

# A Quick Summary

## Chapter 1

- Topological space. Subspace. Continuous map (preimage of an open set is open). Homeomorphism (bijective, continuous, inverse continuous). Closed set, closure, boundary, interior.
- Compact space (in  $\mathbb{R}^d$ : closed and bounded). A continuous function attains its minimum on a compact space. A continuous mapping on a compact metric space is uniformly continuous.
- **Homotopy** (of maps;  $f \sim g$ ). **Homotopy equivalence** (of spaces;  $X \simeq Y$ ). Deformation retract ( $Y$  can be shrunk continuously to  $X$ , “within  $Y$ ” and keeping  $X$  fixed).  $X \simeq Y$  iff  $X$  and  $Y$  are both deformation retracts of some  $Z$ .
- Simplex. **Geometric simplicial complex**. **Abstract simplicial complex**  $K$  (a hereditary system of finite sets, includes  $\emptyset$ ). Geometric realization, polyhedron (unique up to homeomorphism). Associates a topological space with any finite hereditary set system. Further notions:  $V(K)$ ,  $\dim K$ ,  $\text{supp}(\mathbf{x})$  (the support of a point).
- Triangulation ( $X \cong \|K\|$ ). Every  $d$ -dimensional  $K$  can be realized in  $\mathbb{R}^{2d+1}$  (use the moment curve).
- **Simplicial map** (vertex  $\mapsto$  vertex, preserves simplices). A combinatorial counterpart of a continuous map. Yields a continuous map by affine extension on each simplex. Isomorphism.
- Order complex  $\Delta(P, \preceq)$  of a poset (simplices = chains). **Barycentric subdivision**  $\text{sd}(K) := \Delta(K, \sqsubseteq)$ . Geometric view (add barycenters as new vertices);  $\|\text{sd}(K)\| \cong \|K\|$ .

## Chapter 2

- **Borsuk–Ulam theorem:**
  - For every  $f: S^n \rightarrow \mathbb{R}^n$  there is  $\mathbf{x}$  with  $f(\mathbf{x}) = f(-\mathbf{x})$ .
  - Every antipodal  $f: S^n \rightarrow \mathbb{R}^n$  has a zero.
  - There is no antipodal  $f: S^n \rightarrow S^{n-1}$ .
  - There is no  $f: B^n \rightarrow S^{n-1}$  antipodal on the boundary.

- For every cover of  $S^n$  by  $n+1$  sets, each of them either open or closed, one of the sets contains a pair of antipodal points (Lyusternik–Shnirel’man theorem).

Many proofs known.

- Tucker’s lemma (a discrete version of Borsuk–Ulam): If  $T$  is a triangulation of  $B^n$  antipodally symmetric on the boundary and  $\lambda: V(T) \rightarrow \{\pm 1, \dots, \pm n\}$  is a labeling antipodal on the boundary, then there is a complementary edge (labels  $+i$  and  $-i$ ). Reformulation: There is no simplicial map of  $T$  into  $\diamond^{n-1}$  (boundary of the crosspolytope) antipodal on the boundary.

