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List of symbols

(a.s.)	I: 174, 178, 209, 346; II: 210	$\ \cdot \ $	I: 19, 20, 49, 61, 186
\mathcal{C} -lim	I: 140	\cdot^n	II: 203
$\Gamma \downarrow x$		\cdot^∞	II: 203
grad	I: 233	\cdot^{-1}	I: 81; II: 202
l.i.m.	I: 178, 188; II: 211	$\cdot +$	I: 43
lim	I: 133	$\cdot *$	I: 36, 117
$S_T \downarrow x$		\cdot^0	I: 22
lim	I: 74	$\cdot^{\sim 0}$	I: 36
$x \rightarrow \infty$		$[\cdot]$	I: 201
$\underline{\lim}$	I: 103; II: 221	(\cdot, \cdot)	I: 50
$\overline{\lim}$	II: 221	A	I: 3, 22, 55
(p.)	I: 177	$A^{(k, \lambda)}$	II: 225
(q.m.)	I: 178	\tilde{A}	I: 37, 55
s lim	I: 19	a^{ij}	I: 151
w lim	I: 20	a^α	I: 352
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(unif. p.)	I: 178	\mathcal{Q}	I: 3, 140
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+	II: 207	B'	II: 162
-	II: 75	B^+	II: 1
\times	II: 203	B_0	I: 55
\geq, \leq	I: 261; II: 2	B_1	I: 55
\supseteq, \subseteq	I: 186, 210	\tilde{B}_0	I: 55
$\succ, \succ_{\mathbf{a}}, \approx$	II: 153, 157	b^i	I: 151
\downarrow	I: 261	\mathcal{B}	I: 47, 116, 247; II: 119
\uparrow	II: 205	$\mathcal{B}_{\mathbb{R}}$	II: 223
\xrightarrow{h}	I: 238	$\mathcal{B}_{\mathcal{G}}$	II: 96
\xrightarrow{k}	I: 211	\mathcal{B}_T	II: 202
\xrightarrow{q}	I: 214	\mathcal{B}_Δ	I: 33
\xrightarrow{s}	I: 19, 50	\mathcal{B}	I: 47, 83; II: 204
\xrightarrow{w}	I: 20, 50	$\hat{\mathcal{B}}$	I: 85
$\xrightarrow{\mu}$	II: 204	$\tilde{\mathcal{B}}$	II: 169
$\frac{d \cdot}{d \cdot}$	I: 247; II: 102	$C = C(E, \mathcal{C})$	I: 51
\int	I: 21, 37, 212, 237, 238; II: 170, 206, 233	$C = C(E, \mathcal{C}, \mathcal{B})$	I: 51
$ \cdot $	I: 208; II: 208	C^0	I: 62; II: 109
		C^k	I: 9; II: 225
		$C^{(k, \lambda)}$	II: 225
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		$\hat{C} = \hat{C}(E, \mathcal{C})$	I: 74

c	I: 4, 151	$k_i^*(x)$	I: 248
c_i	I: 78	$\tilde{k}_i(x)$	I: 248
\mathcal{C}_0	I: 116	$\mathcal{K} = \mathcal{K}(I) = \mathcal{K}(I, L)$	I: 209, 210
D_v	II: 235	$\mathcal{K}(I, E)$	I: 221
D_v^+, D_v^-	II: 235	\mathcal{K}^*	I: 237
$D_v D_u^+$	II: 139	\mathcal{K}^x	I: 238
$\mathcal{D}(G)$	II: 118	\mathcal{K}^δ	I: 246
$\mathcal{D}(u, v; x)$	II: 139	\mathcal{K}^μ	I: 237
$\mathcal{D}(x)$	I: 151	\mathcal{K}_0	I: 211
\mathcal{D}_A	I: 22, 55	\mathcal{K}_1	I: 210
$\mathcal{D}\mathfrak{A}$	I: 140	$\mathcal{K}_0^*, \mathcal{K}_1^*, \mathcal{K}_0^\mu, \mathcal{K}_1^\mu$	I: 239
$\mathcal{D}\mathfrak{A}(x)$	I: 145	$L = L(E, \tilde{E})$	I: 208
$\mathcal{D}\mathfrak{D}$	II: 103	$L(\Gamma)$	I: 91
\mathcal{D}_μ	II: 102	$l(x)$	II: 135
$\mathcal{D}\Psi$	II: 74	M	I: 208, 334, 346; II: 210
\mathfrak{D}	I: 151; II: 45, 102, 118	$\mathbf{M}(\cdot \cdot)$	II: 212
\mathfrak{D}_0	II: 107	\mathbf{M}_x	I: 3
E	I: 1, 47, 247; II: 119	\mathbf{M}_φ	I: 81
E_a^+, E_a^-	II: 120	$M(\Gamma)$	I: 92
E_c^i	II: 149	$m(x)$	II: 38, 129, 132
(E, \mathcal{B})	I: 47, 77	$m(x, c_1, c_2), m_i(x, a)$	II: 131
(E, \mathcal{C})	II: 218	$m_G(x)$	I: 114
$(E, \mathcal{C}, \mathcal{B})$	I: 51; II: 222	\mathcal{M}^0	I: 77
(E, \mathcal{F})	I: 150	\mathcal{M}_i	I: 2, 77
(E, ϱ)	II: 219	\mathcal{M}_{i+0}	I: 87
$(E, \varrho, \mathcal{B})$	I: 70	\mathcal{M}_x	I: 98
e^A	I: 28	$\tilde{\mathcal{M}}^0, \tilde{\mathcal{M}}_i$	I: 83
F_i^*	I: 104	\mathfrak{M}^e	I: 331; II: 65
\hat{F}_i^*	I: 105	$N(\Gamma)$	I: 91
$f(\infty)$	I: 74	$N'(\Gamma)$	I: 95
f_+, f_-	II: 203	$n(x)$	II: 135
f_i, f_{ij}	I: 153	\mathcal{N}	I: 80
$f_\alpha, f_{\alpha\beta}$	I: 68	\mathcal{N}^0	I: 80
$\mathcal{F}[\cdot]$	II: 201	\mathcal{N}^*	I: 81
$\mathcal{F}(x, U)$	I: 140	\mathcal{N}_i	I: 80
\mathcal{F}_x	I: 150	\mathcal{N}_{i+0}	I: 106
G_φ	II: 78	\mathcal{N}_A	I: 285
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$g_\lambda(x, y)$	II: 87	\mathcal{N}_i^δ	I: 245
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H	II: 148	$\tilde{\mathcal{N}}'$	II: 12
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	II: 1	$\tau_\eta, \tau_{\eta+0}$	I: 115
T_τ	I: 3	$\varphi = \varphi_i^t$	I: 7, 172
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