## Modeling the infrared extinction toward the galactic center

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We model the  $\sim 1-19 \,\mu\text{m}$  infrared (IR) extinction curve toward the Galactic Center (GC) in terms of the standard silicate-graphite interstellar dust model. The grains are taken to have a power law size distribution with an exponential decay above some size. The best-fit model for the GC IR extinction constrains the visual extinction to be  $A_V \sim 38-42$  mag. The limitation of the model, i.e., its difficulty in simultaneously reproducing both the *steep*  $\sim 1-3 \,\mu\text{m}$  near-IR extinction and the *flat*  $\sim 3-8 \,\mu\text{m}$  mid-IR extinction is discussed. We argue that this difficulty could be alleviated by attributing the extinction toward the GC to a combination of dust in different environments: dust in diffuse regions (characterized by small  $R_V$  and steep near-IR extinction), and dust in dense regions (characterized by large  $R_V$  and flat UV extinction).

Key words: ISM: dust, extinction—infrared: ISM—Galaxy: center.

### 1. Introduction

The wavelength dependence of the interstellar extinction-known as the "interstellar extinction law (or curve)"-is one of the primary sources of information about the interstellar grain population (Draine, 2003). The Galactic interstellar extinction curves in the ultraviolet (UV) and visual wavelengths vary from one sightline to another, and can be parameterized in terms of the single parameter  $R_V \equiv A_V/E(B - V)$ , the total-to-selective extinction ratio (Cardelli et al., 1989).<sup>1</sup> Larger values of  $R_{\rm V}$  correspond to size distributions skewed toward larger grains (e.g., dense clouds tend to have large values of  $R_{\rm V} > 4$ ). On average, the dust in the diffuse interstellar medium (ISM) corresponds to  $R_V \approx 3.1$ .

However, the infrared (IR) interstellar extinction law, which also varies from sightline to sightline, cannot be simply represented by  $R_V$ . Various recent studies have shown that there does not exist a "universal" near-IR (NIR) extinction law (Fitzpatrick and Massa, 2009; Gao *et al.*, 2009; Zasowski *et al.*, 2009) and the mid-IR (MIR) extinction law shows a flat curve and lacks the model-predicted pronounced minimum extinction around 7  $\mu$ m (Draine, 1989).<sup>2</sup> It is worth noting that the flat MIR extinction curves determined for various sightlines all appear to agree with the extinction predicted by the standard silicate-graphite interstellar grain model for  $R_V = 5.5$  (Weingartner and Draine, 2001) (hereafter WD01), which indicates a dust size distribution favoring larger sizes compared to that for  $R_V = 3.1$ .

Recently, using the hydrogen emission lines of the minispiral observed by ISO-SWS and SINFONI, Fritz *et al.* (2011) derived the IR extinction curve toward the inner GC from 1 to 19  $\mu$ m. The extinction curve shows a *steep* NIR extinction consistent with that of Nishiyama *et al.* (2006, 2009) and a *flat* MIR extinction consistent with other sightlines (see Fig. 1). It differs from the IR extinction law toward the GC derived by Rieke and Lebofsky (1985) (hereafter RL85) and Rieke *et al.* (1989). Based on their observations, Fritz *et al.* (2011) argued that the extinction at the visual band ( $A_V$ ) toward the GC may be as high as  $A_V \sim 59$  mag (with the exact  $A_V$  depending on the chosen gas-to-dust ratio  $N_H/A_V$ ), much larger than  $A_V \sim 31$  estimated by Rieke *et al.* (1989) which is commonly adopted in the astronomical literature.

In this work, we try to use the standard interstellar grain model which consists of graphite and silicate grains (Draine and Lee, 1984) to fit the observed IR extinction curve toward the GC of Fritz *et al.* (2011) and constrain the total optical extinction ( $A_V$ ) toward the GC. Section 2 briefly describes the grain model. Our model results are presented in Section 3 and discussed in Section 4. In Section 5 we summarize the major conclusion of this work.

