

# The Economic Value of Information



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With 45 Figures



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*To Gail, Sarah, and Dan*

# Preface

## **The Scope of This Book**

Popular culture often refers to current times as the Information Age, classifying many of the technological, economic, and social changes of the past four decades under the rubric of the Information Revolution. But similar to the Iron Age before it, the description “Information Age” suggests the idea that information is a commodity in the marketplace, one that can be bought and sold as an item of value. When people seek to acquire information yet complain about information overload, and when organizations invest millions in information systems yet are unable to pinpoint the benefits, perhaps this reflects a difficulty with the assessment of the value of this commodity relative to its cost, an inability to discern the useless from the useful from the wasteful. The Information Age requires us to assess the value, cost, and gain from information, and to do it from several different viewpoints.

At the most elementary level is the individual who perceives a need for information—her current state of knowledge is insufficient and something needs to be understood, or clarified, or updated, or forecast. There is a universe of alternative information sources from which to choose, some more informative than others, some more costly than others. The individual’s problem is to evaluate the alternatives and choose which sources to access.

An organization comprising many information-seeking employees and agents must take a somewhat broader viewpoint. The organization’s problem is to design and manage a system for information that can meet the needs of diverse groups of individuals as those needs arise, while maximizing the organization’s net gain from the services the system provides.

This is a book about the evaluation and choice of information sources by individuals and the design and management of information systems by organizations. These topics are unified by the thesis that both information sources and information systems are valuable to the extent they contribute to better decision making. Since the incorporation of information is costly in terms of money, time, and effort, optimal information use and system design involves classic economic tradeoffs between value and cost. This book studies the determinants of the value and cost of information, both to the individual and to the organization, provides techniques for the assessment of the value of information and the com-

parison of informativeness among alternative sources, and presents principles for the optimal design and management of information systems.

Decision theory is a ready-made methodology for assessing the economic value of information. Since many activities can be cast into a decision making framework, applications of decision theory are widespread, ranging from the notorious [the Ford Pinto gas tank decision, Gioia (1992)] to the nutritious [the foraging decisions of bumblebees, Real (1993)]. Applications of decision theory to the evaluation of information appear in such diverse scientific disciplines as accounting, economics, engineering, environmental science, geology, information science, management information systems, medical science, meteorology, operations research, psychology, and statistics. As Chapter 1 demonstrates, nowadays the applications are becoming more multidisciplinary in nature—decisions to study the banning of a potential carcinogen or the consequences of global warming necessarily require contributions from many fields.

Unfortunately, much of the existing literature tends to be highly specialized and technical, with little notational uniformity. Even basic words such as data, knowledge, information, and information system have different meanings in different contexts. An integrative understanding of the many aspects of information evaluation, choice, and system design requires consistency and precision in the definition of terms. One of the purposes of this book is to provide students and researchers with a unified and coherent notation and approach to this diverse multidisciplinary literature.

Research described in Chapter 9 indicates that as individuals and teams face more complex and multidisciplinary decision problems, the role of the information system becomes more critical. It is my belief that decision theory has not yet achieved its potential as a tool for corporations, governments, and other organizations to use when evaluating their information systems. One of the goals of this book is to improve the integration of the decision-theoretic approach to information value with the knowledge from information science on the design, management, and cost of cooperative information systems.

This book concentrates on a subset of a vast literature known collectively as the economics of information. The focus is on the evaluation and incorporation of information by a single decision maker, and on the cooperative facilitation of that task by an organization; with only a few exceptions, strategic and noncooperative uses of information, along with the market consequences of differential information, are excluded.

## **A Reader's Guide**

The basic plot of this book is to move from the assessment of the economic value of a specific source, to the choice of source or sources, to the design of an organization's system for information. Although the mathematical prerequisite

for the material is no more than undergraduate courses in calculus and probability theory, there may be different ways to read this book depending upon the reader's background and interest. A student who desires to learn decision theory and its application to the evaluation of information will find Chapters 1 through 4, Sections 5.1, 5.2, 5.4, 6.1, 6.2, 7.1, 7.3, and 8.1 to be most helpful. The reader interested primarily in information systems will find Chapters 1 and 9 most pertinent. Indeed, the book is written so that those interested primarily in information science can skip directly from Chapter 1 to Chapter 9 without loss, picking up the material in between as need be. Researchers who are already familiar with decision theory and who are interested in a particular application or in the more theoretical aspects of information value will find this in Chapters 5 through 8. The primarily technical and mathematical material of this book is constrained to these four chapters; there is a detailed symbol glossary beginning on page 365 to help with the notation. Subsections that are marked with an asterisk (\*) contain either peripheral or highly technical material that can be bypassed without loss of continuity.

The ideas and techniques are illustrated throughout the book by means of examples which are set off from the text by black diamonds (♦). Since they may continue through several chapters, the examples are numbered according to the section in which they first appear: Example 4.2 first appears in Section 4.2. Each example hones in on the substance of the most recently introduced topic; the purpose is to fix ideas and not to provide immediate generality. The proximate text, however, presents citations for models and theories that offer more general, technical, complex, or realistic applications.

