

# Lecture Notes in Mathematics

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Andrey V. Zelevinsky

## Representations of Finite Classical Groups

A Hopf Algebra Approach

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