

Subtle changes in strain prior to sub-Plinian eruptions recorded by vault-housed extensometers during the 2011 activity at Shinmoe-dake, Kirishima volcano, Japan

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This study focuses on strain change observations with a precision of 10^{-9} associated with the 2011 Shinmoe-dake eruptions in Japan, using vault-housed extensometers installed approximately 18 km northwest of the Shinmoe-dake crater. The extensometers recorded major strain changes of 10^{-7} during three sub-Plinian eruptions and subsequent magma effusion. Our analysis indicates that these extensometer records provide a reasonable estimation of the parameters of an isotropic point source that can explain eruption-related ground deformation. The extensometers also recorded subtle strain changes of 10^{-9} prior to the three sub-Plinian eruptions. Time series data indicate that changes in strain at these rates are generally only observed immediately before explosive eruptions, suggesting that these strain changes are precursors to sub-Plinian eruptions. The source of these subtle strain changes is likely to be shallower than the magma chamber associated with these eruptions. The precursory strain changes might have been caused by a pressure increase and a subsequent pressure decrease under the volcano. One possible scenario that can explain these pressure changes is the accumulation of volcanic gases at depth, causing an increase in pressure that was eventually released during gas emissions from the crater prior to the explosive eruptions.

Key words: Extensometer, explosive eruption, sub-Plinian eruption, Shinmoe-dake volcano, Kirishima volcanic group, crustal deformation, magma chamber.

1. Introduction

Some important views on the dynamics of volcanic eruptions owe their origins to precise observations of eruption-related crustal deformations of the order of 10^{-9} in strain and tilt. Previous research has demonstrated that subtle ground deformation occurs prior to the eruptions of some volcanoes, as has been observed using vault-housed extensometers at Sakurajima in Japan (e.g., Kamo and Ishihara, 1986; Ishihara, 1990; Iguchi *et al.*, 2008) and Piton de la Fournaise in the Réunion Islands (Peltier *et al.*, 2007), and by high-precision tiltmeters and dilatometers at the Soufrière Hills volcano on Montserrat (Voight *et al.*, 1998, 1999, 2010; Druitt *et al.*, 2002; Chardot *et al.*, 2010; Linde *et al.*, 2010). Measuring and studying such deformations are clearly important if we are to understand the eruption processes of volcanoes.

However, previously reported examples of eruption-related crustal deformation have not documented all possible types of eruptive activity, and continuous crustal defor-

mation observations, especially high-precision strain observations, have only been undertaken on a few active volcanoes (e.g., Dvorak and Dzurisin, 1997; Peltier *et al.*, 2007). The majority of routine observations have been conducted on volcanoes that frequently erupt (e.g., Linde *et al.*, 1993; Peltier *et al.*, 2007; Iguchi *et al.*, 2008). As a consequence, less frequent events, such as Plinian or sub-Plinian eruptions, have rarely been investigated using continuous crustal deformation data with a precision of 10^{-9} . This situation contrasts sharply with Vulcanian eruptions that have been intensively investigated (e.g., Chardot *et al.*, 2010; Linde *et al.*, 2010; Voight *et al.*, 2010).

Shinmoe-dake, one of the volcanic cones in the Kirishima volcanic group (Fig. 1), erupted in January 2011. This was the first major eruption of Shinmoe-dake in 52 years, although minor eruptions frequently occur, such as those in 1991 and 2010. The 2011 activity was characterized by three sub-Plinian eruptions that were followed by the effusion of magma from the summit crater over 6 days between 26 and 31 January, 2011. This activity was monitored using a dense geophysical network including a global positioning system (GPS) and observations of tilting conducted by several institutions (e.g., Nakao *et al.*, 2013; Ueda *et al.*, 2013). In addition, the Shinmoe-dake activity was observed by vault-housed extensometers at a site approximately 18 km from the summit of the crater (Fig. 1)