The book holds to a number of conventions throughout. The first definition of an important term is indicated by placing that term in italics. In equations, parentheses () always denote functional dependence, and brackets [] and braces {} always indicate separation for arithmetic operation. Finally, the protagonist in this book is the decision maker. The decision maker is considered to be a person and it is convenient to use a pronoun for reference; in many languages such pronouns are indicative of gender. We can use that to our advantage by adopting the following convention from the principal-agent literature: in this book the decision maker is the principal and so is always referred to as "she," and the information source, when human, is the agent and so is always "he."

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tion, but because of depth, rigor, and clarity, in my view the greatest contributor is Jacob Marschak (1974). “It’s all in Marshall” students of microeconomic theory often say; students of the economics of information and organization can equally say, “It’s all in Marschak!” I would also like to thank Karl A. Fox, who introduced me to the topic, Anne Mayère of ENSSIB, whose 1995 conference on the economics of information stimulated me in several directions, and Drake University, whose generous sabbatical policy gave me the time to do this work. Special appreciation and love go to Gail, Sarah, and Dan, who tolerated a lot and to whom this book is dedicated. Finally, there are the people who put me on the right track from the very beginning: Alpha, Louise, George, Jackie, George, Annette, and Doug. Thank you.

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Des Moines, Iowa  
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# Contents

1.	Introduction and Overview	1
1.1	Information in Decision Making	1
1.1.1	The Basic Framework for Decision	1
1.1.2	Information and Information Sources	2
1.1.3	Statistical and Pragmatic Information	5
1.1.4	Ex-Post Value and Gain	6
1.2	Information in the Organization	7
1.2.1	Information Systems	7
1.2.2	User Information Processing	8
1.2.3	Information System Accounting	11
1.3	Economics of the Incorporation of Information	12
1.3.1	The Criterion	12
1.3.2	Ex-Ante Components of Decision Making	13
1.4	The Expected Value of an Information Source	15
1.4.1	Information Structure and Informativeness	15
1.4.2	The Measurement of Information Value: Chapters 2 and 3	16
1.4.3	The Assessment of Information Value: Chapters 4 and 5	18
1.4.4	Case Studies of Information Value	20
1.4.5	The Theory of Information Value: Chapters 6 and 7	25
1.5	Information Value, Cost, and Procurement	28
1.5.1	The Optimal Information Structure	28
1.5.2	Procuring Direct Information	32
1.5.3	Case Studies of Information Cost, Value, and Choice	33
1.6	System Design for Information Gain	35
1.6.1	Decision Theory, Information Science, and System Design	35
1.6.2	Information Use Environments	37
1.6.3	A Model of System Design and User Behavior	38
1.7	Information Social Science	39
1.7.1	The Information Society	39
1.7.2	How Monumental Are Recent Events?	41
2.	The Value of the Informed Decision	45
2.1	Elements of a Decision Problem Under Uncertainty	45

2.1.1	Utility of Outcome	45
2.1.2	Decision Problems	46
2.1.3	Decision Making	49
2.2	The Framing of the Decision Problem	53
2.2.1	Practical Issues in Framing	53
2.2.2	Framing the State Space and Initial Knowledge	55
2.2.3	The Incorporation of Information	57
2.3	Useful Facts About Statistical Information	58
2.3.1	Statistical Properties of the Information Structure	58
2.3.2	The Finite Model	59
2.3.3	Some Specific Expectations	60
2.4	Value of the Informed Decision	65
2.4.1	Extensive Form Analysis	65
2.4.2	Perfect Information	69
2.4.3	Worthless Information	70
3.	Measures of the Value of Information	73
3.1	Measures of the Value of a Message	73
3.1.1	Cash-Equivalent Values of a Decision	73
3.1.2	Value of Decisions Posterior to the Message	78
3.1.3	The Simplest Special Case	81
3.1.4	Two Examples	82
3.1.5	The Need for Preposterior Evaluation	88
3.2	Measures of the Value of a Source	89
3.2.1	Incremental Value from Incorporating Information	89
3.2.2	The Range of the Expected Value of Information	91
4.	The Assessment of Statistical Information	95
4.1	Coherent Assessment of Probability Distributions	95
4.1.1	Coherence and Consistency	95
4.1.2	Families of Probability Densities	97
4.2	Assessment of Beliefs and Foreknowledge	100
4.2.1	Assessing a Univariate Distribution	100
4.2.2	Obtaining Qualitative Foreknowledge of Information	103
4.2.3	Expert Resolution	106
4.2.4	Analysis of a Track Record	107
4.3	Simplifying the Assessment	113
4.3.1	The Preposterior Mean	114
4.3.2	The Calibrated Noiseless Model	115
5.	Models with Convenient Assessment and Interpretation	117
5.1	Models with Payoff Quadratic in the Action	117
5.1.1	The General Case	118