### Chapter 3

- Mass distribution  $\mu$  in  $\mathbb{R}^d$  ( $\mu(\mathbb{R}^d) < \infty$ , open sets measurable, hyperplanes have measure 0). **Ham sandwich theorem:** Every  $d$  mass distributions in  $\mathbb{R}^d$  can be simultaneously bisected by a hyperplane.
- Every  $d$  finite point sets in  $\mathbb{R}^d$  can be simultaneously bisected by a hyperplane ( $A$  bisected by  $h$ : at most  $\frac{1}{2}|A|$  points in each of the open half-spaces).
- Mass partition theorems. For example, a mass distribution in  $\mathbb{R}^2$  can be bisected into 4 equal parts by 2 lines. Generalization to  $2^d$  pieces by  $d$  hyperplanes in  $\mathbb{R}^d$  fails for  $d \geq 5$  (moment curve).
- Akiyama–Alon:  $n$ -point sets  $A_1, \dots, A_d$  in general position in  $\mathbb{R}^d$  can be partitioned into  $n$  rainbow  $d$ -tuples with disjoint convex hulls.
- Any necklace with  $d$  kinds of stones can be divided between two thieves by  $d$  cuts (place the necklace on the moment curve in  $\mathbb{R}^d$  and use ham sandwich). Continuous version (Hobby–Rice).
- Kneser graph  $\text{KG}(\mathcal{F})$ : edges = pairs of disjoint sets. Chromatic number  $\chi(G)$ . **Lovász–Kneser theorem:**  $\chi(\text{KG}(\binom{[n]}{k})) = n - 2k + 2$ ,  $n \geq 2k$ . Important examples of graphs with a large chromatic number.
- First proof of the Lovász–Kneser theorem: Let  $d := n - 2k + 1$ , suppose a  $d$ -coloring exists. Choose  $n$  points in general position on  $S^d$ . For  $i \in [d]$ , let  $A_i$  consist of the  $\mathbf{x} \in S^d$  such that the open hemisphere centered at  $\mathbf{x}$  contains a  $k$ -tuple of color  $i$ ;  $A_{d+1}$  is the rest. Apply Lyusternik–Shnirel’man (“open-or-closed” version).
- Dol’nikov:  $\chi(\text{KG}(\mathcal{F})) \geq \text{cd}_2(\mathcal{F})$ ; here  $\text{cd}_2(\mathcal{F})$  is the minimum number of white points in a red–blue–white coloring with no  $F \in \mathcal{F}$  completely red or completely blue. Proof as before,  $d := \chi(\text{KG}(\mathcal{F}))$ .
- Gale’s lemma:  $d + 2k$  points can be placed on  $S^d$  so that every open hemisphere contains at least  $k$  of them. Bárány’s proof of the Lovász–Kneser theorem: Dimension one lower than before,  $d := n - 2k$ ; supposing that  $(d+1)$ -coloring exists, place points as in Gale’s lemma, define  $A_i$  as in the previous proof (but now  $i \in [d+1]$ ), and apply Lyusternik–Shnirel’man for open sets.

- Schrijver’s theorem: The subgraph of  $\text{KG}(\binom{[n]}{k})$  induced by all stable sets (independent sets in the cycle of length  $n$ ) has chromatic number  $n-2k+2$ , same as the whole graph. Proof: Gale’s lemma in a stronger form, with every open hemisphere containing a stable set.

### Chapter 4

- Quotient space. Sum. Wedge. Contracting a contractible subcomplex is a homotopy equivalence.
- **Join.** For simplicial complexes:  $\mathbf{K} * \mathbf{L} := \{F \uplus G : F \in \mathbf{K}, G \in \mathbf{L}\}$ , where  $F \uplus G = (F \times \{1\}) \cup (G \times \{2\})$ . For spaces:  $X * Y$  is a quotient space of  $X \times Y \times [0, 1]$ . Both give the same ( $\|\mathbf{K} * \mathbf{L}\| \cong \|\mathbf{K}\| * \|\mathbf{L}\|$ ); use geometric interpretation ( $X$  and  $Y$  placed in skew affine subspaces; take all segments  $\mathbf{x}\mathbf{y}$ ,  $\mathbf{x} \in X$ ,  $\mathbf{y} \in Y$ ). Points written  $t\mathbf{x} \oplus (1-t)\mathbf{y}$  (formal convex combinations).
- **$k$ -connected space** (every map from  $S^i$ ,  $i \leq k$ , is nullhomotopic).  $S^n$  is  $(n-1)$ -connected and not  $n$ -connected.
- $k$ -connected  $\Leftrightarrow$  1-connected and zero homology up to dimension  $k$ . ( $k$ -connected) $*$ ( $\ell$ -connected) is  $(k+\ell+2)$ -connected. Nerve theorem: If subcomplexes cover  $\mathbf{K}$  and all of their intersections are contractible or empty, then their nerve is homotopy equivalent to  $\|\mathbf{K}\|$ .
- CW-complex. Cellular map.

