

Notations

C	positive constants in estimates, which may change their value from term to term.
t^+	$\max\{t, 0\}$ for $t \in \mathbb{R}$.
t^-	$\max\{-t, 0\}$ for $t \in \mathbb{R}$.
$a_k \sim b_k$	$\lim_{k \rightarrow \infty} \frac{a_k}{b_k} = 1$.
\mathbb{N}	$= \{0, 1, 2, 3 \dots\}$.
\mathbb{N}^+	$= \{1, 2, 3 \dots\}$.
n	space dimension.
\mathbb{R}_+^n	$= \{x \in \mathbb{R}^n : x_1 > 0\}$, half space.
Ω	domain, an open and connected subset of \mathbb{R}^n .
$\partial\Omega$	$\overline{\Omega} \cap \overline{\mathbb{R}^n \setminus \Omega}$, the boundary of Ω .
$\Omega_0 \subset\subset \Omega$	$\overline{\Omega_0}$ is compact and $\overline{\Omega_0} \subset \Omega$.
A^c	for $A \subset \Omega$: complement of A in Ω , $\Omega \setminus A$.
$d\omega$	surface element for $\partial\Omega$.
ν	exterior unit normal at $\partial\Omega$.
$B_r(x)$	open ball with radius r and centre x .
B	$= B_1(0)$, open unit ball in \mathbb{R}^n .
\mathbb{S}^{n-1}	$= \partial B \subset \mathbb{R}^n$, unit sphere.
e_n	$= \frac{\pi^{n/2}}{\Gamma(1+n/2)}$, volume of the n -dimensional unit ball $B \subset \mathbb{R}^n$. So ne_n is the $(n-1)$ -dimensional measure of the unit sphere.

$d(x)$	$= \text{dist}(x, \partial\Omega)$, for $x \in \Omega$.
$d(x)$	$= 1 - x $, for $x \in B$.
$[XY]$	$= \left x y - \frac{x}{ x } \right $, for $x, y \in B$.
r	$= x $, $x \in \mathbb{R}^n$.
D_{i_1, \dots, i_k}	$= \frac{\partial^k}{\partial x_{i_1} \cdots \partial x_{i_k}}$.
α, β	multiindices $\in \mathbb{N}_0^n$, $ \alpha = \sum_{i=1}^n \alpha_i$.
D^α	$= \prod_{i=1}^n \left(\frac{\partial}{\partial x_i} \right)^{\alpha_i}$ with $ \alpha = \sum_{i=1}^n \alpha_i$.
$C_c^\infty(\Omega)$	space of $C^\infty(\Omega)$ -functions having compact support in Ω .
$W^{m,p}(\Omega)$	Sobolev space of the m -times weakly differentiable functions in Ω with L^p -derivatives.
$D^k u \cdot D^k v$	$= \sum_{i_1, \dots, i_k=1}^n \frac{\partial^k u}{\partial x_{i_1} \cdots \partial x_{i_k}} \cdot \frac{\partial^k v}{\partial x_{i_1} \cdots \partial x_{i_k}}$.
$ D^k u $	$= \left(D^k u \cdot D^k u \right)^{1/2}$.
$\ u\ _{W^{m,p}}$	$= \left(\ u\ _{L^p(\Omega)}^p + \ D^m u\ _{L^p(\Omega)}^p \right)^{1/p}$.
$\ u\ _{W_0^{m,p}}$	$= \ D^m u\ _{L^p(\Omega)}$.
$W_0^{m,p}(\Omega)$	in bounded domains Ω , closure of $C_c^\infty(\Omega)$ with respect to the norm $\ \cdot\ _{W_0^{m,p}}$.
$W_0^{m,p}(\Omega)$	in any domain Ω , closure of $C_c^\infty(\Omega)$ with respect to the norm $\ \cdot\ _{W^{m,p}}$.
$\mathcal{D}^{m,p}(\Omega)$	in unbounded domains Ω , closure of $C_c^\infty(\Omega)$ with respect to the norm $\ \cdot\ _{W_0^{m,p}}$.
$H^m(\Omega)$	$= W^{m,2}(\Omega)$.
$H_0^m(\Omega)$	$= W_0^{m,2}(\Omega)$.
$H_\partial^m(\Omega)$	$= \left\{ v \in H^m(\Omega); \Delta^j v = 0 \text{ on } \partial\Omega \text{ for } j < \frac{m}{2} \right\}$.
$H^{-m}(\Omega)$	dual space $(H_0^m(\Omega))'$.

