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# Lecture Notes in Mathematics

A collection of informal reports and seminars

Edited by A. Dold, Heidelberg and B. Eckmann, Zürich

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Hans Hermes

Universität Freiburg i. Br., Math. Institut

Abteilung für math. Logik und Grundlagen der Mathematik

## Term Logic with Choice Operator

Revised and Enlarged Translation  
of the first German Edition

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