### Chapter 5

- **$\mathbb{Z}_2$ -space**  $(X, \nu)$ ,  $\nu$  a homeomorphism  $X \rightarrow X$ ,  $\nu^2 = \text{id}$ . Free  $\mathbb{Z}_2$ -space ( $\nu$  has no fixed points).  **$\mathbb{Z}_2$ -map**  $(f \circ \nu = \omega \circ f)$ .
- **$\mathbb{Z}_2$ -index**  $\text{ind}_{\mathbb{Z}_2}(X) := \min\{n : X \xrightarrow{\mathbb{Z}_2} S^n\}$ . Main properties:
  - $\text{ind}_{\mathbb{Z}_2}(X) > \text{ind}_{\mathbb{Z}_2}(Y) \Rightarrow X \xrightarrow{\mathbb{Z}_2} Y$ .
  - If  $X$  is  $(n-1)$ -connected, then  $\text{ind}_{\mathbb{Z}_2}(X) \geq n$ .
  - For free  $\mathbf{K}$ , we have  $\text{ind}_{\mathbb{Z}_2}(\mathbf{K}) \leq \dim(\mathbf{K})$ .
  - (Sarkaria’s inequality) If  $\mathbf{L}_0$  is an invariant subcomplex of a  $\mathbb{Z}_2$ -complex  $\mathbf{L}$ , then  $\text{ind}_{\mathbb{Z}_2}(\mathbf{L}_0) \geq \text{ind}_{\mathbb{Z}_2}(\mathbf{L}) - \text{ind}_{\mathbb{Z}_2}(\Delta(\mathbf{L} \setminus \mathbf{L}_0)) - 1$ .
- **Deleted join**  $\mathbf{K}_{\Delta}^{*2} := \{F \uplus G : F, G \in \mathbf{K}, F \cap G = \emptyset\}$  (a free  $\mathbb{Z}_2$ -space).  $\text{ind}_{\mathbb{Z}_2}((\sigma^n)_{\Delta}^{*2}) = n$ . Deleted join  $(\mathbb{R}^d)_{\Delta}^{*2} := (\mathbb{R}^d)^{*2} \setminus \{\frac{1}{2}\mathbf{x} \oplus \frac{1}{2}\mathbf{x} : \mathbf{x} \in \mathbb{R}^d\}$ .  $\text{ind}_{\mathbb{Z}_2}((\mathbb{R}^d)_{\Delta}^{*2}) = d$ .
- **Nonembeddability theorem:** If  $\text{ind}_{\mathbb{Z}_2}(\mathbf{K}_{\Delta}^{*2}) > d$ , then any map  $\|\mathbf{K}\| \rightarrow \mathbb{R}^d$  identifies two points with disjoint support, and in particular,  $\mathbf{K}$  is not realizable in  $\mathbb{R}^d$ . Proof: For a map  $f: \|\mathbf{K}\| \rightarrow \mathbb{R}^d$  with  $f(\mathbf{x}_1) \neq f(\mathbf{x}_2)$  whenever  $\text{supp}(\mathbf{x}_1) \neq \text{supp}(\mathbf{x}_2)$ , the map  $f^{*2}$  can be regarded as a  $\mathbb{Z}_2$ -map  $\|\mathbf{K}_{\Delta}^{*2}\| \rightarrow (\mathbb{R}^d)_{\Delta}^{*2}$ , and the right-hand side has  $\mathbb{Z}_2$ -index  $d$ .
- Topological Radon theorem: Any continuous map of the  $(d+1)$ -simplex into  $\mathbb{R}^d$  identifies two points with disjoint supports.

