A new constraint for chondrule formation: condition for the rim formation of barred-olivine textures

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A barred-olivine (BO) chondrule usually has an olivine rim that covers the chondrule surface. Numerous experiments have been carried out to reproduce the BO texture. However, the rim structure could be reproduced only in a few studies reported in the literature. The difficulty in reproducing the rim structure lies in the fact that its formation condition has not been constrained experimentally or theoretically. In the present paper, we have carried out numerical simulations of crystal growth of a highly-supercooled melt droplet of pure forsteritic composition (Mg₂SiO₄), and succeeded in reproducing the double structure, i.e. the rim and the dendrite. The droplet cools from the surface, the temperature of which should be cooler than the center of the droplet. Since a crystal grows faster along the cooler surface than across the hotter center, the rim was found to be formed when the temperature difference between the center of the droplet and its surface is large enough. From our results, both from numerical simulations and analytical consideration, we found that the double structure of rim and the dendrite could be formed only when the cooling rate is within a narrow range, which depends upon the degree of supercooling. Our results, for the first time, could explain why the formation of rim of BO texture was hardly reproduced in the previous experiments reported in the literature to date.

Key words: Chondrule solidification texture, melt growth, supercooling, hypercooling, phase-field simulation.

1. Introduction

Chondrules are millimeter-sized, spherical-shaped grains containing olivine, pyroxene, metal, sulfide, and glass with igneous textures. They are considered to have been formed from molten droplets about 4.6 billion years ago in the solar nebula (Amelin et al., 2002); it is believed that they melted and cooled again to solidify in a short period of time (Sorby, 1877; Nelson et al., 1972; Tsuchiyama et al., 1980; Lofgren and Russell, 1986; Jones and Lofgren, 1993; Osada and Tsuchiyama, 2001; Tsuchiyama et al., 2004). Since chondrules possess about 80 vol.% of chondritic meteorites in the most abundant cases (Jones et al., 2000), they must carry information about the early history of our solar system. Chondrules have various textures commonly described as porphyritic, barred, and radial textures; all of these textures appear for the same chondrule bulk composition (Lux et al., 1981; Lofgren and Russell, 1986). Many authors have carried out dynamic crystallization experiments to constrain the formation condition of each texture (Hewins et al., 2005 and references therein), however, the formation mechanism is not yet fully understood.

Barred-olivine (BO) chondrules are characterized by parallel set(s) of olivine bars in a thin section (Weisberg, 1987).

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It has been considered that olivine bar crystals are actually platy in three-dimensions (Tsuchiyama et al., 2000; Noguchi, 2002). A BO chondrule usually has an olivine rim that covers the chondrule surface. This olivine rim has the same crystallographic orientation as inner olivine platelets. The olivine rim has not been reproduced in early dynamic crystallization experiments except in a limited number of runs (Lofgren and Lanier, 1990; Radomsky and Hewins, 1990). Tsukamoto et al. (1999, 2001) succeeded in reproducing the rim structure from a forsterite melt droplet in a container-less crystallization experiment using an aeroacoustic levitation technique. They found from their in-situ observation that the droplet cooled very rapidly at a rate of $R_{\rm cool} \approx 100{\text -}1000~{\rm K~s^{-1}}$, and then crystallized at a large supercooling of $\Delta T \approx 600$ K within a very short period of time (less than 1 s). However, they reproduced the rim structure only in a few cases, so the formation condition was not constrained from their experiments. On the other hand, Tsuchiyama et al. (2004) also succeeded in reproducing the rim structure by evaporation in vacuum. The cooling rate was $R_{\text{cool}} = 1000 \text{ K hr}^{-1}$, which is much slower than that of the container-less experiments by about three orders of magnitude. They did not observe the solidification process of the sample in-situ, so detailed information such as the timing of nucleation, the solidification timescale, and crystal growth pattern were not available. They considered that the rim was formed by the rapid crystal growth along the droplet surface, which should become cooler than the interior because of the latent heat of evaporation. However, their hypothesis has not been verified yet.

To clarify the formation condition of the rim, the crystallization process inside the chondrule melt droplet should be investigated. We carried out numerical simulations of crystallization of a highly-supercooled melt droplet with a pure forsteritic (Mg₂SiO₄) composition (Miura *et al.*, 2010). We considered the situation that a tiny crystal seeded at the droplet surface triggers crystallization of the droplet. We found that the rapid crystal growth along the droplet surface occurs when the cooling rate is very large. However, we did not investigate over a wide range of supercooling of the droplet in the previous paper.

The aim of this paper is to clarify the formation condition of the rim structure. We carry out numerical simulations for a wide range of supercooling and cooling rate by using the phase-field method, which is one of the most effective numerical methods to simulate crystal growth in a supercooled liquid. As a first step, we consider the situation of container-less crystallization experiments using levitation methods (Tsukamoto *et al.*, 1999, 2001; Nagashima *et al.*, 2006, 2008; Srivastava *et al.*, 2010) because in these experiments the thermal profile of the droplet and the crystal growth pattern were observed in-situ, so we can verify the results of our numerical simulations. For comparison, we consider a droplet of pure forsteritic (Mg₂SiO₄) composition, which was adopted in these experiments.

Glass formation, which is expected to occur when a melt droplet cools very rapidly, is not taken into consideration in this paper. Tangeman et~al.~(2001) reported the first synthesis of a forsterite (Mg₂SiO₄) composition glass using containerless conditions. Nagashima et~al.~(2008) summarized the condition for glass formation in a Mg₂SiO₄-MgSiO₃ system for various cooling rates (see their figure 4). Under levitated conditions, a pure forsterite melt becomes a glass when it cools at $R_{\rm cool} \approx 300~{\rm K~s^{-1}}$ or faster. In contrast, under non-levitated conditions, an extremely large cooling rate of $R_{\rm cool} \approx 10^6$ – $10^7~{\rm K~s^{-1}}$ is required for glass formation because of the heterogeneous nucleation on the contact area (e.g., sample holder). This suggests that glass formation from a pure forsteritic melt is very difficult once nucleation occurs.

