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PREFACE

The papers contained in these lecture notes were contributed by participants in an NSF Regional Conference held at Kent State University in the summer of 1976. Several of the speakers at that Conference had already submitted the papers on which their lectures were based to various mathematical journals; we were fortunate to be able to corral the contributions contained herein.

The topic of the Conference was Banach Spaces of Analytic Functions, and the main attraction was the lectures of Professor Aleksander Pelczynski of the Polish Academy of Sciences (who fortuitously was visiting at Ohio State University from the Fall of 1975 through the summer of 1976). The subject matter covered in these contributions are all related to various aspects and methods discussed in the lectures by Professor Pelczynski. Incidentally, the text of Professor Pelczynski's lectures will appear in monograph form in the Conference Board of Mathematical Sciences series published under the auspices of the American Mathematical Society. People who find things of interest in these notes will find much of interest in Pelczynski's lectures.

As mentioned above, a number of the hour lecturers had submitted their manuscript elsewhere; however, their lectures stimulated great activity in the other Conference participants. This seems as good a place as any to extend our gratitude to those speakers: Tadeusz Figiel, Gdansk; William Johnson, Ohio State University; Robert Kaufman, University of Illinois; Joram Lindenstrauss, Hebrew University; Richard Rochberg, Washington University; Haskell Rosenthal, University of Illinois; Walter Rudin, University of Wisconsin; Allen Shields, University of Michigan; Edgar Stout, University of Washington; Maury Zippin, Hebrew University.

In preparing this volume, we were fortunate to have had expert help from a number of conscientious referees. To these people we extend our thanks: Colin Bennett Sun-Yung Chang, D. J. H. Garling, J. Garnett, D. R. Lewis, R. H. Lohman, J. T. Peck, A. Pelczynski, J. Rainwater, J. R. Retherford, W. Rudin, C. Seifert, J. Shapiro, M. Stoll.

To the Kent State Mathematics Department among of whose members helped greatly with the painful details always attendant to a Conference--particularly, John Fridy, Chuck Seifert, Chuck Giel, Terry Morrison, Arden Ruttan, and Joe Creekmore -- we extend our thanks.

Finally, last but far from least, our thanks to the Departmental secretaries, Julie Froble and Darlene May. They provided calm reason in moments of panic and kept the Conference on an even keel throughout. Further, it's their typing that fills these pages.