- **Van Kampen–Flores theorem:** Let  $K$  denote the  $d$ -skeleton of the  $(2d+2)$ -simplex; then  $K$  cannot be realized in  $\mathbb{R}^{2d}$  ( $d = 1$  is the nonplanarity of  $K_5$ ). Needed:  $\text{ind}_{\mathbb{Z}_2}(K_{\Delta}^{*2}) > 2d$ .
- First proof of Van Kampen–Flores: Bier spheres; shows that  $\|K_{\Delta}^{*2}\| \cong S^{2d+1}$ .
- The construction of the Bier spheres also gives that most triangulations of  $S^n$  are nonpolytopal.
- Kneser colorings and index of the deleted join: Let  $\mathcal{F}$  be the system of inclusion-minimal nonfaces of a simplicial complex  $K$  on  $[n]$ . Then  $\text{ind}_{\mathbb{Z}_2}(K_{\Delta}^{*2}) \geq n - \chi(KG(\mathcal{F})) - 1$ . Method: Sarkaria’s inequality; an  $m$ -coloring of  $KG(\mathcal{F})$  provides a  $\mathbb{Z}_2$ -embedding of the order complex of  $(\sigma^{n-1})_{\Delta}^{*2} \setminus K_{\Delta}^{*2}$  into  $S^{m-1}$ .
- Implies the Lovász–Kneser theorem, as well as Dol’nikov’s theorem.
- **Neighborhood complex**  $N(G)$  of a graph (vertex set  $V(G)$ , maximal simplices = neighborhoods of vertices). Lovász’s theorem: If  $N(G)$  is  $k$ -connected, then  $\chi(G) \geq k+3$ .
- Box complex  $B(G)$  of a graph (vertex set  $V \times [2]$ , simplices  $A \uplus B$ , where  $A$  and  $B$  are color classes of a complete bipartite subgraph of  $G$ ). Graph homomorphism; induces a  $\mathbb{Z}_2$ -map of the box complexes. Implies  $\chi(G) \geq \text{ind}_{\mathbb{Z}_2}(B(G)) + 2$ . Lovász’s theorem can be proved from this.
- Generalized Mycielski construction  $M_r(G)$ .  $N(M_r(G)) \simeq \text{susp}(N(G))$ ; yields a lower bound on the chromatic number for iterated  $M_r(\cdot)$ .

## Chapter 6

- **$G$ -space**,  $G$ -action  $\Phi = (\varphi_g)_{g \in G}$ ;  **$G$ -map**. Free  $G$ -action (no  $\varphi_g$  has a fixed point for  $g \neq e$ ) vs. fixed-point free  $G$ -action (no point fixed by all  $\varphi_g$ ).
- The only group acting freely on  $S^{2n}$  is  $\mathbb{Z}_2$ . Every  $\mathbb{Z}_q$  acts freely on  $S^1$  (rotation) and on  $S^{2n-1}$  (join of  $S^1$ ’s).
- $E_n G$  space ( $G$  finite):  $n$ -dimensional,  $(n-1)$ -connected, finite, free simplicial  $G$ -complex. Canonical example:  $G^{*(n+1)}$ .
- **$G$ -index**  $\text{ind}_G(X) := \min\{n : X \xrightarrow{G} E_n G\}$ . Properties analogous to the  $\mathbb{Z}_2$ -index. Nontrivial part:  $E_n G \xrightarrow{G} E_{n-1} G$  (generalized Borsuk–Ulam).
- $X_{\Delta(k)}^n$  ( $n$ -fold  $k$ -wise deleted product of a space; delete from  $X^n$  all  $n$ -tuples in which some  $k$  components coincide). We need  $(\mathbb{R}^d)_{\Delta(p)}^p$  for prime  $p$ , which has  $\mathbb{Z}_p$ -index  $d(p-1)-1$  (deformation retraction to  $S^{d(p-1)-1}$ ).
- $X_{\Delta(k)}^{*n}$  ( $n$ -fold  $k$ -wise deleted join of a space; delete from  $X^{*n}$  all  $\frac{1}{n}x_1 \oplus \frac{1}{n}x_2 \oplus \dots \oplus \frac{1}{n}x_n$ , where some  $k$  of the  $x_i$  coincide). Again, we need only  $(\mathbb{R}^d)_{\Delta(p)}^{*p}$  for prime  $p$ ;  $\mathbb{Z}_p$ -index is  $(d+1)(p-1)-1$ .
- $K_{\Delta(k)}^{*n}$  ( $n$ -fold  $k$ -wise deleted join of a simplicial complex; delete from  $K^{*n}$  all  $n$ -tuples of simplices in which some  $k$  simplices share a vertex). We use mainly  $k = 2$ .