We describe the basic equation of the phase-field method in Section 2, where the basic concept of the phase-field method is summarized in Appendix A. In Section 3, we show the results of the calculation, in which various crystal growth patterns appear inside the droplet. In Section 4, we discuss the conditions for rapid crystal growth along the droplet surface and propose a new constraint for chondrule formation, especially, for barred-olivine chondrules. We present some conclusions in Section 5.

2. Method

2.1 Basic equations

We employ the phase-field method for the crystallization of a pure material from its melt (model I in Wang *et al.*, 1993). In their model, the solid and liquid phases were distinguished by $\phi = 0$ and $\phi = 1$, respectively. We adopt the same basic equations as those used in our previous paper, in which the cooling term at the droplet surface was

taken into consideration (Miura *et al.*, 2010). The time evolutions of phase ϕ and temperature T are given by

$$\frac{W}{\mu}\frac{\partial\phi}{\partial t} = \frac{\sqrt{2}}{12}\frac{T_{\rm M}}{T}p'(\phi)(T - T_{\rm M}) - \frac{T_{\rm M}\Gamma}{4W}g'(\phi) + T_{\rm M}\Gamma W\nabla^2\phi \tag{1}$$

and

$$\frac{\partial}{\partial t} \int_{V} \left[cT + Lp(\phi) \right] dv = \oint_{A-A_s} \kappa \nabla T \cdot \mathbf{n} \, d\mathbf{a} - \oint_{A_s} q_s \, d\mathbf{a}, \tag{2}$$

respectively, where μ is the kinetic coefficient (see Eq. (A.5)), $T_{\rm M}$ is the equilibrium melting point, $\Gamma \equiv \sigma/L$ is the capillary length, σ is the interfacial free energy between crystal and liquid, L is the latent heat of crystallization per unit volume, W is the thickness of the solidliquid interface, c is the volumetric heat capacity per unit volume, and κ is the thermal conductivity. Functions $p(\phi)$ and $g(\phi)$ are given by $p(\phi) = \phi^3(10 - 15\phi + 6\phi^2)$ and $g(\phi) = \phi^2 (1 - \phi)^2$, respectively, and the prime indicates the derivative by ϕ . Equation (2) can be obtained by integrating a time-dependent thermal diffusion equation over a small volume element V having a boundary A and then applying Gauss's theorem (Miura et al., 2010). A_s is an intersection of the boundary A and the droplet surface if such a surface exists. n is the outward pointing unit normal of the boundary da. The second term of Eq. (2) represents the energy loss at the droplet surface caused by thermal radiation, thermal conduction with ambient nebula gas, and latent heat of evaporation, where q_s is the net heat flux.

Although one could introduce anisotropies in μ and σ to express an anisotropic interface and to simulate facet formation (McFadden *et al.*, 1993; Uehara and Sekerka, 2003), for simplicity we do not take anisotropy into account.

The governing equation of phase ϕ , Eq. (1), was derived from an entropy function to satisfy the entropy production being positive in any small volume element (Wang *et al.*, 1993). The details of the derivation will be found in the reference. We briefly describe the physical meaning of Eq. (1) in Appendix A.

2.2 Numerical scheme

Chondrules are three-dimensional spherules, so a three-dimensional calculation is desirable. However, this requires an unrealistically large number of computational nodes for a chondrule-sized object ($\sim 10^9~\mu m^3$). To reduce the computational cost, we consider a two-dimensional disk in the xy-plane (circle but not a sphere), assume uniformity in the z-direction and drop the derivative by z. Figure 1 shows a schematic picture of the square mesh used for computation. We adopt a computational domain of $-250 \le x \le 250~\mu m$ and $-250 \le y \le 250~\mu m$ to consider a droplet of $250~\mu m$ in radius, and discretized by a 1000×1000 square mesh (mesh sizes for x- and y-directions are $\Delta_x = \Delta_y = 0.5~\mu m$). Other numerical procedures are the same as Miura et~al.~(2010).

We carried out a convergence test with smaller mesh sizes of $\Delta_x = \Delta_y = 0.25 \ \mu \text{m}$, and found that the calculation result was not modified except for minor changes in the shapes of dendrite tips.

We put a seed crystal at the droplet surface to trigger the crystal growth of the supercooled droplet. At the beginning

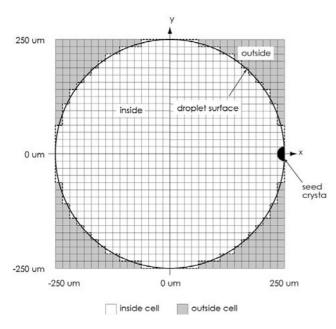


Fig. 1. Two-dimensional square mesh for computation. The thick solid curve is the *actual* surface of droplet. The computational cells inside (white) and outside (gray) the *actual* surface are defined by whether positions of their centers locate the inside or outside, respectively. The *computational* surface (thick dashed lines) is the mesh boundaries between inside cells and outside cells. The crystal growth is triggered by a seed crystal at the droplet surface.

of the calculation, we substitute $\phi=0$ only at the seeding point without any change in temperature (see Fig. 2(a), for example). The radius of the seed crystal is assumed to be $10 \ \mu m$.

2.3 Initial temperature profile

In this paper, we suppose that a completely-molten melt droplet cools rapidly from the surface. Due to the surface cooling, the droplet surface is cooler than the center. The temperature profile inside the droplet is given by an analytic solution of the thermal diffusion equation assuming a uniform cooling $(\partial T/\partial t$ does not depend on r) and a constant value of q_s (Miura $et\ al.$, 2010). The analytic solution is given by

$$T_0(r) = T_{s,0} + \delta T_{c-s,0} \left[1 - \left(\frac{r}{r_d} \right)^2 \right],$$
 (3)

where $T_{s,0}$ is the temperature at the droplet surface, r_d is the droplet radius, and

$$\delta T_{\rm c-s,0} = \frac{q_{\rm s} r_{\rm d}}{2\kappa_{\rm L}} \tag{4}$$

is the temperature difference between the center and surface of the droplet with the thermal conductivity of the liquid phase equal to κ_L . The subscript "0" means t=0, namely, at the time when the seeding occurs.

