

# Appendix

## A1 Fractional powers of nonnegative operators

Let  $A$  be a nonnegative operator in a Banach space  $E$ , and let  $\alpha \in \mathbb{C}$  with  $\operatorname{Re} \alpha > 0$ .

**Definition A1.1.** (i) If  $A \in \mathbf{L}(E)$  and  $0 \in \rho(A)$ ,

$$A^\alpha := \frac{1}{2\pi i} \int_{\mathcal{C}} \lambda^\alpha R(\lambda; A) d\lambda,$$

where the contour  $\mathcal{C}$  surrounds  $\sigma(A)$ , avoiding the negative real axis and the origin, and  $\lambda^\alpha$  is taken to be positive for  $\lambda > 0$ .

(ii) If  $A \in \mathbf{L}(E)$  and  $0 \in \sigma(A)$ ,

$$A^\alpha := \lim_{\varepsilon \rightarrow 0^+} (A + \varepsilon)^\alpha.$$

(iii) If  $A \notin \mathbf{L}(E)$  and  $0 \in \rho(A)$ ,

$$A^\alpha := \left[ (A^{-1})^\alpha \right]^{-1}.$$

(iv) If  $A \notin \mathbf{L}(E)$  and  $0 \in \sigma(A)$ ,  $A^\alpha$  is defined by

$$A^\alpha u := \lim_{\varepsilon \rightarrow 0^+} (A + \varepsilon)^\alpha u, \quad u \in \mathcal{D}(A^\alpha),$$

where  $\mathcal{D}(A^\alpha)$  is the set of all  $u \in E$  for which the above limit exists.

**Theorem A1.2.**  $\mathcal{D}[(A + \varepsilon)^\alpha] = \mathcal{D}(A^\alpha)$  for each  $\varepsilon > 0$ .

**Theorem A1.3.**  $A^\alpha$  is a closed linear operator in  $E$ .

**Theorem A1.4.** If  $\alpha \in \mathbb{N}$ , then  $A^\alpha$  is the usual power of  $A$ .

**Theorem A1.5.** (i) For  $0 < \operatorname{Re} \alpha < 1$ ,  $u \in \mathcal{D}(A)$ ,

$$A^\alpha u = \frac{\sin \alpha \pi}{\pi} \int_0^\infty \lambda^{\alpha-1} (\lambda + A)^{-1} A u d\lambda.$$

(ii) For  $0 < \operatorname{Re} \alpha < 2$ ,  $u \in \mathcal{D}(A^2)$ ,

$$A^\alpha u = \frac{\sin \alpha \pi}{\pi} \int_0^\infty \lambda^{\alpha-1} [(\lambda + A)^{-1} - \lambda(1 + \lambda^2)^{-1}] A u d\lambda + \sin\left(\frac{\alpha \pi}{2}\right) A u.$$

**Theorem A1.6.** Let  $\operatorname{Re} \alpha, \operatorname{Re} \beta > 0$ . Then

$$A^{\alpha+\beta} = A^\beta A^\alpha = A^\alpha A^\beta.$$

**Theorem A1.7.** Let  $0 < \alpha < 1$ . Then  $A^\alpha$  is a nonnegative operator and for  $\beta \in \mathbb{C}$  with  $\operatorname{Re} \beta > 0$  we have

$$(A^\alpha)^\beta = A^{\alpha\beta}.$$

**Theorem A1.8.**  $\sigma(A^\alpha) = \{|z|^\alpha e^{i\alpha \arg z}; z \in \sigma(A), |\arg z| < \pi\}$ .

**Theorem A1.9.** Let  $0 < \alpha < 1$ . Then

$$\|A^\alpha u\| \leq \operatorname{const} (a^\alpha \|u\| + a^{\alpha-1} \|Au\|)$$

for all  $u \in \mathcal{D}(A)$ ,  $a > 0$ .

**Definition A1.10.** If  $0 \in \rho(A)$ ,

$$A^{-\alpha} := (A^\alpha)^{-1}.$$

For details on fractional powers of nonnegative operators, please see, e.g., Balakrishnan [1], Martínez-Sanz-Marco [1], Fattorini [6, 7] and Pazy [2].