- Necklace for  $q$  thieves with  $d$  kinds of stones:  $N := d(q-1)$  stones suffice. Proof: For prime  $q$ , encode divisions by points of  $(\sigma^N)_{\Delta(2)}^{*q}$ ; if no just division existed, the shares of the thieves would yield a  $\mathbb{Z}_q$ -map  $(\sigma^N)_{\Delta(2)}^{*q} \rightarrow (\mathbb{R}^d)_{\Delta(q)}^q$ .
- Tverberg's theorem: Any  $(d+1)(r-1)+1$  points in  $\mathbb{R}^d$  can be partitioned into  $r$  groups whose convex hulls all have a common point. **Topological Tverberg theorem:** Any continuous map  $f: \|\sigma^N\| \rightarrow \mathbb{R}^d$  identifies some  $p$  points with disjoint supports into a single point, where  $N = (d+1)(p-1)$ . Proof: A bad  $f$  would yield a  $\mathbb{Z}_p$ -map  $(\sigma^N)_{\Delta(2)}^{*p} \rightarrow (\mathbb{R}^d)_{\Delta(p)}^{*p}$ . Works only for  $p$  prime; the theorem is also known for prime powers but not in general!
- A lower bound for the number of Tverberg partitions follows by a similar method (find many smaller invariant subcomplexes of  $(\sigma^N)_{\Delta(2)}^{*p}$  that still have  $\mathbb{Z}_p$ -index  $N$ ).
- Kneser hypergraph  $\text{KG}_r(\mathcal{F})$ . Chromatic number of a hypegraph (no monochromatic edge). Embeddability of  $\|\mathbf{K}\|$  into  $\mathbb{R}^d$  without  $p$ -fold points, with  $p$  prime, can be related to  $\chi(\text{KG}_r(\mathcal{F}))$ , where  $\mathcal{F}$  consists of the minimal nonfaces of  $\mathbf{K}$ , as in the  $\mathbb{Z}_2$ -case.
- **Colored Tverberg theorem:** If we have points of  $d+1$  colors in  $\mathbb{R}^d$ , sufficiently many points of each color, then we can select  $r$  disjoint rainbow subsets whose convex hulls all have a common point. Proof: Let  $r$  be a prime. Consider the simplicial complex  $\mathbf{K}$  with  $(d+1)$ -element rainbow sets as maximal simplices, and produce a good coloring of  $\text{KG}_r(\mathcal{F})$ . Result:  $2r-1$  points of each color suffice.

# Hints to Selected Exercises

**1.2.4.** They are; all maps into  $\mathbb{R}^3$  are nullhomotopic.

**1.4.1.** It is known that the smallest triangulation has 14 2-simplices.

**1.4.2(a).** For a face with vertex set  $F$ , a defining hyperplane is  $\langle \mathbf{a}_F, \mathbf{x} \rangle = 1$  with  $\mathbf{a}_F = \sum_{\mathbf{v} \in F} \mathbf{v}$ .

**1.4.4(f).** The triangulation in (a) is the same on the facets  $x_1 = 0$  and  $x_1 = 1$ .

**1.5.1.** A torus.

**1.7.1.** One possibility is to observe that the barycentric subdivision of a  $(d-1)$ -simplex is obtained from the triangulation of the cube in Example 1.4.2 by slicing it with the hyperplane  $\sum_1^d x_i = 1$ .