2.4 Physical properties of forsterite sample

In this study, we consider the sample of pure forsteritic composition. The physical properties we adopted are as follows; $c = 5.7 \times 10^7$ erg cm⁻³ K⁻¹, $L = 2.4 \times 10^{10}$ erg cm⁻³, $T_{\rm M} = 2163$ K (Nagashima *et al.*, 2006, 2008), $\kappa_{\rm C} = 5.0 \times 10^5$ erg cm⁻¹ K⁻¹ s⁻¹ (Pertermann and Hofmeister,

2006), $\kappa_{\rm L}=2.0\times10^5~{\rm erg~cm^{-1}~K^{-1}~s^{-1}}$ (Moriya, 1963), $\sigma=620~{\rm erg~cm^{-2}}$ (Tanaka *et al.*, 2008), $\mu=0.4~{\rm cm~s^{-1}~K^{-1}}$ (Tsukamoto *et al.*, 1999, 2001; Nagashima *et al.*, 2006), and $W=0.25~\mu{\rm m}$ (Murray *et al.*, 1995), where $\kappa_{\rm C}$ is the thermal conductivity of the crystal phase. These parameters are the same as those adopted in Miura *et al.* (2010).

2.5 Input parameters

2.5.1 Heat flux at droplet surface q_s Let us estimate the heat flux q_s at the droplet surface from containerless crystallization experiments (Tsukamoto *et al.*, 1999; Nagashima *et al.*, 2006, 2008). Samples were melted during levitation using a CO₂ laser and then quenched by turning off the laser (Tsukamoto *et al.*, 1999). In this case, the droplet cools at a maximum rate due to the thermal radiation and the heat conduction by the gas-jet (Nagashima *et al.*, 2008). The cooling rate can be controlled to be slower by adjusting the output power of the laser (Nagashima *et al.*, 2006).

The net heat flux at the droplet surface determines the cooling rate of the droplet R_{cool} . The heat flux q_s is calculated by (Miura *et al.*, 2010)

$$q_{\rm s} = c r_{\rm d} R_{\rm cool} / 3. \tag{5}$$

In Table 1, we summarize the cooling rate $R_{\rm cool}$ and the heat flux $q_{\rm s}$ expected in container-less experiments. In this table, we use c of a pure forsteritic melt (see Section 2.4). The typical heat flux is found to be $q_{\rm s}\approx 10^8-10^9$ erg cm⁻² s⁻¹. Based on Table 1, we adopt the following values; $q_{\rm s}=5\times 10^8, 1\times 10^9, 2\times 10^9, 5\times 10^9, 1\times 10^{10}$ erg cm⁻² s⁻¹. The smallest value is the same order of magnitude to that estimated from the container-less experiments. The reason why we consider larger $q_{\rm s}$ values is to see how the growth pattern changes at such an extremely large cooling rate.

2.5.2 Supercooling at droplet surface $\Delta T_{s,0}$ The molten droplet becomes largely supercooled by a few hundred K or more in the container-less environment (Nelson et al., 1972; Tsukamoto et al., 1999; Nagashima et al., 2006, 2008; Tanaka et al., 2008). Tsukamoto et al. (1999) carried out container-less crystallization experiments by using an aero-acoustic levitator and observed a forsterite melt droplet being supercooled by $\Delta T \approx 600 \text{ K}$ at a cooling rate of $R_{\rm cool} \approx 400~{\rm K~s^{-1}}$. Nagashima *et al.* (2006) adopted a gasjet levitator and observed a forsterite melt droplet being supercooled by $\Delta T \approx 1000$ K at a cooling rate of $R_{\rm cool} \approx 100$ K s $^{-1}$. Tanaka *et al.* (2008) modeled the homogeneous nucleation and sequential crystal growth inside a supercooled melt droplet based on classical nucleation theory and found that a forsterite melt droplet should be supercooled by about 1000 K even if it cools at a much smaller cooling rate, e.g., $R_{\rm cool} = 10^{-2} \,\mathrm{K \ s^{-1}}.$

In this paper, we suppose that a forsterite melt droplet never nucleates homogeneously at a relatively low supercooling ($\Delta T < 600$ K), so the crystallization is triggered by a collision with a micron-sized crystal (seeding). Depending on the timing of the seeding, crystallization occurs at various values of supercooling. In this paper, we adopt values of the supercooling at the droplet surface when the seeding occurs of $\Delta T_{\rm s,0} = 200$ K, 300 K, 400 K, 500 K, and 600 K.

Table 1. Cooling rate R_{cool} of molten droplet in container-less crystallization experiments using levitation methods. We read R_{cool} from each cooling curve obtained at each experiment just before the droplet crystallized. We calculate the heat flux q_s and the initial temperature difference between the center and surface of the droplet $\delta T_{c-s,0}$ by using Eqs. (5) and (4), respectively. Refs: [1] Tsukamoto *et al.* (2001), [2] Nagashima *et al.* (2006), [3] Nagashima *et al.* (2008).