5.1.2	The Bivariate Normal Case	119
*5.1.3	The Quadratic Team	121
5.2	Models with Payoff Linear in the State	122
5.2.1	Raiffa and Schlaifer's Approach	123
5.2.2	Application to Statistical Decision Problems	127
5.2.3	Application in a Dichotomy	131
5.2.4	The Inventory Problem	133
5.3	Models with Concave-Exponential Utility	136
5.3.1	Information Value with Separable Outcome	136
5.3.2	Applications with the Bivariate Normal Information Structure	138
5.4	Models with Nonseparable Outcome; Betting and Investing Models	141
5.4.1	Nonseparability and Information Value: Two Examples	141
5.4.2	Arrow's Contingent Securities Model	145
5.5	Models with Multicategorical State Description	147
5.5.1	Multicategorical Information Structures	148
5.5.2	Bidding Models	148
5.6	Dynamic Models and the Role of Timeliness	155
5.6.1	Dynamic Decision Problems	156
5.6.2	Delay	159
5.6.3	The Value of Timeliness and Accuracy	160
*5.6.4	Assessing the Joint Distribution of Messages and States Via the Kalman Filter	163
5.6.5	Stochastic Control Theory	166
5.7	Approximations and Bounds for the Value of Information	166
*5.7.1	Use of the Taylor Series Expansion	167
5.7.2	Bounds for Stochastic Programming Problems	169
5.7.3	Approximating Information Value by Sampling	173
6.	Statistical Determinants of Information Value	177
6.1	The Normal Form of Decision Analysis	177
6.1.1	Randomized Courses of Action	178
6.1.2	Decision Rules	179
6.1.3	Utility Possibilities and Admissibility	184
6.1.4	The Finite Model in Normal Form	190
6.1.5	Convexity in the Probabilities	192
6.2	Comparative Informativeness	197
6.2.1	The Relation "More Informative Than"	197
6.2.2	Blackwell's Theorem	199
6.2.3	Special Cases	204

6.2.4	Constructing a Sequence of Structures Ranked by Informativeness	209
6.3	Informativeness, Prior Knowledge, and Value	213
6.3.1	The Value of Statistical Informativeness: The Binary Case	214
6.3.2	The Value of Systematic Redistribution of the Probability: Stochastic Dominance	218
*6.3.3	The Differential Approach to the Value of Statistical Informativeness	224
*6.3.4	Environmental Uncertainty	226
7.	Stochastic Preference and Information Value	231
7.1	Prospects and Attitude Towards Risk	231
7.1.1	Prospects Induced by Actions	232
7.1.2	Cash Summarizations for Optimal Prospects	234
7.1.3	Attitude Towards Risk	242
7.2	Risk Preference and Information Value	247
7.2.1	Comparison of the Risk Averter's Optimal Prospects with the Risk Neutral Benchmark	248
7.2.2	Bounds on the Comparative Demand Value of Information	248
7.3	Nonlinear Models and Information Aversion	256
7.3.1	The Expected Utility Criterion	256
7.3.2	Troubles with the Expected Utility Model	259
7.3.3	Aversion to Information	261
8.	Information Demand and Procurement	265
8.1	The Demand for Information	265
8.1.1	The Value of the Costly Informed Decision	265
8.1.2	Economic Consequences of Differential Information	270
8.1.3	Optimal and Suboptimal Information Possession	272
8.2	Information Procurement	276
8.2.1	The Informant as Agent of the DM	277
8.2.2	The Framework and Primary Assumptions	279
8.2.3	The Contract Design Problem	281
8.3	Optimal Incentive Contracts to Procure Information	284
8.3.1	The Expected Value of Information	284
8.3.2	The Optimal Contract Design	287
8.3.3	Implementation	290
8.3.4	Examples	292
*8.3.5	Proofs of Lemmas 2, 3, and 4	296
9.	Economics of Valuable Information Systems	299
9.1	Information Use Environments	299

9.1.1	Business Environments	300
9.1.2	Scientific and Technical Environments	303
9.1.3	User Assessment of Information Value	305
9.2	System Design and Information Gain	307
9.2.1	The Gain-Producing Activities of an Information System	308
9.2.2	System Data Processing	310
9.2.3	Design and Performance	317
9.3	Experiments in Ex-Ante Information Behavior	319
9.3.1	Normative and Descriptive Economics	319
9.3.2	Experiments in Information Acquisition	321
9.3.3	Experiments in Value Assessment	325
9.4	A Decision-Theoretic Model for System Design	328
9.4.1	The Framework	328
9.4.2	A Theory of Information Production and Cost	330
9.4.3	Information Gain in a Canonical Decision Problem	333
9.4.4	Reported Results from a Survey	336
9.4.5	Characterization of the Organization's Optimal System	340
9.5	Postlude	342
	References	345
	Acknowledgments	365
	Symbol Glossary	367
	Author Index	375
	Subject Index	383