## A2 Strongly continuous semigroups and cosine functions

**Definition A2.1.** Let  $E$  be a SCLCS. A family  $\{T(t)\}_{t \geq 0}$  of continuous linear operators on  $E$  is a (exponentially equicontinuous) strongly continuous (operator) semigroup if

(i)  $T(0) = I$ ,  $T(s+t) = T(t)T(s)$  ( $t, s \geq 0$ ),

(ii)  $\lim_{t \rightarrow 0^+} T(t)u = u$  ( $u \in E$ ),

(iii) there exists  $\omega > 0$  such that  $\{e^{-\omega t} T(t); t \geq 0\}$  is equicontinuous.

The generator  $A$  of a strongly continuous semigroup  $\{T(t)\}_{t \geq 0}$  is defined by

$$Au = \lim_{h \rightarrow 0^+} \frac{1}{h} [T(h)u - u], \quad u \in \mathcal{D}(A).$$

where  $\mathcal{D}(A)$  is the set of all  $u \in E$  for which the above limit exists.

A strongly continuous (operator) group (as well as its generator) is defined analogously, with the parameter  $t$  running over  $\mathbb{R}$  instead of  $\mathbb{R}^+$  (with  $h \rightarrow 0$  instead of  $h \rightarrow 0^+$ ).

Condition (iii) is implicitly contained in conditions (i) and (ii) in the case when  $E$  is a Banach space.

**Definition A2.2.** Let  $E$  be a SCLCS. A family  $\{C(t)\}_{t \geq 0}$  of continuous linear operators on  $E$  is a strongly continuous cosine (operator) function if

$$(i) \ C(0) = I, \quad 2C(t)C(s) = C(s+t) + C(|s-t|) \quad (t, s \geq 0),$$

$$(ii) \ \lim_{t \rightarrow 0^+} C(t)u = u \quad (u \in E),$$

$$(iii) \ \text{there exists } \omega > 0 \text{ such that } \{e^{-\omega t}C(t); t \geq 0\} \text{ is equicontinuous.}$$

The generator  $A$  of a strongly continuous cosine function  $\{C(t)\}_{t \geq 0}$  is defined by

$$Au = \lim_{t \rightarrow 0^+} \frac{2}{t^2} [C(t)u - u], \quad u \in \mathcal{D}(A),$$

where  $\mathcal{D}(A)$  is the set of all  $u \in E$  for which the above limit exists. Clearly, condition (iii) is implicitly contained in (i) and (ii) in the case when  $E$  is a Banach space; a strongly continuous cosine function  $\{C(t)\}_{t \geq 0}$  can be extended to the real axis  $\mathbb{R}$  by defining

$$C(t) = C(-t), \quad t < 0$$

such that  $\{C(t)\}_{t \in \mathbb{R}}$  satisfies

$$2C(t)C(s) = C(s+t) + C(s-t), \quad t, s \in \mathbb{R}.$$

**Theorem A2.3.** Let  $A$  be a closed linear operator in a SCLCS. Then the following statements are equivalent.

(i)  $A$  generates a strongly continuous semigroup  $T(t)$ .

(ii) The Cauchy problem for  $u'(t) = Au(t)$  ( $t \geq 0$ ) is wellposed (with the propagator  $T(t)$ ).

(iii)  $\{\lambda \in \mathbb{C}; \operatorname{Re} \lambda > \omega\} \subset \rho(A)$  for some  $\omega > 0$  and

$$\lambda \mapsto R(\lambda; A) \in LT - L(E)$$

(with the determining function  $T(t)$ ).

**Theorem A2.4.** Let  $A$  be a closed linear operator in a SCLCS. Then the following statements are equivalent.

(i)  $A$  generates a strongly continuous cosine function  $C(t)$ .

(ii) The Cauchy problem for  $u''(t) = Au(t)$  ( $t \geq 0$ ) is wellposed (with the two propagators  $C(t)$ ,  $\int_0^t C(s)ds$ ).

(iii)  $\{\lambda^2; \operatorname{Re} \lambda > \omega\} \subset \rho(A)$  for some  $\omega > 0$  and

$$\lambda \mapsto \lambda R(\lambda^2; A) \in LT - L(E)$$

(with the determining function  $C(t)$ ).

In the sequel, we assume that  $E$  is a Banach space.