Sample	Radius	Cooling rate	Heat flux	Temp. diff.	Levitation	Ref.
composition	$r_{ m d} \ [\mu m m]$	$R_{\rm cool} [{\rm K \ s^{-1}}]$	$q_{\rm s} [{\rm erg} {\rm cm}^{-2} {\rm s}^{-1}]$	$\delta T_{\mathrm{c-s,0}}$ [K]	method	
forsterite	≈1000	≈350	$\approx 6.7 \times 10^{8}$	≈170	aero-acoustic	[1]
forsterite	≈1000	≈50	$\approx 1.0 \times 10^8$	≈25	gas-jet	[2]
forsterite	≈1000	≈70	$\approx 1.3 \times 10^8$	≈10	gas-jet	[3]
$Mg_{1.8}SiO_{3.8}$	≈1000	≈30–40	$\approx (0.6-0.8) \times 10^8$	≈5	gas-jet	[3]

Here, we introduce a hypercooling limit ΔT_{hyp} defined by (Glicksman and Schaefer, 1967; Herlach, 1994);

$$\Delta T_{\text{hyp}} = L/c.$$
 (6)

The crystallization process from a highly supercooled melt changes drastically when the supercooling exceeds ΔT_{hyp} . When $\Delta T < \Delta T_{\text{hyp}}$, crystallization takes place by a twostep process. Once nucleation has initiated solidification, the subsequent growth of the solid phase leads to the release of the latent heat of crystallization. In the case of rapid crystal growth, a steep rise in temperature will occur, termed recalescence, which takes place under nearadiabatic conditions. After recalescence, some fraction of the liquid phase still remains. The remaining liquid will solidify under near-equilibrium conditions as the latent heat is removed. The latter step was termed a "filling-in" process (Chalmers, 1964). On the other hand, when $\Delta T > \Delta T_{\rm hyp}$, the supercooled melt solidifies exclusively during recalescence, so there is no remaining liquid because the droplet temperature during recalescence does not exceed the melting point. The hypercooling limit of a pure forsterite melt is $\Delta T_{\text{hyp}} = 425 \text{ K}$ (Nagashima *et al.*, 2006).

3. Result

3.1 Dendritic growth

Figure 2 shows a result of phase-field simulation for $\Delta T_{s,0} = 200 \text{ K} (T_{s,0} = 1963 \text{ K}) \text{ and } q_s = 5 \times 10^8 \text{ erg cm}^{-2}$ s⁻¹. This is a gray contour map of the phase value ranging from $\phi = 0$ (solid phase, black) to $\phi = 1$ (liquid phase, white). The transition layer between the solid and liquid is too thin to distinguish in this map, meaning that the solidliquid interface is very sharp. At the beginning, there is a tiny seed crystal on the right hand side at the droplet surface (panel (a)). At 0.02 s after seeding, a dendritic crystal grows from the seed crystal (panel (b)). The temperature distribution is shown by isothermal lines in terms of $T-T_{\rm M}$. Crystal growth is accompanied by release of the latent heat of crystallization, so the temperature around the dendritic crystal increases up to almost the melting point. On the other hand, the supercooling far from the dendritic crystal is still large, resulting in a steep temperature gradient ahead of the growing dendrite tips. The dendritic crystal is spreading into the entire region inside the droplet (panel (c)). Around 0.06 s after seeding, the rapid dendritic crystal growth comes to a stop because the temperature inside the droplet increases to the melting point (panel (d)). It is found that a liquid phase still remains at the gap between dendrite tips. Finally, the remaining liquid solidifies completely as the latent heat of

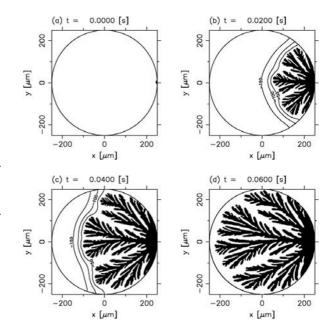


Fig. 2. Result of phase-field simulation for $\Delta T_{\rm s,0}=200~{\rm K}$ and $q_{\rm s}=5\times10^8~{\rm erg~cm^{-2}~s^{-1}}$. A circle of 250 $\mu{\rm m}$ in radius is the external shape of droplet and the target of the calculation is only inside the circle. Black and white regions represent crystal and liquid phases, respectively. The temperature distribution is shown by contours with labels indicating $T-T_{\rm M}$, namely, negative and positive labels mean supercooled and above melting point, respectively. The interval of the isotherms is 50 K. The initial condition (a), and $t=0.02~{\rm s}$ (b), 0.04 s (c), and 0.06 s (d) after seeding.

crystallization is removed by the surface cooling. It took 0.42 s to solidify completely. The luminosity of the droplet increases rapidly from panel (a) to (d), and then decreases gradually (Miura *et al.*, 2010).

3.2 Dendritic growth with rim structure

Figure 3 shows a result for $\Delta T_{\rm s,0}=300~{\rm K}~(T_{\rm s,0}=1863~{\rm K})$ and $q_{\rm s}=2\times10^9~{\rm erg~cm^{-2}~s^{-1}}$. At the beginning, one can see concentric isothermal lines of $T_0-T_{\rm M}=-250~{\rm K}$ and $-200~{\rm K}$ (panel (a)), meaning that there is a large temperature difference between the center and surface of the droplet. The temperature difference calculated by Eq. (4) is $\delta T_{\rm c-s,0}=125~{\rm K}$, so the temperature at the droplet center $(T_0-T_{\rm M}=-175~{\rm K})$ is 175 K below the melting point. At 0.008 s after seeding, a dendritic crystal grows from a seed crystal as well, as shown in Fig. 2(b) (panel (b)). At 0.016 s after seeding, it is found that the dendritic crystal growing across the droplet center is suppressed compared with Fig. 2(c) (panel (c)). At 0.024 s after seeding, the crys-

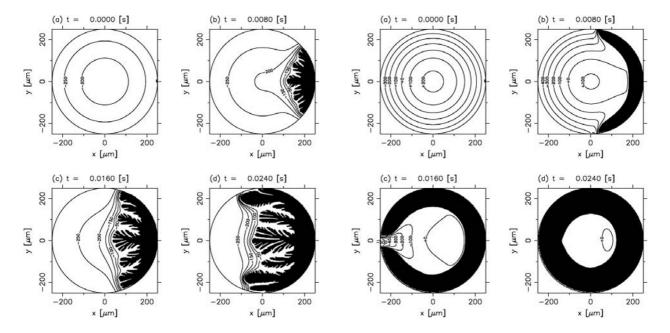


Fig. 3. Result of phase-field simulation for $\Delta T_{\rm s,0}=300$ K and $q_{\rm s}=2\times10^9$ erg cm⁻² s⁻¹. The initial condition (a), and t=0.008 s (b), 0.016 s (c), and 0.024 s (d) after seeding. Others are the same as Fig. 2.

