

# Index

Subscripts refer to authors' names: [B] for Bellaïche, [C] for Coron, [G] for Gromov, [M] for Montgomery, and [S] for Sussmann.

Example: "Chow's theorem, 2<sub>B</sub>, 3, 15, 87<sub>G</sub>, 95, 113, 380<sub>C</sub>", means that the entry appears on pages 2, 3 and 15 of Bellaïche's article; 87, 95 and 113 of Gromov's article; and on page 380 of Coron's article.

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