**Definition A2.5.** Let  $\{T(t)\}_{t \geq 0}$  be a strongly continuous semigroup on  $E$ .

(i)  $T(t)$  is a semigroup of contractions on  $E$  if

$$\|T(t)\| \leq 1, \quad \text{for all } t \geq 0.$$

(ii)  $T(t)$  is an analytic semigroup of angle  $\theta$  ( $\theta \in (0, \frac{\pi}{2}]$ ) if it extends to a semigroup  $\{T(z); z \in \Sigma_\theta\}$ , analytic (in the norm of  $L(E)$ ) in  $\Sigma_\theta$  and satisfying that

$$T(z)u \longrightarrow u, \quad \text{as } z \longrightarrow 0 \quad (z \in \Sigma_{\theta'}),$$

for each  $u \in E$  and each fixed  $\theta' \in (0, \theta)$ .

(iii)  $T(t)$  is a differentiable semigroup (or differentiable for  $t > 0$ ) if for every  $u \in E$ ,  $t \mapsto T(t)u$  is differentiable for  $t > 0$ .

**Theorem A2.6 (Phillips' perturbation theorem).** Let  $A$  be the generator of a strongly continuous semigroup on  $E$ . If  $B \in L(E)$ , then  $A + B$  is also the generator of a strongly continuous semigroup on  $E$ .

**Theorem A2.7 (Stone).**  $A$  is the generator of a strongly continuous group of unitary operators on a Hilbert space if and only if  $iA$  is self-adjoint.

**Theorem A2.8.** Let  $A$  generate a strongly continuous semigroup  $T(t)$  on  $E$ . Then  $T(t)$  is norm continuous at  $t = 0$  if and only if  $A \in L(E)$ .

For the proofs, please see Davies [1, Section 1.3] and Pazy [2, Section 1.1].

**Theorem A2.9.** Let  $A$  generate a strongly continuous semigroup on  $E$ . Then  $-(-A)^{\frac{1}{2}}$  generates an analytic semigroup of angle  $\frac{\pi}{2}$ .

Please see Fattorini [6, Section 6.4] for a proof.

**Theorem A2.10.** Assume  $A$  is the generator of a strongly continuous cosine function  $\{C(t)\}_{t \geq 0}$  on  $E$ . Then  $A$  generates an analytic semigroup  $\{T(t)\}_{t \geq 0}$  of angle  $\frac{\pi}{2}$ , given by the abstract Weierstrass formula

$$T(t)u = \frac{1}{(\pi t)^{\frac{1}{2}}} \int_0^\infty e^{-\frac{t^2}{4s}} C(s) u ds, \quad t > 0, \quad u \in E.$$

Please see Fattorini [7, §VI.2] for a proof.

**Definition A2.11.** A linear operator  $A$  in  $E$  is dissipative if for every  $u \in \mathcal{D}(A)$  there is a  $u^* \in E^*$  with  $\langle u^*, u \rangle = \|u\|^2 = \|u^*\|^2$  such that  $\operatorname{Re} \langle u^*, Au \rangle \leq 0$ .

**Theorem A2.12.** *A linear operator  $A$  in  $E$  is dissipative if and only if*

$$\|(\lambda - A)u\| \geq \lambda\|u\|, \quad u \in \mathcal{D}(A), \quad \lambda > 0.$$

**Theorem A2.13.** *Let  $A$  be a dissipative operator in  $E$ .*

- (i) *If  $A$  is closable, then  $\overline{A}$  is also dissipative.*
- (ii) *If  $\overline{\mathcal{D}(A)} = E$ , then  $A$  is closable.*

Please see Pazy [2, Section 1.4] for a proof.

**Theorem A2.14 (Lumer-Phillips).** *Let  $A$  be a densely defined linear operator in  $E$ . If  $A$  is dissipative and there exists a  $\lambda_0 > 0$  such that  $\mathcal{R}(\lambda_0 - A) = E$ , then  $A$  is the generator of a strongly continuous semigroup of contractions on  $E$ .*

**Theorem A2.15.** *If  $A$  generates a strongly continuous semigroup of contractions on a Hilbert space  $H$ , then so does  $A^*$ .*

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$A^*$ ,	Preface	$\mathcal{M}_p$ ,	1.5
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$\mathcal{N}(A)$ ,	Preface	$\ \cdot\ _r$ ,	Preface

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