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Jean-Yves Béziau • Gianfranco Basti

Editors

# The Square of Opposition: A Cornerstone of Thought

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ISSN 2297-0282

Studies in Universal Logic

ISBN 978-3-319-45061-2

DOI 10.1007/978-3-319-45062-9

ISSN 2297-0290 (electronic)

ISBN 978-3-319-45062-9 (eBook)

Library of Congress Control Number: 2016961939

Mathematics Subject Classification (2010): 03Axx

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Printed on acid-free paper

This book is published under the trade name Birkhäuser, [www.birkhauser-science.com](http://www.birkhauser-science.com)

The registered company is Springer International Publishing AG

The registered company address is: Gewerbestrasse 11, 6330 Cham, Switzerland

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