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The above list contains only a fraction of the publications on constructive mathematics that have appeared in the last forty years, and does not include the sources of all results in our book. The reader should not fall into the trap of believing that an unascribed result was first produced by the authors.

We mention two websites that may interest the reader:

`http://www.math.canterbury.ac.nz/php/groups/cm/faq/`
`http://plato.stanford.edu/entries/mathematics-constructive/`

In addition, many of the authors of items in the bibliography have websites that are worth a visit.

The primary historical reference on constructive analysis is [9], the review of which [85] is interesting in its own right. Later references for Bishop-style constructivism are [12, 34], the latter of which gives comparisons between BISH, INT, and RUSS. Beeson [6] and Troelstra–van Dalen [88] contain a wealth of information about the logic, philosophy, and practice of constructive mathematics. For some applications of constructive mathematics, see [20, 33, 92]. The definitive reference for constructive algebra is [72], but [49] should be consulted for more recent work in the field.

The classic work on intuitionism is [48]. The life and works of Brouwer himself are discussed in [44, 45, 84]. Martin-Löfs early work on constructive mathematics is found in [68], and his theory of types appears in [69].

Among the most recent varieties of computable analysis is that of Weihrauch [91]; the translation of BISH into Weihrauchs framework is described in [5].

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