## 2. Dust Model

We take the dust to be a mixture of separate amorphous silicate and graphite grains, with the optical properties taken from Draine and Lee (1984). For the dust size distribution, we adopt a power law with an expoential cutoff at some large size:  $dn/da = A n_{\rm H} a^{-\alpha} \exp(-a/a_{\rm b})$  with 50 Å  $< a < 1 \,\mu$ m, where *a* is the grain radius,<sup>3</sup> *dn* is the number density of dust with radii in the interval [*a*, *a*+*da*] per H nuclei, *n*<sub>H</sub> is the number density of H nuclei, *A* is the normalization constant,  $\alpha$  is the power index, and *a*<sub>b</sub> is the

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<sup>&</sup>lt;sup>1</sup>  $E(B-V) \equiv A_B - A_V$  is the interstellar reddening,  $A_B$  is the extinction at the "B" (blue;  $\lambda_B \approx 4400$  Å) band, and  $A_V$  is the extinction at the "V" (visual;  $\lambda_V \approx 5500$  Å) band.

 $<sup>^2</sup>$  In this work by "NIR" we mean 1  $\mu m < \lambda < 3 \,\mu m$  and by "MIR" we mean 3  $\mu m < \lambda < 8 \,\mu m$ .

<sup>&</sup>lt;sup>3</sup> We assume the dust to be spherical.



Fig. 1. IR extinction laws compiled from the literature. Red stars plot  $A_{\lambda}/A_{K_s}$  toward the GC based on H lines (Fritz *et al.*, 2011). Blue triangles are derived from stars toward the GC (RL85). Green squares are derived from the red clump giants toward the GC (Nishiyama *et al.*, 2009). Cyan diamonds are the Galactic plane average extinction at  $|l| < 5^{\circ}$  and  $|b| < 2^{\circ}$  (Gao *et al.*, 2009). The other three kinds of symbols plot the extinction laws obtained from sightlines away from the GC. For comparison, the extinction curves calculated from the interstellar grain model (WD01) for  $R_V = 3.1$  (black solid line) and  $R_V = 5.5$  (black dot-dashed line) are also shown.

cutoff size. In our modeling, we will have six parameters:  $A_{si}$ ,  $\alpha_{si}$ ,  $a_{b,si}$  for the silicate component, and  $A_c$ ,  $\alpha_c$ ,  $a_{b,c}$  for the graphite component. The total extinction at wavelength  $\lambda$  is given by

$$A_{\lambda} = (2.5 \log e) N_{\rm H} \sum_{i} \int da \frac{dn_i(a)}{da} C_{\text{ext},i}(a,\lambda), \quad (1)$$

where the summation is made over the two grain types (i.e., silicate and graphite),  $N_{\rm H} \equiv \int n_{\rm H} dl$  is the H column density which is the H number density integrated over the line of sight *l*, and  $C_{\text{ext},i}(a, \lambda)$  is the extinction cross section of grain type *i* of size *a* at wavelength  $\lambda$ . The goodness of fitting is evaluated by

$$\frac{\chi^2}{\text{d.o.f}} = \frac{\sum_{j=1}^{N_{\text{obs}}} \left(A_{\lambda}^{\text{mod}} - A_{\lambda}^{\text{obs}}\right)^2 / \sigma_j^2}{N_{\text{obs}} - N_{\text{para}}} \quad , \tag{2}$$

where  $A_{\lambda}^{\text{obs}}$  is the IR extinction toward the GC derived by Fritz *et al.* (2011) (see their table 2),  $N_{\text{obs}}$  is the number of observational data points,  $N_{\text{para}}$  is the number of adjustable parameters ( $N_{\text{para}} = 6$  if we assume different size distributions for silicate and graphite;  $N_{\text{para}} = 4$  if we assume that both dust components have the same size distribution),  $A_{\lambda}^{\text{mod}}$  is the model extinction computed from Eq. (1), and  $\sigma_j$ is the weight of the observed extinction.