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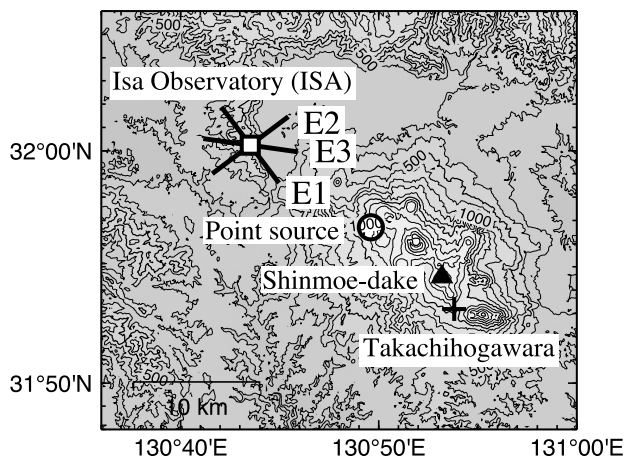


Fig. 1. Map showing the location of the Shinmoe-dake volcano crater (solid triangle) and the ISA site (open square) where strain data were recorded. Thick bars at the ISA site show the directions of extensometers, and contours indicate the surface topography at 100 m intervals. An open circle represents the location of a magma chamber proposed by the Geospatial Information Authority using GPS data, with a cross representing the location of the Takachihogawara seismic station of the Japan Meteorological Agency, where seismograms are recorded in a 100-m-deep borehole.

(Yamazaki *et al.*, 2011).

This paper presents extensional ground strain data with a precision of 10^{-9} , or better, obtained during the most recent eruptions of Shinmoe-dake. In particular, we demonstrate precursory ground deformations of a type that has not previously been recognized.

2. Vault-housed Strain Observations near the Shinmoe-dake Cone and Their Resolution

Strain observations using vault-housed extensometers were obtained at the Isa-Yoshimatu observatory (ISA, at $32^{\circ}00'14.4''N$, $130^{\circ}43'31.4''E$). The summit crater of Shinmoe-dake ($N31^{\circ}54'34''$, $E130^{\circ}53'11''$; Japan Meteorological Agency, 2005) is 18.5 km from the ISA site at an azimuth of $S55.48^{\circ}E$ (Fig. 1). The ISA consists of tunnels in three directions, E1 ($N37^{\circ}W$), E2 ($N53^{\circ}E$), and E3 ($N82^{\circ}W$). Each tunnel houses extensometers made up of 30-m lengths of super-invar rods (Fig. 2). One end of each extensometer is fixed to the ground, and the other end is free. Displacement of the free end is measured at 1-s intervals using a differential transformer, and the amount of displacement is divided by the length of the rod to obtain the ground extension (strain) in the corresponding direction.

The precision of the strain measurement data at ISA is 1×10^{-9} in the E1 and E3 directions. The precision of the E2 component, obtained during the 2011 eruption of Shinmoe-dake, is somewhat poorer than the precision of the E1 and E3 components, at around $2\text{--}3 \times 10^{-9}$, primarily because the electrical system in this part of the vault was damaged during a lightning strike one month before the eruption.

The large distance between the Shinmoe-dake crater and ISA observatory means that the strain data obtained at ISA may be less sensitive to volumetric changes of subsurface pressurized magma than at facilities elsewhere that are closer to the volcanoes being observed. Vault-housed ex-

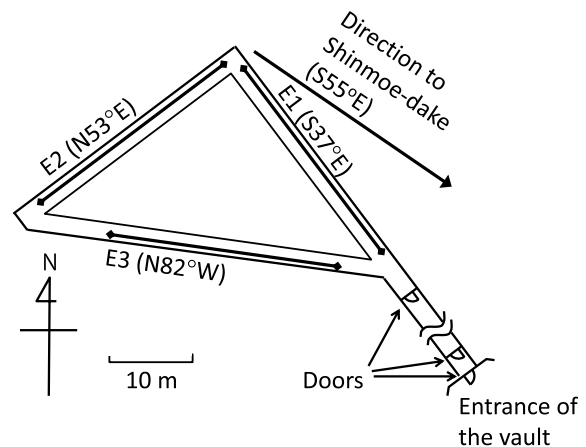


Fig. 2. Plan view of the observational setup at ISA.