**2.1.3(a).** Suppose  $g: B^{n+1} \rightarrow \mathbb{R}^{n+1}$  is antipodal on the boundary and has no zero. For  $t \in [0, 1]$ , define  $f_t: S^n \rightarrow S^n$  by  $f_t(\mathbf{x}) = \frac{g(t\mathbf{x})}{\|g(t\mathbf{x})\|}$ . The  $f_1$  is antipodal, but the  $f_t$  define a homotopy of  $f_1$  with the constant map  $f_0$ .

**2.1.3(b).** The trick in (a) can be reversed.

**2.1.4.** For the less trivial implication, observe that a nonsurjective map  $S^n \rightarrow S^n$  is nullhomotopic.

**2.1.5.** An antipodal map  $S^n \rightarrow S^{n-1}$  can be regarded as an antipodal nonsurjective map  $S^n \rightarrow S^n$ . Use Exercise 3.

**2.1.6.** As in the proof of (LS-o) $\Rightarrow$ (LS-c), but wrap only the closed  $A_i$ .

**2.3.1(b).** Apply (BU2b) to the canonical affine extension of  $g$  on  $\hat{B}^n$ , and use (a).

**3.1.3.** Map the sets into  $\mathbb{R}^3$  by the mapping  $(x, y) \mapsto (x, y, x^2 + y^2)$ . How is halving of the sets by circles in the plane related to dissection of their images in  $\mathbb{R}^3$  by planes?

**3.1.5(a).** Use 4 tiny disks.

**3.1.5(b).** 2 + 2 + 2 tiny disks in suitably general position.

**3.1.5(c).** 4 + 4 tiny disks in suitably general position.

**3.5.3.** Fix a coloring, choose a random Schrijver subgraph, and use the fact that it has at least one monochromatic edge.

**4.1.4.** Contract the edges of a spanning tree.

**4.1.6.** Check that  $K/K_2$  is homeomorphic to  $K_1/(K_1 \cap K_2)$ .

**5.3.7.** Use Exercise 5(c).

**5.3.8(a).** The inequality for joins is reversed!

**5.5.2(a).** One can  $\mathbb{Z}_2$ -map into  $\mathbb{R}^d \setminus \{\mathbf{0}\}$  by  $(1-t)\mathbf{x} \oplus t\mathbf{y} \mapsto (1-t)\mathbf{x} - t\mathbf{y}$ .

**5.5.4.** For  $\mathbf{x}, \mathbf{y} \in \|\mathbf{K}\|$  with disjoint supports, map  $1\mathbf{x} \oplus 0\mathbf{y} \mapsto (\mathbf{x}, \mathbf{v})$ , where  $\mathbf{v}$  is the apex of cone  $\mathbf{K}$ ,  $\frac{1}{2}\mathbf{x} \oplus \frac{1}{2}\mathbf{y} \mapsto (\mathbf{x}, \mathbf{y})$ ,  $0\mathbf{x} \oplus 1\mathbf{y} \mapsto (\mathbf{v}, \mathbf{y})$ , and interpolate linearly.

**5.8.1.** Use Kuratowski's theorem.

**5.8.4(a).** The deleted join is a Bier sphere.

**5.8.4(b).** Kneser coloring by  $r$  colors.

**6.2.3(b).** By the assumption, no  $\mathbb{Z}_p$ -map  $S^{n-1} \rightarrow S^{n-1}$  is nullhomotopic. Composing a  $\mathbb{Z}_p$ -map as in the conclusion with the map in (a) would yield a nonsurjective, and thus nullhomotopic,  $\mathbb{Z}_p$ -map  $S^{n-1} \rightarrow S^{n-1}$ .