Assuming that  $\approx 30\%$  of the cosmic C is in the gas phase, WD01 adopt the solar C abundance of Grevesse and Sauval (1998) to constrain their models. For Si, they also adopt the solar abundance of Si/H =  $3.63 \times 10^{-5}$ , but assuming a complete depletion in dust. Their CASE A models tried to seek the best fit by varying the total volume per H in both the carbonaceous and silicate distributions, while their CASE B models fixed at approximately the values found for  $R_V = 3.1$ . Following WD01, we fix the total dust quantity (per H nuclei) to be consistent with the cosmic abundance constraints. Let  $V_{\text{tot,si}}$  be the total volume of the silicate dust, and  $V_{\text{tot,c}}$  be the total volume of the graphitic dust. We take  $V_{\text{tot,si}} = 2.98 \times 10^{-27} \text{ cm}^3 \text{ H}^{-1}$  and  $V_{\text{tot,c}} = 2.07 \times 10^{-27} \text{ cm}^3 \text{ H}^{-1}$  (i.e., values for constraining all "CASE A" models of WD01)<sup>4</sup>. We will also consider  $V_{\text{tot,si}} = 3.9 \times 10^{-27} \text{ cm}^3 \text{ H}^{-1}$  (i.e., fixed values for all "CASE B" models of WD01).<sup>5</sup> The mass densities of amorphous silicate and graphite are taken to be  $\rho_{\text{sil}} \approx 3.5 \text{ g cm}^{-3}$  and  $\rho_{\text{carb}} \approx 2.24 \text{ g cm}^{-3}$ .

## 3. Model Extinction

To testify the dust model, we first fit the standard extinction curve of  $R_V = 3.1$ . With  $dn/da \propto a^{-3.5}e^{-a/0.14}$ for amorphous silicates and  $dn/da \propto a^{-3.1}e^{-a/0.11}$  for graphite, the model closely reproduces the  $R_V = 3.1$  Galactic extinction curve. To fit the observed IR extinction curve from 1  $\mu$ m to 19  $\mu$ m toward the GC (Fritz *et al.*, 2011), for

<sup>&</sup>lt;sup>4</sup> The abundances of C and Si given by Asplund *et al.* (2009) are 2.95 ×  $10^{-4}$  and 3.55 ×  $10^{-5}$ , respectively. If considering the solar abundances of Asplund *et al.* (2009), one would get  $V_{\text{tot,si}} = 2.91 \times 10^{-27} \text{ cm}^3 \text{ H}^{-1}$  and  $V_{\text{tot,c}} = 1.85 \times 10^{-27} \text{ cm}^3 \text{ H}^{-1}$ , i.e.  $V_{\text{tot,si}}/V_{\text{tot,c}} = 0.61/0.39$ , which is close to the ratio of the WD01 "CASE B" models. We also fitted the extinction curve by varying the ratio of  $V_{\text{tot,si}}/V_{\text{tot,c}}$ : by taking the silicate-to-graphite mass ratio to  $m_{\text{gra}}/m_{\text{sil}} = 0.4$ , 0.5, and 0.6, our model results show that  $A_{\text{V}}$  toward the GC is in the range of ~ 35–45 mag.

<sup>&</sup>lt;sup>5</sup> The WD01 "CASE B" model extinction curve of  $R_V = 5.5$  shows a similar tendency as the observed flat MIR extinction (Draine, 2003; Indebetouw *et al.*, 2005; Jiang *et al.*, 2006; Gao *et al.*, 2009; Nishiyama *et al.*, 2009; Zasowski *et al.*, 2009).

