

IUTAM SYMPOSIUM ON  
ADVANCES IN NONLINEAR STOCHASTIC MECHANICS

# SOLID MECHANICS AND ITS APPLICATIONS

Volume 47

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## *Aims and Scope of the Series*

The fundamental questions arising in mechanics are: *Why?*, *How?*, and *How much?* The aim of this series is to provide lucid accounts written by authoritative researchers giving vision and insight in answering these questions on the subject of mechanics as it relates to solids.

The scope of the series covers the entire spectrum of solid mechanics. Thus it includes the foundation of mechanics; variational formulations; computational mechanics; statics, kinematics and dynamics of rigid and elastic bodies; vibrations of solids and structures; dynamical systems and chaos; the theories of elasticity, plasticity and viscoelasticity; composite materials; rods, beams, shells and membranes; structural control and stability; soils, rocks and geomechanics; fracture; tribology; experimental mechanics; biomechanics and machine design.

The median level of presentation is the first year graduate student. Some texts are monographs defining the current state of the field; others are accessible to final year undergraduates; but essentially the emphasis is on readability and clarity.

*For a list of related mechanics titles, see final pages.*

IUTAM Symposium on  
**Advances in Nonlinear  
Stochastic Mechanics**

Proceedings of the IUTAM Symposium  
held in Trondheim, Norway,  
3–7 July 1995

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## PREFACE

The IUTAM Symposium on Advances in Nonlinear Stochastic Mechanics, held in Trondheim July 3-7, 1995, was the eighth of a series of IUTAM sponsored symposia which focus on the application of stochastic methods in mechanics. The previous meetings took place in Coventry, UK (1972), Southampton, UK (1976), Frankfurt/Oder, Germany (1982), Stockholm, Sweden (1984), Innsbruck/Igls, Austria (1987), Turin, Italy (1991) and San Antonio, Texas (1993).

The symposium provided an extraordinary opportunity for scholars to meet and discuss recent advances in stochastic mechanics. The participants represented a wide range of expertise, from pure theoreticians to people primarily oriented toward applications. A significant achievement of the symposium was the very extensive discussions taking place over the whole range from highly theoretical questions to practical engineering applications. Several presentations also clearly demonstrated the substantial progress that has been achieved in recent years in terms of developing and implementing stochastic analysis techniques for mechanical engineering systems. This aspect was further underpinned by specially invited extended lectures on computational stochastic mechanics, engineering applications of stochastic mechanics, and nonlinear active control. The symposium also reflected the very active and high-quality research taking place in the field of stochastic stability. Ten presentations were given on this topic of a total of 47 papers. A main conclusion that can be drawn from the proceedings of this symposium is that stochastic mechanics as a subject has reached great depth and width in both methodology and applicability.

The Opening Address of the symposium was given by The Secretary General of the IUTAM, Dr. F. Ziegler. On the first day of the symposium, a reception in the Archbishop's Palace was hosted by the City of Trondheim. This was preceded by an organ concert hosted by Golar Nor Offshore AS in the Nidaros Cathedral. The symposium banquet was hosted by Dr. Steen Krenk and Dr. Arvid Naess in the Banquet Hall of the Ringve Museum of Musical History, with Dr. Y.K. Lin serving as the banquet speaker. The Closing Address was delivered by Dr. K. Sobczyk, Member of the IUTAM Symposium Committee.

On behalf of the Scientific and Organizing Committees, we would like to thank the IUTAM Bureau for promoting and sponsoring this symposium. We are also greatly in debt to the other sponsors, whose contributions made this symposium possible. The contributions of the authors and participants in the symposium are, of course, instrumental in producing a successful meeting and its proceedings, and we deeply appreciate their efforts. The assistance in processing the manuscripts provided by Mrs. A.M. Soeberg of the Norwegian Institute of Technology and Ms. M. Jönsson of Lund University is gratefully acknowledged.

