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# Multiphysics Simulation

Electromechanical System Applications  
and Optimization

 Springer

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# Foreword

It was 1986, at the Technical University of Denmark, when Prof. Martin Bendsøe and I were working on ‘topology’ optimization in structural design by finding an optimal distribution of a linearly elastic porous microstructure defined by infinitely many very small-scale rectangular holes, which are appropriately rotated. To deal with a linearly elastic porous material defined by infinitely many small-scale rectangular holes (characterized by width,  $a$ , and height,  $b$ , in a unit cell with rotation,  $\theta$ ), we applied the homogenization method to calculate the equivalent macro-scale linearly elastic constitutive relation,  $\sigma = \mathbf{C}^H(a, b, \theta)\varepsilon$ . Instead of rectangular holes, square holes were assumed characterizing size,  $a$ , in the unit cell, and the elasticity matrix,  $\mathbf{C}^H(a, b, \theta)$ , was simplified to  $\mathbf{C}^H(a, \theta)$ . If rotation of micro-scale holes is not considered, then this problem is simplified even further as  $\mathbf{C}^H(a)$ . If  $a = 1$ , then the unit cell is completely occupied with a hole, that is, it is equivalent to no material in the macro-scale ‘porous’ structure. On the other hand, if  $a = 0$ , then the unit cell is completely occupied with elastic material, that is, it represents solid material in the macro-scale ‘porous’ material. Shape and topology of a solid structure, then may be defined by the portion where  $a < 1$  in the unit cell. In other words, topology and shape optimization problems are transferred to finding the optimal distribution of porosity, that is, the optimal distribution of a solid material. This idea was published in the paper Bendsøe and Kikuchi [1] and then its concept was extensively extended by Bendsøe [2], Bendsøe and Sigmund [3].

In these books, we can find applications not only in elastic structures, but in heat conduction and also in fluid mechanics. However, at present, a dependable monograph cannot be found on topology optimization for electromagnetism and its industrial applications, which are now very critical to developing various advanced electrical/magnetic devices even for automobiles.

Thus, I have encouraged the writing of such a monograph to researchers at the Toyota Research Institute of North America, Ann Arbor, Michigan, USA, where the topology optimization approach is widely taken as a design tool for many

devices and structures for automobiles. It is my great pleasure to endorse this monograph to many talented graduate students and researchers in the field of electromagnetism and its related applications in design.

April 2014

Noboru Kikuchi

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# Preface

This book developed out of a collaboration by the authors at the Toyota Research Institute of North America, where multiphysics simulation and optimization is used on a daily basis for a variety of engineering studies related to electromechanical systems. Multiphysics simulation is a rapidly growing field, and the term itself is broad and may be applied to an extremely wide variety of coupled-physics problems. By nature, multiphysics simulation requires an array of technical skills in different intersecting disciplines. As such, this book aims to narrow down the topic by specifically focusing on multiphysics simulation for electromechanical systems, the original target application investigated by the authors. It is our hope that the collaborative aspects of such studies become apparent as the various technical topics throughout the book are presented.

## Overview

Understanding and predicting the performance of electromechanical systems is of prime importance in the design of many of today's key products including computers, vehicles and consumer electronics. In these systems, increased efficiency and higher power density in a smaller package size is crucial. Success in design requires both analytical and numerical skills plus a foundation in mechanical and electrical engineering. Efficient analysis also necessitates an understanding of how best to build a numerical model that is accurate yet balances complexity and computational cost.

Beyond basic performance prediction, today's engineers and researchers are constantly seeking methods for optimizing complex electromechanical systems. The multiphysics aspects of these systems present constant challenges in terms of how best to arrive at an 'optimal solution.' Many optimization techniques exist, although the use of structural topology optimization is emphasized herein along with some aspects of discrete parameter optimization.

