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Moments of Linear Positive Operators and Approximation

 Springer

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Preface

Moments of Linear Positive Operators and Approximation deals with several problems concerning positive linear operators.

In Chaps. 1 and 2, we present—without proofs—a large collection of formulas concerning the values on power functions (moments) of some of the most well-known positive linear operators studied in approximation theory. Formulas which could be very useful for any future study devoted to the properties of these linear positive operators. Subsequently, Chap. 3 is concerned with the presentation of approximation properties of certain integral type operators.

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