**6.7.1(d).** For the upper bound,  $\text{index} \leq \text{dimension}$ . For the lower bound, since deleted join and join commute, it suffices to show  $(r-3)$ -connectivity of the  $(r-2)$ -skeleton of  $\sigma^{r-1}$ .

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The references are sorted alphabetically by the abbreviations (rather than by the authors' names).

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# Index

The index starts with notation composed of special symbols, and Greek letters are listed next. Terms consisting of more than one word mostly appear in several variants, for example, both “convex set” and “set, convex.” An entry like “armadillo, 19(8.4.1), 22(Ex. 4)” means that the term is located in theorem (or definition, etc.) 8.4.1 on page 19 and in Exercise 4 on page 22. For many terms, only the page with the term’s definition is shown. Names or notation used only within a single proof or remark are usually not indexed at all.

- $a := B$  (definition), xii
- $\lfloor x \rfloor$  (floor function), xii
- $\lceil x \rceil$  (ceiling function), xii
- $|S|$  (cardinality), xi
- $2^S$  (powerset), xi
- $\binom{S}{k}$  ( $k$ -element subsets), xi
- $\binom{S}{\leq k}$  (at most  $k$ -element subsets), xi
- $[n]$  ( $= \{1, 2, \dots, n\}$ ), xi
- $\partial X$  (boundary), 3
- $X \sqcup Y$  (disjoint sum), 70(4.1.4)
- $X \vee Y$  (wedge), 70(4.1.4)
- $X \times Y$  (Cartesian product), 73
- $X * Y$  (join), 74(4.2.1)
- $f * g$  (join of maps), 77
- $\|K\|$  (polyhedron), 9(1.3.5)
- $\|f\|$  (affine extension of a simplicial map), 15(1.5.3)
- $\Delta^{\leq k}$  ( $k$ -skeleton), 10
- $A_1 \uplus A_2 \uplus \dots \uplus A_n$  ( $= (A_1 \times \{1\}) \cup (A_2 \times \{2\}) \cup \dots \cup (A_n \times \{n\})$ ), 74
- $t_1x_1 \oplus t_2x_2 \oplus \dots \oplus t_nx_n$  (point in a join), 77
- $X_{\Delta}^2$  (deleted product of a space), 110
- $\Delta_{\Delta}^2$  (deleted product of a simplicial complex), 110
- $X_{\Delta}^n$  ( $n$ -fold  $n$ -wise deleted product of a space), 158(6.3.1)
- $X_{\Delta(k)}^n$  ( $n$ -fold  $k$ -wise deleted product of a space), 158(6.3.1)
- $K_{\Delta}^{*2}$  (deleted join of a simplicial complex), 112(5.5.1)
- $K_{\Delta}^{*n}$  ( $n$ -fold  $n$ -wise deleted join of a simplicial complex), 158(6.3.1)
- $K_{\Delta(k)}^{*n}$  ( $n$ -fold  $k$ -wise deleted join of a simplicial complex), 158(6.3.1)
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- $K \cong L$  (isomorphic simplicial complexes), 14(1.5.2)
- $f \sim g$  (homotopic maps), 5(1.2.1)
- $X \simeq Y$  (homotopy equivalent spaces), 6(1.2.2)
- $X \xrightarrow{G} Y$  (a  $G$ -map exists), 149
- $X \not\xrightarrow{G} Y$  (no  $G$ -map exists), 149
- $X \leq_G Y$  (same as  $X \xrightarrow{G} Y$ ), 149

- $\|\mathbf{x}\|$  (Euclidean norm), xi
- $\|\mathbf{x}\|_p$  ( $\ell_p$  norm), xi
- $\|\mathbf{x}\|_\infty$  (maximum norm), xi
- $\langle \mathbf{x}, \mathbf{y} \rangle$  (scalar product), xi
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- $\Delta(\mathcal{F})$  ( $= \Delta(\mathcal{F}, \subseteq)$ ), 122
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- $\chi(G)$  (chromatic number), 58
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