## Organization and Features

Accordingly, this book highlights a unique combination of numerical tools including numerous strategies for handling the aforementioned simulation challenges. In [Chap. 1](#), the concept of design via simulation is introduced along with the role of multiphysics simulation in today's engineering environment. The importance of structural optimization techniques in the design and development of electromechanical systems is additionally discussed. From there, an overview of the physics commonly involved with electromechanical systems is provided ([Chap. 2](#)) for applications such as electronics, magnetic components, radio frequency components, actuators and motors. Governing equations for the simulation of related multiphysics problems are reviewed in [Chap. 3](#), while the relevant topology optimization and parametric size analysis methods for electromechanical systems are outlined in [Chap. 4](#). Several multiphysics simulation and optimization example studies in both two and three-dimensions are then described in detail throughout [Chap. 5](#). Extensions to new topics are suggested in [Chap. 6](#). Sample numerical code for a related electro-thermal topology optimization example is provided in the appendix in [Chap. 7](#).

A challenge in writing a book of this nature on the topic of multiphysics simulation is the preparation of the engineering nomenclature used for various physical constants, state variable, functions, etc. Specifically, the governing equations for the multitude of separate physical processes are often described using the same symbols for different variables. As such, every effort has been made to provide a comprehensive list of nomenclature with distinct variable usage wherever possible.

In addition to the above features, extensive references are provided at the end of each chapter. These references are related to prior research on multiphysics simulation and optimization methods, techniques, and application studies.

## Target Audiences

It is our hope that the content presented in this book will serve as a reference for industry and academic researchers and engineers in the field of advanced electromechanical system design. The topics in this book are appropriate for undergraduate and graduate level students, although many of the design examples may be of interest to anyone curious about the unique design solutions that arise when optimization methods are coupled with multiphysics simulation strategies.

## Acknowledgments

We would like to thank our colleagues at the Toyota Research Institute of North America (TRINA), Korea Aerospace University, and Toyota Central Research and Development Labs (TCRDL), for their support in the completion of this project.

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Ann Arbor, April 2014  
Goyang

Ercan M. Dede  
Jaewook Lee  
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# Contents

<b>1</b>	<b>Introduction</b>	1
1.1	Design via Simulation	1
1.2	Single Physics Versus Multiphysics Simulation	3
1.3	Challenges of Multiphysics Simulation	5
1.4	The Role of Structural Optimization Methods	6
1.4.1	Topology Optimization	7
1.4.2	Size and Shape Optimization	8
	References	9
<b>2</b>	<b>Overview of Physics for Electromechanical Systems</b>	11
2.1	Electronic System Components	12
2.2	Magnetic Components	14
2.3	RF Components	15
2.4	Motors and Actuators	17
	References	19
<b>3</b>	<b>Governing Equations for Electromechanical Systems</b>	21
3.1	Single Physics Structural Mechanics Example	21
3.2	Joule Heating	25
3.3	Thermal Stress	27
3.4	Conjugate Heat Transfer	28
3.5	Low Frequency Electromagnetics	30
3.6	High Frequency Electromagnetics	34
	References	39
<b>4</b>	<b>Optimization Methods for Electromechanical Systems</b>	41
4.1	Topology Optimization	41
4.1.1	Level Set Function Approach	52
4.2	Parametric Size Analysis	55
	References	57