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Abundance	dn/da		$\chi^2/d.o.f$	$A_{\rm V}$	$A_{\rm Ks}$	$R_{\rm V}$	N <sub>H</sub>		
	silicate	graphite					$\times 10^{22} \mathrm{cm}^{-2}$		
Fitting the observed extinction curve from $1 \mu m$ to $19 \mu m^a$									
CASE A	$a^{-2.4}e^{-a/0.04}$		21.3/14	39.93	2.81	2.23	7.5		
CASE B	$a^{-2.6}e^{-a/0.05}$		20.4/14	38.38	2.79	2.34	7.2		
CASE A	$a^{-3.1}e^{-a/0.10}$	$a^{-2.7}e^{-a/0.04}$	17.2/12	40.57	2.71	2.31	7.6		
CASE B	$a^{-2.9}e^{-a/0.08}$	$a^{-2.5}e^{-a/0.04}$	17.0/12	41.28	2.69	2.34	7.7		
Only fitting the observed extinction from 1 $\mu$ m to 7 $\mu$ m									
CASE B	$a^{-3.0}e^{-a/0.09}$	$a^{-3.1}e^{-a/0.04}$	10.5/9	39.93	2.40	2.12	7.5		
CASE B with AMC	$a^{-3.1}e^{-a/0.12}$	$a^{-3.0}e^{-a/0.06}$	10.4/9	35.70	2.55	2.50	6.7		
Only fitting the observed extinction from $3 \mu m$ to $19 \mu m$									
CASE B	$a^{-4.0}e^{-a/0.03}$	$a^{-3.1}e^{-a/0.02}$	10.6/9	30.84	3.04	1.77	5.8		
CASE B with AMC	$a^{-3.8}e^{-a/0.02}$	$a^{-3.3}e^{-a/0.03}$	11.7/9	19.26	3.01	2.19	3.6		
Fitting with combinations of multi-extinction curves (see Section 4.3)									
$f_{R_V=2.1}$	$f_{R_V=3.1}$	$f_{R_V=5.5}$	$\chi^2/d.o.f$	$A_{\rm V}$	$A_{\rm Ks}$	$R_{\rm V}$			
0.30	0.49	0.21	39.1/14	34.56	2.66	2.60			
0.28	0.39	0.33 <sup>b</sup>	40.7/15	33.67	2.63	2.70			

Table 1. Model parameters for fitting the GC IR extinction curve.

<sup>a</sup>We only consider 18 of 21 points of Fritz *et al.* (2011) in order to reduce the effect of the 3.1  $\mu$ m H<sub>2</sub>O feature.

<sup>b</sup>McFadzean *et al.* (1989) argued that the molecular clouds may contribute as much as  $\sim 1/3$  ( $\sim 10$  mag) of the total visual extinction  $A_V$  towards the GC. Therefore, we fixed the fraction of the  $R_V = 5.5$ -type extinction to be 0.33.

simplicity we first assume that both graphite and silicate have the same size distribution (i.e.  $\alpha_{si} = \alpha_c$ ,  $a_{b,si} = a_{b,c}$ ). We then consider models with different power indices and cutoff sizes for the two dust components to search for better fits. The best-fit results are summarized in Table 1. We note that it makes little difference either taking the same size distribution or assuming different size distributions for silicate and graphite. None of these attempts could fit the flat MIR extinction well, although "CASE B" works relatively better.

In Fig. 2 we show the "CASE B" best-fit model extinction assuming different size distributions for silicate and graphite. Compared with the observed IR extinction curve toward the GC (Fritz et al., 2011), the model extinction is a little too high at the 2.166  $\mu$ m (Brackett- $\gamma$ ) band and too low at ~ 7  $\mu$ m:  $A_{2.166}^{\text{mod}} \approx 2.68$  mag while Fritz *et al.* (2011) obtained  $A_{2.166} \approx 2.49 \pm 0.11$  mag. The size distribution of  $\alpha_{\rm c} \approx -2.5$  and  $a_{\rm b,c} \approx 0.04 \,\mu{\rm m}$  for graphite reproduces well the steep NIR extinction but causes the minimum extinction near 7  $\mu$ m. The small cutoff  $a_{\rm b,c} \approx 0.04 \,\mu$ m implies that the model is rich in small graphite grains so that the model extinction curve is similar to that of  $R_V = 2.1$  in the UV. The size distribution of  $\alpha_{\rm si} \approx -2.9$  and  $a_{\rm b,si} \approx 0.08 \,\mu{\rm m}$  for silicate causes the strong silicate feature at 9.7  $\mu$ m. Our results show that it may require some dust grains with a size distribution peaking around  $0.5 \,\mu m$  or even larger to produce the flat MIR extinction. To avoid the complication of the silicate features we have also modeled the observed extinction but limiting ourselves to the extinction from  $1 \,\mu m$ to 7  $\mu$ m. To fit the MIR extinction, we have also tried models confining us to the observed extinction from  $3 \mu m$  to 19  $\mu$ m (i.e., ignoring the 1–3  $\mu$ m NIR extinction). These approaches seem to work well for the chosen wavelength range, but unfortunately, none of these attempts results in satisfactory fits for the whole range of  $1-19 \,\mu \text{m.}^6$  Finally, we replace graphite by amorphous carbon (AMC). But we are still not able to simultaneously fit both the NIR and MIR extinction.

