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Christoph Meinel

Modified
Branching Programs and
Their Computational Power



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PREFACE

This monograph is a revised version of my habilitation thesis submitted to the presidential council of the Academy of Science of GDR. It summarizes the results of my research on branching program based complexity theory over the last years.

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