**5 Electromechanical System Simulation and Optimization Studies . . . . . 61**

5.1 Electronic System Component Analysis and Design . . . . . 62

    5.1.1 Design Optimization of Electrothermal Systems . . . . . 63

    5.1.2 Design Optimization of Thermal-Structural Systems . . . . . 68

    5.1.3 Design Optimization of Thermal-Fluid Systems . . . . . 76

    5.1.4 Design Optimization of Thermomagnetic Convective Systems . . . . . 90

    5.1.5 Design Optimization of Thermal Composites . . . . . 100

5.2 Magnetic Component Analysis and Design . . . . . 113

    5.2.1 Multiphysics Analysis of Magnetic Components . . . . . 114

    5.2.2 Analysis Example: 2-D Inductor Model . . . . . 116

    5.2.3 Design Optimization of 2-D Inductor . . . . . 119

5.3 RF Component Analysis and Design . . . . . 123

    5.3.1 Design Optimization of Microstrip Device . . . . . 124

    5.3.2 Design Optimization of Dielectric Resonator Antenna . . . . . 132

5.4 Actuator Analysis and Design . . . . . 149

    5.4.1 Design Optimization for Magnetostructural Coupling . . . . . 150

    5.4.2 Simultaneous Design Optimization of Permanent Magnet, Coils, and Ferromagnetic Material . . . . . 157

5.5 Electric Motor Analysis and Design . . . . . 168

    5.5.1 Design Optimization of Switched Reluctance Motors . . . . . 168

    5.5.2 Multiphysics Analysis of Interior Permanent Magnet Motors . . . . . 178

References . . . . . 183

**6 Extensions to New Topics . . . . . 189**

6.1 Scaling-Up of Systems . . . . . 189

6.2 Treatment of Surfaces and Interfaces . . . . . 191

6.3 Free Versus Constrained Systems-Toward Manufacturability . . . . . 192

References . . . . . 196

**7 Appendix: Sample Multiphysics Optimization Code . . . . . 199**

7.1 MATLAB<sup>®</sup> Example Program for Multiphysics Topology Optimization of Electrothermal Systems . . . . . 200

References . . . . . 208

**Index . . . . . 209**

# Acronyms

2-D	Two-dimensional
3-D	Three-dimensional
ABC	Absorbing boundary condition
AC	Alternating current
ALE	Arbitrary Lagrangian–Eulerian
AVM	Adjoint variable method
BC	Boundary condition
CAD	Computer-aided design
CAE	Computer-aided engineering
CFD	Computational fluid dynamics
CTE	Coefficient of thermal expansion
CVW	Coulomb Virtual Work
DARPA	Defense Advanced Research Projects Agency
DBC	Direct bonded copper
DC	Direct current
DOF	Degrees-of-freedom
DRA	Dielectric resonator antenna
EMC	Electromagnetic compatibility
EMI	Electromagnetic interference
FDTD	Finite difference-time domain
FEA	Finite element analysis
FE-BI	Finite element-boundary integration
FEM	Finite element method
GA	Genetic algorithm
HPC	High performance computing
HV	Hybrid vehicle
IC	Integrated circuit
IPMSM	Interior permanent magnet synchronous motor
LSM	Level set method
MEMS	Microelectromechanical systems
MMA	Method of Moving Asymptotes
MST	Maxwell Stress Tensor
NASA	National Aeronautics and Space Administration
OC	Optimality criteria

PCB	Printed circuit board
PDE	Partial differential equation
PEC	Perfect electric conductor
PM	Permanent magnet
PML	Perfectly matched layer
PSO	Particle swarm optimization
RF	Radio frequency
RMS	Root mean square
RPM	Revolutions per minute
SAR	Specific absorption rate
SAW	Surface acoustic wave
SIMP	Solid isotropic material with penalization
SLP	Sequential linear programming
SRM	Switched reluctance motor
TBC	Transition boundary condition
TEM	Transverse electric and magnetic
TIM	Thermal interface material
US	United States

# Symbols

## Scalar Quantities

$A_s$	Surface area
$B$	Magnitude of magnetic flux density
$B_r_{PM}$	Permanent magnet strength
$B_{rx}$	$x$ -direction component of residual magnetic flux density
$B_{ry}$	$y$ -direction component of residual magnetic flux density
$C$	Curie constant
$C_p$	Specific heat capacity
$D$	Extended design domain
$E$	Elastic (or Young's) modulus
$F$	Force
$f$	Frequency
$f_i$	Inclusion volume fraction
$g$	Behavior constraint
$H$	Magnitude of magnetic field
$h$	Surface convection coefficient
$h_c$	Channel height
$h_t$	Heaviside function transition bandwidth
$I, i$	Electric current
$J$	Electric current density
$k$	Thermal conductivity
$k_h$	Hysteresis coefficient
$L$	Inductance
$l$	Mechanical compliance
$M_w$	Molecular weight
$N$	Nodal shape function
$N_c$	Number of coils
$P$	Pressure
$p$	Penalization parameter
$P_r$	Number of rotor poles
$P_s$	Number of stator poles
$\mathcal{P}$	Power