The NIR extinction law toward the GC derived by Fritz et al. (2011) and Nishiyama et al. (2009) is much steeper than that derived by Rieke and Lebofsky (1985) and Rieke et al. (1989), with  $\beta \approx -2.0$  compared to the common value of  $\beta \approx -1.6$  to -1.8. For comparison, we also fit the extinction curve of Rieke et al. (1989), which is actually the  $R_{\rm V} = 3.1$ -type extinction, and the model also works very well with  $dn/da \propto a^{-2.1}e^{-a/0.08}$  for amorphous silicates and  $dn/da \propto a^{-3.0}e^{-a/0.28}$  for graphite. For the sake of clear comparison, we replot in Fig. 3 the results shown in Fig. 2 but in terms of  $A_{\lambda}/A_{\rm V}$ . We see that the IR extinction toward the GC derived by Fritz et al. (2011) seems to be a combination of the steep UV-to-NIR extinction of  $R_{\rm V} =$ 2.1, the flat MIR extinction of  $R_V = 5.5$ , and the strong silicate feature of  $R_{\rm V} = 3.1$ . It seems that a trimodal size distribution is required in order to achieve a close fit to the observed extinction from the UV through NIR, MIR to the silicate absorption band.

### 4. Discussion

# 4.1 The extinction features in the $3-7 \,\mu m$ wavelength range

The extinction curve toward the GC obtained by Fritz *et al.* (2011) shows the strong 3.1  $\mu$ m H<sub>2</sub>O feature and the 3.4  $\mu$ m aliphatic hydrocarbon feature. Fritz *et al.* (2011) found that the COMP-AC-S model of Zubko *et al.* (2004) seems to best fit their observations as judged by  $\chi^2/d.o.f.$  and the presence of the H<sub>2</sub>O ice features. The porosity of ice dust grains also makes Zubko *et al.* (2004)'s extinction

<sup>&</sup>lt;sup>6</sup> Fritz *et al.* (2011) obtained an optical depth of  $\tau_{9.7 \,\mu\text{m}} \approx 3.84 \pm 0.52$  relative to the continuum at 7  $\mu$ m from their interpolated extinction curve. However, in the wavelength range of the silicate features, there are too few points to extract the optical depth accurately, also because of the large errors. Considering the possible large uncertainty, we did not use  $\tau_{9.7 \,\mu\text{m}}$  to constraint our fitting.



Fig. 2. Comparison of the model extinction curve (red solid line) with the  $\sim 1-19 \,\mu$ m IR extinction of the GC (blue squares) observed by Fritz *et al.* (2011). Also shown are the extinction curves of  $R_V = 2.1$  (dotted line, see Cardelli *et al.* (1989)),  $R_V = 3.1$  (dashed line, WD01) and  $R_V = 5.5$  (dot-dashed line, WD01) with the silicate absorption features added (Draine, 2003).



Fig. 3. Same as Fig. 2 but with the y-axis plotted as  $A_{\lambda}/A_{\rm V}$ . The GC IR extinction curve of Fritz *et al.* (2011) is normalized to  $A_{\rm V} = 42$  mag (blue squares). Also shown is the GC extinction of Rieke *et al.* (1989) (cyan triangles), taking  $A_{\rm V} = 31$  mag.



