

**Imperfect Information  
and Investor Heterogeneity  
in the Bond Market**



# Contributions to Economics

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# Imperfect Information and Investor Heterogeneity in the Bond Market

With 7 Figures

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*Frank Riedel*

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