$Q$	Volumetric power density
$q$	Convex interpolation tuning parameter
$q''$	Heat flux
$R$	Electrical resistance
$R_f$	Helmholtz filter radius
$R_{th}$	Thermal resistance
$R''_{th}$	Unit thermal resistance
$R_{th(cnv)}$	Convective thermal resistance
$Re$	Reynolds number
$\mathcal{R}$	Residual
$S$	Scattering parameter
$s$	Adaptive scaling factor
$T$	Temperature
$t$	Time
$\mathcal{T}$	Torque
$u$	Displacement
$V$	Voltage drop
$v$	Volume
$v_e$	Element volume
$W$	Energy or work
$W_{co}$	Co-energy
$W_{mag}$	Magnetic energy
$w$	Objective function weighting value
$w_c$	Channel width
$Z_s$	Surface impedance
$\alpha$	Coefficient of thermal expansion
$\alpha_i$	Inclusion aspect ratio
$\tilde{\alpha}$	Inverse permeability
$\chi$	Fluid magnetic susceptibility
$\delta\varepsilon$	Virtual strain
$\delta U$	Virtual strain energy
$\delta W$	Virtual work
$\Delta P$	Pressure drop
$\epsilon$	Electric permittivity
$\epsilon_o$	Electric permittivity of free space
$\epsilon_b$	Bandwidth for smoothed surface convection coefficient function
$\eta$	Fluid dynamic viscosity
$\gamma$	Optimization design (density) variable
$\lambda_{link}$	Magnetic flux linkage
$\mu$	Magnetic permeability
$\mu_o$	Magnetic permeability of free space
$\mu_r$	Relative magnetic permeability
$\mu_{r\_mf}$	Magnetic fluid permeability

$v$	Poisson's ratio
$\Omega$	Domain
$\Omega_d$	Design domain
$\Omega_m$	Material domain
$\omega$	Angular frequency or velocity
$\Phi$	Electric scalar potential
$\Phi_B$	Magnetic flux
$\rho$	Density
$\rho_e$	Electric resistivity
$\rho_q$	Electric charge density
$\zeta$	Electric conductivity
$\theta$	Inclusion angle
$\theta_r$	Rotor angle
$\zeta$	Channel aspect ratio
Vector, Matrix, or Tensor Quantities	
<b>A</b>	Magnetic vector potential
<b>B</b>	Magnetic flux density
<b>B<sub>r</sub></b>	Residual magnetic flux density
<b>B<sub>e</sub></b>	Array of derivatives of element nodal shape functions
<b>C</b>	Stiffness tensor
<b>D</b>	Electric displacement
<b>E</b>	Electric field
$\mathbb{E}$	Electric field variable
$\hat{\mathbf{e}}$	Target unit vector
<b>F, f</b>	Force (global, element)
<b>H</b>	Magnetic field
<b>J</b>	Electric current density
<b>J<sub>e</sub></b>	External current density
<b>J<sub>eddy</sub></b>	Eddy current density
<b>K, k</b>	Stiffness matrix (global, element)
$\hat{\mathbf{n}}$	Normal unit vector
<b>Q</b>	Magnetic load vector
<b>q</b>	Heat flux vector
<b>t</b>	Surface load vector
$\hat{\mathbf{t}}$	Tangential unit vector
<b>U, u</b>	Displacement (global, element)
<b>v</b>	Velocity
<b>x</b>	Position
<b>δu</b>	Virtual displacement
$\varepsilon$	Strain
$\hat{\lambda}$	Lagrange multipliers (adjoint variables)
$\sigma$	Stress

## Functions

 $F_o$  $F_c$  $H$  $\tilde{H}$  $L$  $\phi$  $\psi$  $\tilde{\psi}$ 

## Subscripts

avg

 $d$  $F, f$ 

in

init

 $l$  $M$ 

max

min

 $o$ 

out

 $S$  $s$  $T$  $u$ 

Optimization objective function

Convergence function

Heaviside function

Regularized Heaviside function

Lagrangian

Level set function

Scalar function

Filtered scalar function

Average

Distributed

Fluid

Inlet

Initial

Lower

Magnetic

Maximum

Minimum

Reference value

Outlet

Structural

Solid

Thermal

Upper