Fig. 4. Comparison of the GC IR extinction of Fritz *et al.* (2011; blue squares) with the best fit model extinction (red solid line) obtained from the combination of three extinction curves of  $R_V = 2.1$  (28%, dotted line),  $R_V = 3.1$  (39%, dashed line), and  $R_V = 5.5$  (33%, dot-dashed line). Also shown are the observed extinction toward the GC by Nishiyama *et al.* (2009; green triangles) and the best fit with our dust model (see Section 3; red dotted line).

model to fit the GC observed extinction well. However, the ice features only appear in dense regions, while the flat extinction in the 3–7  $\mu$ m range is observed towards many different sightlines, including both diffuse clouds and dense clouds. It is highly possible that some dust materials other than ices are responsible for the flat MIR extinction towards the GC and elsewhere.<sup>7</sup> The silicate-graphite dust model considered here is suitable for the diffuse ISM and does not include ice and aliphatic hydrocarbon material. Therefore we do not expect to reproduce the 3.1  $\mu$ m H<sub>2</sub>O ice feature and the 3.4  $\mu$ m aliphatic C–H feature.

However, these extinction features could be properly reproduced if the appropriate candidate materials are added in the dust model. For the 3.4  $\mu$ m aliphatic C–H feature, Draine (2003) argued that if the graphite component is replaced with a mixture of graphite and aliphatic hydrocarbons, it seems likely that the extinction curve, including the  $3.4\,\mu\text{m}$  feature, could be reproduced with only slight adjustments to the grain size distribution. The  $3.1 \,\mu\text{m}$  H<sub>2</sub>O feature may be more complicated because the H<sub>2</sub>O feature usually appears in sightlines passing through dense molecular clouds. In cold, dense molecular clouds, interstellar dust is expected to grow through coagulation (as well as accreting an ice mantle) and the dust is likely to be porous (Jura, 1980). Therefore, introducing a porous structure with ices coated on silicate, graphite and aliphatic hydrocarbon dust, both the H<sub>2</sub>O absorption feature and the 3.4  $\mu$ m aliphatic C-H feature could be reproduced in the model extinction curves (Zubko et al., 2004; Gao et al., 2010).

### 4.2 $A_v$ : The extinction at the visual band

Rieke *et al.* (1989) estimated the visual extinction toward the GC to be  $A_V \approx 31$  mag based on the extinction law of Rieke and Lebofsky (1985) ( $R_V = 3.1$ ). Our best-fit model for the Rieke *et al.* (1989) extinction law also gives  $A_V \approx$ 31.4 mag. However, with  $\beta \approx -2.11 \pm 0.06$ , Fritz *et al.* (2011) obtained  $R_V \approx 2.48 \pm 0.06$  for the extinction toward the GC based on the correlation between  $R_V$  and the IR power-law index  $\beta$  of Fitzpatrick and Massa (2009). Fritz *et al.* (2011) obtained  $A_V \approx 44$  mag by extrapolating this curve. They also argued that the X-rays can shed lights on  $A_V$ , and  $A_V$  toward the GC may be higher, up to ~59 mag (assuming different  $N_H/A_V$  ratios).

Our model extinction curves suggest that models for small  $R_V$  ratios work better for the steep NIR extinction obtained by Fritz et al. (2011). Since a smaller  $R_V$  ratio implies a higher  $A_{\rm V}$  (on a per unit NIR extinction basis), this again suggests that  $A_V$  toward the GC is probably larger than previous estimated. Our best-fit models suggst that  $A_V$  toward the GC is ~ 42 mag (see Table 1). If we do not fix the total silicate  $(V_{tot,si})$  and graphite volume  $(V_{tot,c})$ , instead, we allow the quantity of the silicate component to vary with respect to that of graphite: by taking the silicate-to-graphite mass ratio to be  $m_{\rm gra}/m_{\rm sil}$  = 0.4, 0.5, and 0.6, our model results show that  $A_{\rm V}$  toward the GC is in the range of  $\sim$  35–45 mag. In the diffuse ISM,  $A_V/N_H \approx 5.3 \times 10^{-22} \text{ mag cm}^2$  (WD01), which leads to  $N_H \approx 7.7 \times 10^{22} \text{ cm}^{-2}$  for our best "CASE B" model extinction curve. However, towards the GC, the interstellar environments should be much denser than that of the diffuse ISM. Although  $A_V/N_H$  is less clear for dense clouds, Cardelli et al. (1989) and Draine (1989) argued that  $A_{\rm I}/N_{\rm H} \approx 2.6 \times 10^{-22} \,{\rm mag}\,{\rm cm}^2$  typical of the diffuse ISM may also hold for dense clouds. If this is indeed the case, we estimate the column density  $N_{\rm H}$  for the sightline toward