A. Naess

S. Krenk

## Opening Address of the Secretary General of IUTAM

Chairmen, Ladies and Gentlemen,

On behalf of the International Union of Theoretical and Applied Mechanics it is my duty and my pleasure to welcome you at the IUTAM Symposium on Advances in Nonlinear Stochastic Mechanics. The proposal to arrange this Symposium was accepted in August 1992 by the General Assembly of IUTAM. Since that time both chairmen, Professor S Krenk and Professor A Naess have done an excellent job in preparing the scientific program. The chairmen have been advised by the Scientific Committee in selecting and inviting participants from all over the world.

There are sometimes some misunderstandings about the appointment of the Scientific Committee by IUTAM: If you look back to the related IUTAM Symposia held in Turin 1991 and San Antonio 1993, to mention just the two recent ones, you see different members of the Scientific Committees with only a small overlap to the current one: Professor S T Ariaratnam, Professor P Bernard, Professor V Bolotin, Professor R N Iyengar, Professor Y K Lin, Professor J B Roberts, Professor W Schiehlen (ex officio), Professor K Sobczyk and Professor P Spanos. Since the value and quality of IUTAM is reflected by its Symposia, we are very happy to have the series of proceedings and meetings in the field of Stochastic Mechanics. There are many more meetings referring to that important subject, some people even speak of an inflation, however, the quality of the IUTAM Symposia is hardly reached elsewhere.

Norway is a member of IUTAM since 1949. Its National Committee is represented in the Union by the Chairman, Professor B Gjevik, University of Oslo. There have been many important conferences organized in Norway, I just refer to the recent 15th International Congress of Acoustics (Norwegian Institute of Technology, Trondheim, Norway, 26-30 June 1995) which is related to our Union. However, we are opening the first IUTAM Symposium to be held in this beautiful country.

We look forward to a dense, but exciting program, divided into 16 Sessions. I am especially happy to see sessions devoted to evolving fields like Stochastic Finite Elements and System Identification and Control. Stochastic Mechanics will be present at the 19th ICTAM, Kyoto, 25-31 August 1996, to celebrate 20 years of IUTAM engagement in that field that have passed since the first IUTAM Symposium held in 1976 in Southampton, England. The General Assembly held during the Congress will decide on future Symposia for the years 1998/99, depending on the quality of the proposals received. It would be a good idea to consider the future of Stochastic Mechanics in the tenure of our Symposium. We shall start with an exciting session with the specially invited lecture given by Professor Masanobu Shinozuka on Computational Stochastic Mechanics.

Thank you for your kind attention.

Franz Ziegler

## Final Address at the Closing Ceremony on behalf of IUTAM

Ladies and Gentlemen,

The Secretary General of IUTAM - Professor F Ziegler- and the former Secretary General - Professor W Schiehlen - who were here with us during the first part of the Symposium had to leave earlier because of other important commitments. So, being recently associated with IUTAM as a member of the IUTAM Symposium Panel, I have the honor and pleasure to say a few words on behalf of IUTAM, and in the name of Professor F Ziegler, particularly. Above all, I wish to express thanks and gratitude to the chairmen of this Symposium - Professor Arvid Naess and Professor Steen Krenk - for all the arrangements which they have made in connection with our Symposium. I also wish to express the appreciation of IUTAM to the Local Organizing Committee for all the technical and administrative help in bringing this Symposium to its successful end.

We have spent five exciting days together, presenting papers, participating in discussions and deliberations on stochastic mechanics - our favourite field of science. But we also had the occasion - which is extremely important as well - to familiarize ourselves a little with this unique and beautiful country. The visit to Ringve Museum of Musical History, followed by the Symposium Dinner, will remain in our memories as an impressive sign of the Norwegian culture and hospitality.

Let me now say a few words on the future IUTAM Symposium on Stochastic Mechanics. IUTAM encourages all of you to continue your engagement in this series of Symposia. What is especially needed now is preparation of good proposals for the next symposium of this type. According to the Secretary General, various competitive proposals are welcome. Proposals for the Symposium in 1998/1999 should be sent to the Secretary General by the end of April of next year. The decision will be made by the General Assembly of IUTAM, after careful evaluation of the proposals by the IUTAM Symposia Panel.

In closing, I wish to thank you - Arvid and Steen - once again for this very successful Symposium. I wish you all a good journey back home and pleasant summer vacations.

K Sobczyk

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