Fig. 4. Result of phase-field simulation for $\Delta T_{\rm s,0} = 400$ K and $q_{\rm s} = 1 \times 10^{10}$ erg cm⁻² s⁻¹. The interval of the isotherms is 100 K. The initial condition (a), and t = 0.008 s (b), 0.016 s (c), and 0.024 s (d) after seeding. Others are the same as Fig. 2.

tal is growing rapidly along the droplet surface (panel (d)). The crystal along the droplet surface is one of the branches of the dendritic crystal, and it seems to be surrounding the droplet like the rim of a BO chondrule.

3.3 Rim growth

Figure 4 shows a result for $\Delta T_{\rm s,0}=400~{\rm K}~(T_{\rm s,0}=1763~{\rm K})$ and $q_{\rm s}=1\times10^{10}~{\rm erg~cm^{-2}~s^{-1}}.$ One can see dense concentric isotherms at the beginning (panel (a)). The temperature difference between the center and surface is calculated to be $\delta T_{\rm c-s,0}=625~{\rm K}$ from Eq. (4). The inner most isotherm is $T_0-T_{\rm M}=200~{\rm K}$, indicating a temperature above the melting point. The crystal growth pattern is completely different from Figs. 2 and 3. No dendritic crystal grows inside the droplet (panel (b)). The crystal grows only along the droplet surface where the temperature is below the melting point. At 0.016 s after seeding, almost of all of the droplet surface is covered with the crystal (panel (c)). There is liquid remaining inside the crystal rim (panel (d)). The remaining liquid gradually solidifies from the outside to the inside as the latent heat of crystallization is removed through the shell crystal.

3.4 Parallel dendritic growth

Figure 5 shows a result for $\Delta T_{\rm s,0} = 500$ K ($T_{\rm s,0} = 1663$ K) and $q_{\rm s} = 2 \times 10^9$ erg cm⁻² s⁻¹. The temperature difference between the center and surface of the droplet is calculated as $\delta T_{\rm c-s,0} = 125$ K, so the temperature at the center ($T_0 - T_{\rm M} = -375$ K) is 375 K below the melting point. Note that the temperature distribution can be divided into two regions; a hypercooled region along the surface, and normally supercooled at the central region, where "normally" means that the supercooling does not exceed the hypercooling limit $\Delta T_{\rm hyp}$ (see Eq. (6)). The seed crystal grows isotropically at first (panel (b)). However, when the crystal-liquid interface

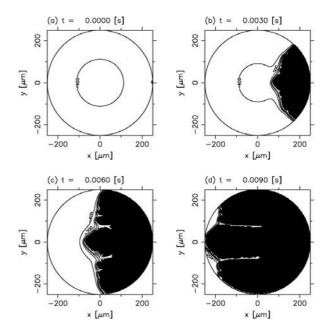


Fig. 5. Result of phase-field simulation for $\Delta T_{\rm s,0}=500$ K and $q_{\rm s}=2\times10^9$ erg cm⁻² s⁻¹. The interval of the isotherms is 100 K. The initial condition (a), and t=0.003 s (b), 0.006 s (c), and 0.009 s (d) after seeding. Others are the same as Fig. 2.

reaches the normally supercooled region, it splits into some parallel branches (panel (c)). After the tips of the branches pass the normally supercooled region, it is found that a liquid phase remains among the branches (panel (d)). The remaining liquid solidifies as the latent heat of crystallization is removed.

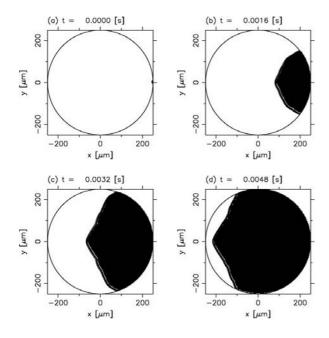


Fig. 6. Result of phase-field simulation for $\Delta T_{\rm s,0}=600$ K and $q_{\rm s}=5\times10^8$ erg cm⁻² s⁻¹. The interval of the isotherms is 100 K. No labels indicating $T-T_{\rm M}$ is displayed for the purpose of visualization. The initial condition (a), and t=0.0016 s (b), 0.0032 s (c), and 0.0048 s (d) after seeding. Others are the same as Fig. 2.

3.5 Isotropic growth

Figure 6 shows a result for $\Delta T_{\rm s,0}=600~{\rm K}~(T_{\rm s,0}=1563~{\rm K})$ and $q_{\rm s}=5\times10^8~{\rm erg~cm^{-2}~s^{-1}}$. The temperature difference between the center and surface of the droplet is only $\delta T_{\rm c-s,0}\approx30~{\rm K}$. The temperature at the center $(T_0-T_{\rm M}=-570~{\rm K})$ is 570 K below the melting point, so the entire droplet is hypercooled. From panels (b)–(d), one can see that the crystal grows isotropically from the seed crystal. There is no remaining liquid after the crystal growth front has passed because the liquid can solidify completely without removal of the latent heat of crystallization. The shape of the crystal-liquid interface is quasi-planar, which denotes macroscopic planarity of the interface, but on the microscopic scale of the heat-flow the interface does not necessarily behave as a plane front (Glicksman and Schaefer, 1967).

4. Discussion

4.1 Constraint on cooling rate for rim formation

Here, we derive the constraint on the cooling rate for rim formation based on the discussion of Miura *et al.* (2010).

