

Table of notation

Logic and sets. $\wedge, \vee, \Rightarrow, \Leftrightarrow, \forall, \exists$ (1); $\varepsilon, \notin, \subseteq, \not\subseteq$
 $\supseteq, \subset, \supset, \emptyset, \cup, \cap$ (2); $\{a, b, c, \dots\}, \{x: \phi(x)\},$
 $\{t(x): \phi(x)\}, \mathcal{P}(U)$ (3); nV (4); I_V (8); $\prod_{i \in I} U_i, i \in I$ (7).

Cardinal and ordinal numbers. $n^+, \aleph_\alpha, \omega$ (12); $\omega_\alpha, |A|$ (13).

Relations. $\langle a_0, a_1, \dots, a_{m-1} \rangle, R|V, \overline{R}, \overline{R}^T, aRb$ (4);
 x/R (5, 149, 150, 167); $R(X), R;S, R^\vee, R^n$ (5); $\text{Eq}(U)$ (8)

Functions. $f \circ g, fg, f \upharpoonright U$ (6); $f: U \rightarrow V, f: U \leftrightarrow V,$
 id_U (7); $\ker f$ (9); $\prod (f_i, i \in I), I_h, f^\#, [f(i)]_{i \in I}$ (14);
 $\text{id}(U, n, k)$ (83).

Lattices and partially ordered sets. $\leq, \geq, <, >, \equiv$ (11);
 $+, \cdot, L_d$ (21); M_3, N (22); \sum, \prod (23).

Algebras and relational structures. $\text{Hom}(A, B)$ (24); $\text{Iso}(A, B),$
 $\approx, \mathcal{C}(A)$ (25); $\leq_s, \geq_s, <_s, >_s, \text{Ss}(A), \text{Sa}(A), \text{Su}(A), A|X$ (66);
 $\text{Sg}_A(X)$ (77); $[X]_A$ (78); $\text{Pol}_n(A), \text{Pol}(A)$ (84); $\text{Alg}_n(A), \text{Alg}(A)$ (87);
 DCCS (120); $\text{Con}(A)$ (149); $\text{Rel}(A)$ (152); $\text{con}_A(R), \text{con}_A(R), \text{con}(R),$
 $\text{con}_A(a, b), \text{con}(a, b)$ (153); $\text{Mon}(A, B), \text{Epi}(A, B), 213; \text{Aut}(A), \text{End}(A), 214.$

Partial algebras. $\leq_s, B|X, \text{Su}(A), \text{Sg}_A(X)$ (177); $\text{Con}(A),$
 $\text{con}_A(R), \text{con}_A(x, y)$ (178).

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