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# Probability in Banach Spaces 6

*Proceedings of the Sixth International  
Conference, Sandbjerg, Denmark 1986*

U. Haagerup  
J. Hoffmann-Jørgensen  
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## Preface

This volume contains a selection of papers by the participants of the 6. *International Conference on Probability in Banach Spaces, Sandbjerg, Denmark, June 16–21, 1986*. The conference was attended by 45 participants from several countries. One thing makes this conference completely different from the previous five ones, namely that it was arranged jointly in Probability in Banach spaces and Banach space theory with almost equal representation of scientists in the two fields. Though these fields are closely related it seems that direct collaboration between researchers in the two groups has been seldom. It is our feeling that the conference, where the participants were together for five days taking part in lectures and intense discussions of mutual problems, has contributed to a better understanding and closer collaboration in the two fields.

The papers in the present volume do not cover all the material presented in the lectures; several results covered have been published elsewhere.

The sponsors of the conference are:

The Carlsberg Foundation,  
The Danish Natural Science Research Council,  
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The participants and the organizers would like to thank these institutions for their support.

The Organizers.

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