Let us consider crystal growth from a seed crystal at one side of the droplet surface to the opposite side. There are two possible routes for crystal growth; along the droplet surface and across the center. For the former case, the distance of the growth route is the longest, however, the growth velocity is the fastest because the surface should be cooler than the center due to surface cooling. Here, we assume that the growth velocity of the crystal is $V(\Delta T_0) \propto \Delta T_0^{\beta}$, where ΔT_0 is the supercooling inside the droplet when the seeding occurs. The index is $\beta \approx 2.5$ –3.5 according to the dendrite growth theory (Langer and Müller-Krumbhaar, 1978; Xu, 1998). Hereinafter, we adopt $\beta = 3$ as a typical value. The growth timescale along the droplet surface τ_s is given by di-

viding the arc distance $\pi r_{\rm d}$ by the growth velocity $V(\Delta T_{\rm s,0})$

$$\tau_{\rm s} = \frac{\pi r_{\rm d}}{V(\Delta T_{\rm s,0})},\tag{7}$$

where we consider a constant supercooling of $\Delta T_{s,0}$, namely, a constant growth velocity along the droplet surface. On the other hand, the growth velocity across the droplet center is not constant because of the temperature gradient inside the droplet (see Eq. (3)). The growth timescale across the center τ_c is given by the following integral form;

$$\tau_{\rm c} = 2 \int_0^{r_{\rm d}} \frac{dr}{V(\Delta T_0(r))} = \frac{2r_{\rm d}}{V(\Delta T_{\rm s,0})} I(\beta, \alpha), \quad (8)$$

where

$$\alpha \equiv \frac{\delta T_{\text{c-s},0}}{\Delta T_{\text{s},0}}, \quad I(\beta,\alpha) \equiv \int_0^1 \frac{d\tilde{r}}{[\alpha(\tilde{r}^2 - 1) + 1]^{\beta}}, \quad (9)$$

r is the distance from the droplet center, and $\tilde{r}=r/r_{\rm d}$. The condition for rapid crystal growth along the droplet surface is given by $\tau_{\rm s}<\tau_{\rm c}$, which is rewritten as

$$I(\beta, \alpha) > \frac{\pi}{2}.\tag{10}$$

By integrating $I(\beta, \alpha)$ numerically, we obtain (Miura *et al.*, 2010)

$$\alpha > \sim 0.2$$
, for $\beta = 3$. (11)

The cooling rate is rewritten as $R_{\rm cool} = 6\alpha \kappa_{\rm L} \Delta T_{\rm s,0}/cr_{\rm d}^2$ by using Eqs. (4), (5), and (9). Substituting Eq. (11) into the expression for the cooling rate, we obtain the formation condition of the rim as

$$R_{\text{cool}} > \sim 2000 \left(\frac{\Delta T_{\text{s},0}}{300 \text{ K}}\right) \left(\frac{r_{\text{d}}}{250 \ \mu\text{m}}\right)^{-2} \text{ K s}^{-1}.$$
 (12)

It should be noted that the condition given by Eq. (11) or (12) is applicable only when $\tau_s < \tau_{cool}$, where τ_{cool} is the cooling timescale of the droplet (Miura *et al.*, 2010). If not, the droplet temperature drops considerably during solidification, so Eq. (3) cannot be used in this analysis. We can apply the condition given by Eq. (11) or (12) to our results because the typical growth timescale of $\tau_s < 0.1$ s is shorter than the cooling timescale of $\tau_{cool} > 0.1$ s.

4.2 Condition to produce each growth pattern

Figure 7 shows the calculation conditions and the resultant crystal growth patterns on a q_s - $T_{s,0}$ diagram. The top border is $\delta T_{c-s,0}$ calculated by Eq. (4). The right border is the normalized supercooling at the droplet surface defined by (Glicksman and Schaefer, 1967)

$$\Delta \theta_{\rm s,0} = \frac{T_{\rm M} - T_{\rm s,0}}{\Delta T_{\rm hyp}}.$$
 (13)

Note that the droplet surface is hypercooled when $\Delta\theta_{s,0} > 1$ (see Eq. (6)). Filled symbols indicate the calculation conditions in which the rim was formed (Section 3.1, 3.2, and 3.3). Two solid curves in Fig. 7 show the conditions of $\alpha=0.2$ and $\alpha=1$, respectively; the former is the criterion for rim formation, and the latter corresponds to the condition above which the temperature at the droplet

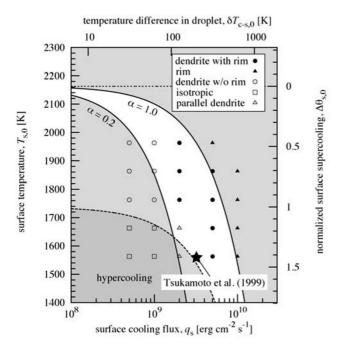


Fig. 7. Calculation conditions and the resultant crystal growth patterns on q_s - $T_{s,0}$ diagram. $\delta T_{c-s,0}$ is the temperature difference between the surface and center of the droplet. $\theta_s = (T_M - T_{s,0})/\Delta T_{hyp}$ is the normalized supercooling at the droplet surface, where ΔT_{hyp} is the hypercooling limit. The solid curves correspond to the conditions of $\alpha=0.2$ and $\alpha=1$, respectively, where $\alpha=\delta T_{c-s,0}/\Delta T_{s,0}$ is the normalized temperature difference. The dashed curve is the criterion below which the entire droplet is hypercooled.

center exceeds the melting point (see Eq. (11)). The rim was found to be formed at conditions to the upper right of the $\alpha=0.2$ curve. From comparison with the results of phase-field simulations, we conclude that the condition given by Eq. (11) or (12) are plausible as the criterion for rim formation.

The dashed curve is the parameter space below which the entire droplet is hypercooled. It is found that isotropic growth (see Section 3.5) occurred at conditions below the dashed curve.

A large star symbol indicates the condition of the container-less crystallization experiment by Tsukamoto et al. (1999), in which the rim surrounding parallel sets of olivine bars was successfully reproduced from a pure forsteritic composition melt droplet. In their experiment, the droplet crystallized at a supercooling of $\Delta T_{\rm s,0} \approx 600$ K, which gives the normalized surface undercooling of $\Delta \theta_{\rm s,0} \approx 1.4$. The temperature difference inside the droplet was estimated as $\delta T_{\rm c-s,0} \approx 170$ K (see Table 1), which gives $\alpha \approx 0.4$. Since this experimental condition satisfied the condition for rim formation, their sample having the rim structure is a reasonable result.