<sup>&</sup>lt;sup>7</sup> Fritz *et al.* (2011) (see their section 5.6) argued the flat MIR extinction is not caused by the molecular clouds in front of the GC, which produce the ice features on the extinction curves. They also argued (see their section 5.8) that something else aside from ices produces the flat MIR extinction towards the GC and elsewhere, and additional pure ice grains produce the extinction features towards the GC.

the GC to be  $N_{\rm H} \approx 6.42 \times 10^{22} \,{\rm cm}^{-2}$  for our best "CASE B" model extinction curve ( $A_{\rm I} \approx 16.69 \,{\rm mag}$ ). It is smaller than  $N_{\rm H} \approx (10.5 \pm 1.4) \times 10^{22} \,{\rm cm}^{-2}$  obtained by Fritz *et al.* (2011) which implies  $A_{\rm V}/N_{\rm H} \approx 6.6 \times 10^{-22} \,{\rm mag} \,{\rm cm}^2$ . It is also much smaller than that of Nowak *et al.* (2012), who derived the X-ray absorbing column density to be  $N_{\rm H} \approx 15 \times 10^{22} \,{\rm cm}^{-2}$ .

## 4.3 A simple model based on combinations of multiextinction curves

When the starlight from the GC reaches us, it may have passed through the spiral arms where star formation is actively occurring, diffuse regions, and dense regions of molecular clouds. McFadzean et al. (1989) argued that the molecular clouds along the line of sight toward the GC may contribute as much as  $\sim 1/3$  ( $\sim 10$  mag) of the total visual extinction  $A_{\rm V}$ . Therefore, the extinction curve toward the GC may be a combination of different extinction curves produced by dust grains in different environments of different size distributions. The best fits of this trimodal model are shown in the last two rows of Table 1. The first row shows the best fit derived by varying the contribution of different extinction curves (i.e.  $R_V$ ), while the 2nd row is for fixing the  $R_V = 5.5$ -type extinction to account for 1/3 of the total extinction if we assume the molecular cloud contributes as much as  $\sim 1/3$  ( $\sim 10$  mag) of  $A_V$  towards the GC. As shown in Fig. 4, the observed IR extinction of the GC is fitted well in terms of three different extinction curves, characterized by  $R_{\rm V} = 2.1, 3.1, \text{ and } 5.5, \text{ respectively, each}$ contributing 30%, 49%, and 21% of the total  $A_{\rm V}$ , with the  $R_{\rm V} = 2.1$  extinction representing that of the region where the dust subjects to heavy processing such as in HD 210121, a high Galactic latitude cloud (Larson et al., 1996; Li and Greenberg, 1998).<sup>8</sup> Although the  $\chi^2$  is not lower than that of single  $R_V$  models (see Table 1), we think that the trimodal model is an useful description because it seems reasonable that the dust in the lines of sight towards the GC is characteristics of different environments.

### 5. Summary

The ~1–19  $\mu$ m IR extinction curve of the GC recently derived by Fritz *et al.* (2011) is fitted with a mixture of graphite and amorphous silicate dust. The model has difficulty in simultaneously reproducing the steep NIR extinction and the flat MIR extinction. The best-fit model estimates the total visual extinction toward the GC to be  $A_V \sim 38-42$  mag. In view that the starlight from the GC passes through different interstellar environments, the observed extinction curve toward the GC could be a combination of different extinction curves produced by grains with different size distributions characteristic of different environments: dust in diffuse regions (characterized by small  $R_V$  and steep near-IR extinction), and dust in dense regions (characterized by large  $R_V$  and flat UV extinction).

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<sup>&</sup>lt;sup>8</sup> In Fig. 4, although it appears to fit the extinction well in the range of  $1.2-8.0 \,\mu$ m, the  $R_V = 2.1$  (HD 210121) extinction curve actually is not the suitable extinction curve for the interstellar environment towards the GC because it predicts a very strong silicate absorption feature at 9.7  $\mu$ m.

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