tensometers for monitoring specific volcanoes are usually installed at distances less than several kilometers, as exemplified by the vault-housed extensometers at the Harutayama observatory near the Minamidake crater of Sakurajima volcano. These extensometers have similar geometries (i.e., three components arranged in a triangular shape) and lengths (~ 30 m) to the extensometers at ISA, but the distance between the crater and the observatory is < 3 km (e.g., Kamo and Ishihara, 1986).

Nevertheless, we can confirm that the somewhat distal extensometers at ISA are more sensitive to some types of subsurface volume changes than are GPS-based measurements. Assuming that the resolution of displacement using GPS is up to 1 mm, the detection limit for subsurface volume changes using extensometers located 20 km away from the source epicenter is much better than when using densely deployed GPS, except in the case of an extremely shallow source (~ 1 km; see Appendix for detail).

3. Strain Changes Associated with Major Eruptive Events

The most prominent phenomena involved in the 2011 activity of Shinmoe-dake were three sub-Plinian eruptions on 26 and 27 January, 2011, and the subsequent effusion of magma during 28–31 January, 2011. All these events were accompanied by major variations in strain that were recorded at the ISA site. The temporal strain variations are shown in Fig. 3. Strain variations were characterized by an extension in the E1 component and by contraction in the E2 component. The E1 component approximately coincides with the direction of the Shinmoe-dake volcano from the ISA observatory (Fig. 1), indicating that this component is nearly radial to the eruptive vent. In comparison, the E2 direction is perpendicular to this direction and as such is nearly transverse to the eruptive vent.

To clarify the nature of the strain changes generated during the eruptions, we estimated eight major strain time-series tidal components and removed them from the original time series. This was done using the algorithm proposed by Tamura *et al.* (1991) based on Akaike Bayesian Information Criteria (ABIC; Akaike, 1980). Although the underground recording of strain data by extensometers is