We consider the experimental condition of Tsuchiyama *et al.* (2004). In their experiment, the cooling rate of the droplet was $R_{\rm cool}=1000~{\rm K~hr^{-1}}$ if we assume that it is the same as the cooling rate of the furnace. The temperature difference between the center and surface of the droplet can be estimated as $\delta T_{\rm c-s,0}\approx 0.02~{\rm K}$ for a sample radius of $r_{\rm d}=500~\mu{\rm m}$ and with typical thermodynamic properties of silicates ($c=3\times10^7~{\rm erg~K^{-1}~cm^{-3}}$ and $\kappa_{\rm L}=2\times10^5$

erg cm⁻¹ s⁻¹ K⁻¹, Murase and McBirney, 1973). From the condition of Eq. (11), the molten sample in their experiment must have crystallized at very low supercooling as $\Delta T_{s,0} < 0.1$ K to form the rim. The nucleation at such very small supercooling might be due to the contact of the droplet to the carbon capsule. However, the exact value of the nucleation supercooling was not measured, so we cannot test our new constraint with their experiment. Insitu temperature measurement during droplet solidification is required to clarify the condition of rim formation.

4.3 Implication for chondrule solidification textures

The numerical model that we adopted in this study was used to simulate the crystal growth process in a supercooled melt droplet of a single composition, namely, the composition of the crystal phase is the same as that of the parent liquid phase. However, real chondrules are multi-component, namely, the composition of the crystal phase is not necessarily the same as the bulk composition of the parent liquid (e.g., Jones, 1990). Therefore, not only the temperature distribution inside the droplet, but also the partitioning and diffusion of elements near the crystal-liquid interface (Watson, 1996, 2004) should be taken into consideration. To elucidate the formation mechanism of chondrule solidification textures, it is required to model the crystallization process of a multi-component melt droplet at a largely undercooled state (e.g., Bi and Sekerka, 1998, 2002).

Before the multi-component modeling begins, we make some predictions for chondrule solidification textures based on our single-component phase-field calculations. In our model, the droplet after complete solidification is just a single crystal spherule, probably with no solidification texture remaining inside. However, if the droplet contains small amounts of incompatible elements in olivine, such as Ca and Al, these elements tend to partition into the remaining liquid phase during crystal growth (Libourel, 1999; Pack and Palme, 2003). The inhomogeneity in elemental composition should relate to the solidification texture. Therefore, the distribution of the remaining liquid phase inside the droplet has some implications for the formation mechanism of chondrule solidification textures.

To visualize the distribution of the remaining liquid phase, we introduce a crystallization timescale τ_{cry} into our phase-field calculation. The timescale τ_{cry} shows how long the liquid takes to solidify at a certain position, and it is calculated by

$$\tau_{\text{cry}}^{(i,j)} = t_{0.1}^{(i,j)} - t_{0.9}^{(i,j)},\tag{14}$$

where $t_{0.1}^{(i,j)}$ and $t_{0.9}^{(i,j)}$ are the times when $\phi_{i,j}=0.1$ and 0.9, respectively, at the grid point (i,j). $t_{0.9}^{(i,j)}$ means the time when the liquid at the grid point (i,j) begins to crystallize, and $t_{0.1}^{(i,j)}$ means the time when the grid point is almost completely solidified. The remaining liquid phase should have large $\tau_{\rm cry}$ because it solidified very slowly.

Figure 8 is the gray-scale map of τ_{cry} for each result of the phase-field simulation shown in Figs. 2–6. The gray map shows the value of τ_{cry} on a logarithmic scale; darker gray for rapidly crystallized regions and lighter gray for more slowly crystallized ones. It is found that the shape of the darker gray region corresponds to the crystal growth pattern for each phase-field simulation. In panels (d) and (e), there

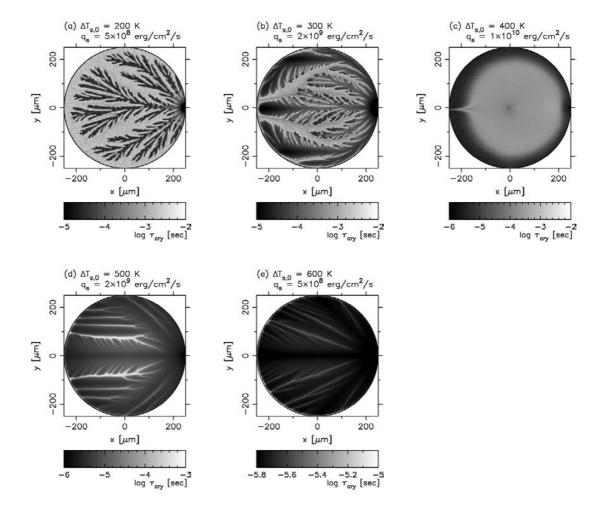


Fig. 8. Distribution of crystallization timescale τ_{cry} in a completely solidified droplet. Panels (a)–(e) correspond to Figs. 2-6, respectively. Note that the range of gray scale are different in each panel.

are some light gray lines that were not clearly identified in Figs. 5 and 6, respectively. These lines correspond to positions of some dents at the quasi-planar crystal-liquid interface. As shown in Figs. 5 and 6, the interface is not a complete plane but has some small undulations. During the advance of the interface, the released latent heat of crystallization poured into the dents by thermal diffusion even at the hypercooled state. The temperature at the dents becomes slightly higher than the ambient region, making the growth speed slower. Therefore, the track of the dent position remains on the map as the region where the liquid solidified more slowly.

The gray-scale map of τ_{cry} just visualized the difference of crystal growth timescale during solidification. The relationship to the chondrule solidification textures was not clear. However, we consider that the chondrule solidification textures reflect the crystal growth pattern inside the droplet. Our phase-field simulations are the first step to understand the formation mechanism of chondrule solidification textures.

