Dr. F. William Lawvere
Department of Mathematics
State University of New York
at Buffalo
Amherst, N. Y. 14226/USA

Dr. Christian Maurer
Freie Universität Berlin
Institut für Mathematik II
D-1 Berlin 33
Königin-Luise-Str. 24-26

Dr. Gavin C. Wraith
School of Mathematical
and Physical Sciences
University of Sussex
Brighton BN1 9QH/England

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