

**STUDIES ON GOTTLOB FREGE AND
TRADITIONAL PHILOSOPHY**

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AND TRADITIONAL
PHILOSOPHY



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PARENTIBUS UXORIQUE DEDICATUM

PREFACE

I wish to express, first of all, my profound gratitude to Professor J. M. Bocheński, without whose assistance the present work would have not been possible. To be concise, I would like to state that his contribution to this book may be viewed at three levels: (1) that of the general *spirit*, (2) that of the specific ideas, theses or approaches which are expressed in its pages, (3) that of this work *qua* doctoral dissertation. The general spirit which has guided my research coincides with that underlying Professor Bocheński's own works, in particular his *Formale Logik* (München 1956). Moreover, the particular occasion which suggested my investigation was a statement included in that book according to which the literature in the field still lacked a detailed work on Frege (p. 317).

I wish, likewise, to express my gratitude to other professors of the University of Fribourg for their generous help. I mention especially Professors P. Wyser, M. D. Philippe, N. Luyten, and V. Kuiper.

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