$\ u\ _{H_0^m}^2$	$= \sum_{i_1, \dots, i_m=1}^n \int_{\Omega} D_{i_1, \dots, i_m} u ^2 dx = (\text{see (2.12)})$
	$= \begin{cases} \int_{\Omega} (\Delta^{m/2} u)^2 dx & \text{if } m \text{ is even,} \\ \int_{\Omega} \nabla \Delta^{(m-1)/2} u ^2 dx & \text{if } m \text{ is odd.} \end{cases}$
$(\cdot, \cdot)_{H_0^m}$	corresponding scalar product in $H_0^m(\Omega)$.
$\ u\ _{\mathcal{G}^{m,2}}^2$	$= \begin{cases} \int_{\Omega} (\Delta^{m/2} u)^2 dx & \text{if } m \text{ is even,} \\ \int_{\Omega} \nabla \Delta^{(m-1)/2} u ^2 dx & \text{if } m \text{ is odd.} \end{cases}$
$(\cdot, \cdot)_{\mathcal{G}^{m,2}}$	corresponding scalar product in $\mathcal{G}^{m,2}$.
$\langle f, u \rangle$	dual pairing: $u \in$ Banach space, $f \in$ its dual.
$\Lambda_{m,j}$	j -th Dirichlet-eigenvalue of $(-\Delta)^m$, according to its multiplicity.
φ_j	corresponding eigenfunctions, orthonormal in $H_0^m(\Omega)$.
$G_{m,n}, \mathcal{G}_{m,n}$	Green's function, Green's operator, resp. for $(-\Delta)^m$ under Dirichlet boundary conditions in $B \subset \mathbb{R}^n$.
$G_{(-\Delta)^m, \Omega}, \mathcal{G}_{(-\Delta)^m, \Omega}$	the same for $\Omega \subset \mathbb{R}^n$.
$G_{m,n,\mathcal{A}}, \mathcal{G}_{m,n,\mathcal{A}}$	the same for $(-\Delta)^m + \mathcal{A}$ in $B \subset \mathbb{R}^n$, where $\mathcal{A}u = \sum_{ \alpha \leq 2m-1} a_{\alpha} D^{\alpha} u$.
$G_{(-\Delta)^m, \Omega, \mathcal{A}}, \mathcal{G}_{(-\Delta)^m, \Omega, \mathcal{A}}$	the same in $\Omega \subset \mathbb{R}^n$.
s	$= \frac{n+2m}{n-2m}$, for $n > 2m$; critical Sobolev exponent.
For measurable functions f, g :	
$f > 0$	$f(x) > 0$ for almost all x .
$f > g$	$f - g > 0$.
$f \not\geq 0$	$f(x) < 0$ for x in a set of positive measure.
$f \not\geq g$	$f - g \not\geq 0$.
$f \not\equiv 0$	$f(x) \neq 0$ for x in a set of positive measure and $f(x) \geq 0$ for almost all x .
$f \not\equiv g$	$f - g \not\equiv 0$.
$f(t) \simeq g(t)$	$\exists C > 0 \forall t : \frac{1}{C} f(t) \leq g(t) \leq C f(t)$; for $f, g \geq 0$.
$f(t) \preceq g(t)$	$\exists C > 0 \forall t : f(t) \leq C g(t)$, for $f, g \geq 0$.
Ω^*	a ball centered at the origin such that $ \Omega = \Omega^* $.

u^*	spherical rearrangement of a measurable function u , see Definition 3.10.
$(g_{ij})_{i,j=1,\dots,n}$	Riemannian metric, positive definite tensor. In case of parametrisations X in \mathbb{R}^3 over a two dimensional parameter domain: $g_{ij} = \partial_i X \cdot \partial_j X$.
g	$= \det((g_{ij})_{i,j=1,\dots,n})$, Gram's determinant.
$(g^{ij})_{i,j=1,\dots,n}$	inverse of the metric tensor.
$(L_{ij})_{i,j=1,\dots,n}$	second fundamental form. In case of parametrisations X in \mathbb{R}^3 over a two dimensional parameter domain:

$$L_{ij} = \frac{1}{\sqrt{g}} \det(\partial_i \partial_j X, \partial_1 X, \partial_2 X).$$

H	mean curvature. In case of parametrisations X in \mathbb{R}^3 over a two dimensional parameter domain:
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$$H = \frac{1}{2} \sum_{i,j=1}^2 g^{ij} L_{ij} = \frac{1}{2g} (g_{22} L_{11} - 2g_{12} L_{12} + g_{11} L_{22}).$$

K	Gaussian curvature. In case of parametrisations X in \mathbb{R}^3 over a two dimensional parameter domain:
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$$K = \frac{\det((L_{ij})_{i,j=1,2})}{g}.$$

Γ_{ij}^k	$= \sum_{\ell=1}^n \frac{1}{2} g^{k\ell} (\partial_j g_{i\ell} + \partial_i g_{j\ell} - \partial_\ell g_{ij})$, Christoffel symbols.
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$$R_{kij}^\ell = -R_{kji}^\ell = \partial_i \Gamma_{jk}^\ell - \partial_j \Gamma_{ik}^\ell + \sum_{m=1}^n (\Gamma_{im}^\ell \Gamma_{jk}^m - \Gamma_{jm}^\ell \Gamma_{ik}^m),$$

Riemannian curvature tensor.

$$R_{klij} = -R_{\ell kij} = R_{ijkl} = \sum_{m=1}^n g_{km} R_{lij}^m.$$

$$R_{ij} = \sum_{k,\ell=1}^n g^{k\ell} R_{ikj\ell} = \sum_{k=1}^n R_{ikj}^k, \text{ Ricci tensor.}$$

$$R = \sum_{i,j=1}^n g^{ij} R_{ij}, \text{ scalar curvature.}$$

$$S_{ij} = \frac{1}{n-2} \left(2R_{ij} - \frac{R}{(n-1)} g_{ij} \right), \text{ Schouten tensor.}$$

$$W_{ijkl} = R_{ijkl} - \frac{1}{n-2} (R_{ik} g_{j\ell} - R_{i\ell} g_{jk} + R_{j\ell} g_{ik} - R_{jk} g_{i\ell}) + \frac{R}{(n-1)(n-2)} (g_{j\ell} g_{ik} - g_{jk} g_{i\ell}), \text{ Weyl tensor.}$$

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