5. Conclusion

The chondrule solidification texture reflects the crystal growth pattern inside the melt droplet at the time of forma-

tion in the early solar nebula. We numerically investigated the following two thermal effects on the crystal growth pattern; (i) the cooling at the droplet surface and (ii) the release of latent heat of crystallization. Surface cooling makes the droplet surface cooler than the center. Since the crystal growth rate is faster along the cooler surface than across the hotter center, the rim was formed when the cooling rate is large enough. The release of the latent heat of crystallization caused a rapid temperature increase near the growing rim, resulting in a very steep temperature gradient at the interface between the rim and the remaining liquid (melt) phase. This "reversed" temperature gradient led to dendrite formation due to the morphological instability. We found that the double structure of rim and dendrite could be formed only when the cooling rate is within a narrow range. An understanding of these thermal effects on chondrule melt solidification is the first step to elucidate the formation mechanism of chondrule solidification textures.

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Appendix A. Phase-Field Method (PFM)

The classical approach to the modeling of first order phase transformations involves tracking the free boundary that separates the growing phase (e.g., crystal) from the parent phase (e.g., supercooled liquid). PFM provides an alternative approach, according to which a new variable, the phase field ϕ , is introduced to keep track of the phase, taking on constant values indicative of each of the bulk phases and making a transition between these values over a thin transition layer that plays the role of the classically sharp interface. One of the advantages of PFM is not to require explicit tracking of the free boundary. This makes the numerical model simpler than the classical approach.

In the PFM developed by Wang *et al.* (1993), the crystallization process can be simulated by solving the coupled equations for the phase field and temperature field given by Eqs. (1) and (2), respectively. The latter is easily recognized as the time-dependent thermal diffusion equation taking into account the release of latent heat of crystallization, as explained in the text.

The physical meaning of Eq. (1) except for the diffusion term is that the phase value $\phi(x, t)$ changes to minimize the Helmholtz free energy density $f(T(x, t), \phi(x, t))$ as time goes on, where T is the temperature. The Helmholtz free energy density is given by (Wang $et\ al.$, 1993)

$$\frac{f(T,\phi)}{L} = \frac{T}{T_{\rm M}} \left[\frac{3\sqrt{2}\,\Gamma}{2W} g(\phi) - \frac{T - T_{\rm M}}{T} p(\phi) \right]. \quad (A.1)$$

Figure A.1 shows $f(T,\phi)$ as a function of ϕ . The solid, dashed and dotted curves are for $T=T_{\rm M}$ (equilibrium), $T< T_{\rm M}$ (solidification), and $T>T_{\rm M}$ (melting), respectively. When $T=T_{\rm M}$, $f(T,\phi)$ has two minima at $\phi=0$ (solid) and $\phi=1$ (liquid). This stands for solid-liquid coexistence. When $T< T_{\rm M}$, the minimum at $\phi=0$ is lower than the (local) minimum at $\phi=1$. The difference in free energy between these two minima gives a driving force for solidification. On the contrary, when $T>T_{\rm M}$, the minimum at $\phi=1$ is lower than the (local) minimum at $\phi=0$, leading to melting of the solid phase.

The diffusion term of Eq. (1) makes the crystal-liquid interface smooth. This term represents the effect that the undulated interface in equilibrium with the parent liquid becomes flat. This effect is termed as the Gibbs-Thomson effect, namely, the equilibrium temperature at the curved interface is given by

$$T_{\rm N} = T_{\rm M}(1 - \Gamma/\rho), \tag{A.2}$$

where ρ is a local radius of curvature at a point of the interface (positive ρ when convex toward the liquid). The term $T_{\rm M}\Gamma/\rho$ is the melting point depression due to the surface tension.

In PFM, the solid-liquid interface has finite thickness. The thickness w is obtained from a steady-state solution of Eq. (1) at $T = T_{\rm M}$ (Wang *et al.*, 1993). By dropping the time-derivative term and substituting $T = T_{\rm M}$, Eq. (1) can

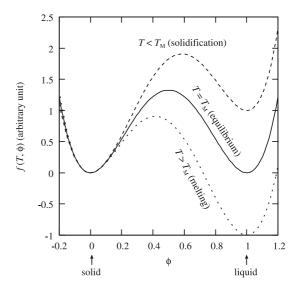


Fig. A.1. The helmholtz free energy density $f(T, \phi)$ adopted in PFM of Wang *et al.* (1993).

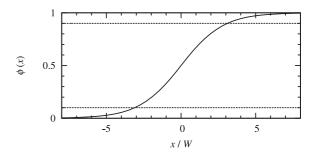


Fig. A.2. One-dimensional solution of Eq. (A.3) under equilibrium condition. $T = T_M$.

be rewritten as

$$\frac{\partial^2 \phi}{\partial x^2} = \frac{1}{4W^2} g'(\phi). \tag{A.3}$$

The solution with boundary conditions $\phi \to 0$ as $x \to -\infty$, and $\phi \to 1$ as $x \to +\infty$ is found to be

$$\phi(x) = \frac{1}{2} \left[\tanh\left(\frac{x}{2\sqrt{2}W}\right) + 1 \right], \quad (A.4)$$

where we have chosen a constant of integration to locate the interface at x=0. Figure A.2 shows this solution with respect to x. If we consider the solid-liquid interface being at $0.1 \le \phi \le 0.9$ (see Section 4.3), the width is found to be $w \approx 6 \, W$.

Wang *et al.* (1993) formulated the phase-field equation to solve the crystal growth velocity V consistently with well-known Wilson-Frenkel low in the limit of $W \to 0$. The Wilson-Frenkel low (Wilson, 1900; Frenkel, 1932) means that the growth velocity V is proportional to the local supercooling, so we obtain

$$V = \mu \left(T_{\rm N} - T \right),\tag{A.5}$$

where the proportionality constant μ is called the kinetic coefficient and represents the efficiency for a growth unit to be incorporated into the crystal phase. Therefore, we can calculate the crystal growth velocity correctly by using a

sufficiently fine computational mesh (Murray et al., 1995; Nelson, L. S., M. Blander, S. R. Skaggs, and K. Keil, Use of a co2 laser Wang and Sekerka, 1996).

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