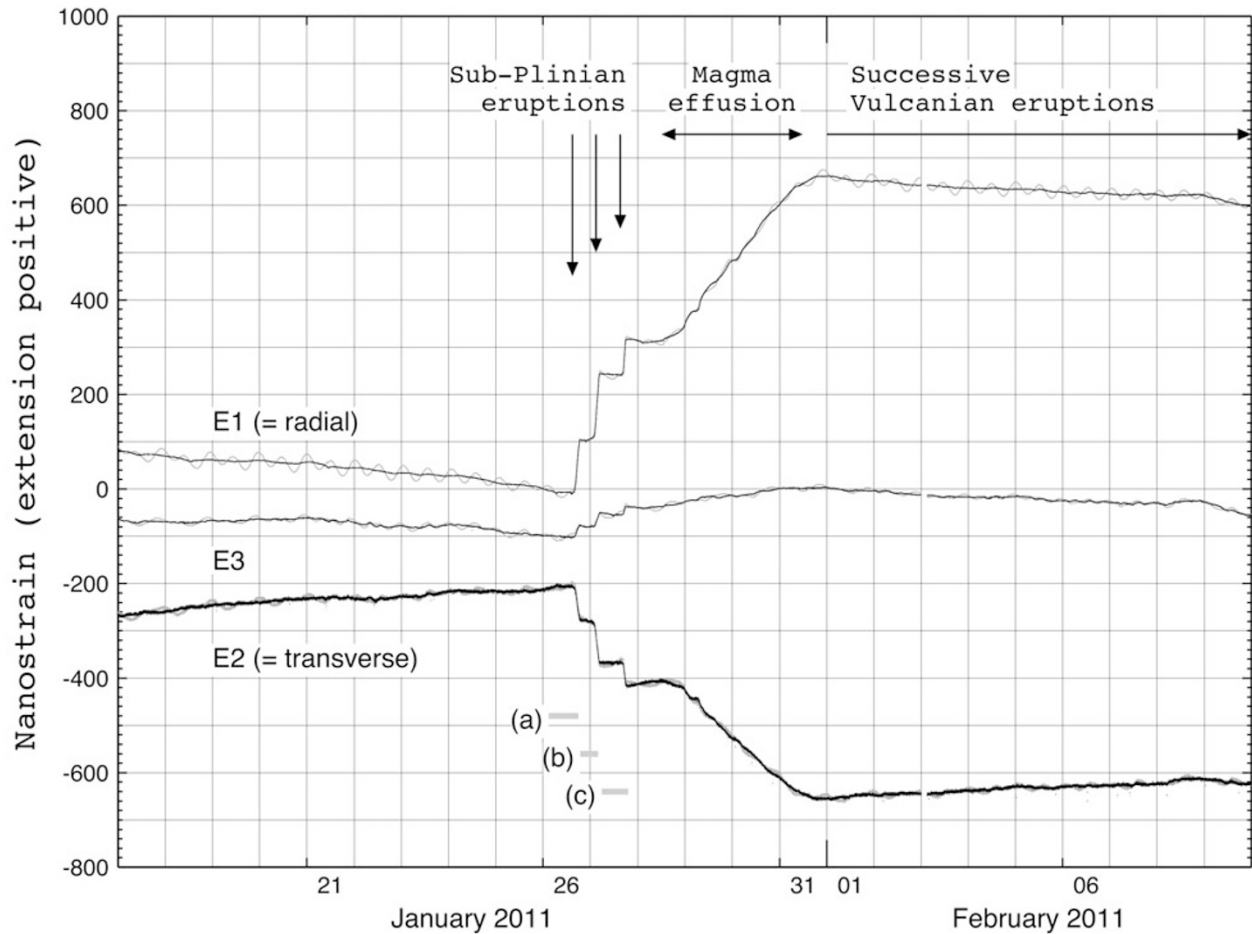


Fig. 3. Strain (extension) time series in E1–E3 directions, with black lines showing time series after the removal of tidal components, and gray lines showing the original time series data. More detailed illustrations of the time series data between the periods indicated by the gray bars (a–c) are shown in Fig. 5.

distorted significantly by precipitation (e.g., Kasahara *et al.*, 1983), the data acquired during the 2011 Shinmoe-dake eruptions were only slightly distorted because the eruptions occurred during a period of low precipitation.

Figure 3 shows that three rapid strain changes occurred at 15:30–18:50 (local time) on 26 January, and 01:30–05:00 and 16:30–17:50 on 27 January. These three intervals correspond to the duration of the three sub-Plinian eruptions that were recorded by other means, including seismograms, infrasonic monitoring, and eyewitness observations (e.g., Earthquake Research Institute, University of Tokyo, 2011). The duration of these three strain variations, all of which were longer than 1 hour, justifies the classification of this event as a sub-Plinian eruption. A significant and gradual variation in strain was also recorded between 28 and 31 January, associated with magma effusion within the summit crater. It is reasonable to consider that these strain variations were generated by decreases in volume of pressurized magma that had been stored underground before its effusion to the surface.

The location of the magma chamber associated with the eruptions between 26 January and 1 February and the associated volume changes have already been estimated from the analysis of GPS data. By assuming the deformation was generated by an isotropic point source, the Geospa-

tial Information Authority of Japan (GSI, 2011) estimated that the source was located at 31.945°N, 130.827°E, with a depth of 6.2 km, and that the total change in volume was $1.0 \times 10^7 \text{ m}^3$. The estimated horizontal location of this point source is 11.6 km from the ISA observatory towards S55.75°E, and 6.9 km away from the Shinmoe-dake crater towards N54.58°W (Fig. 1).

We have attempted to estimate the parameters of the source of these major events using extensometer-derived data, including the determination of separate source parameters for each event (i.e., the three sub-Plinian eruptions and the magma effusion event). The extensometer records on their own do not allow us to determine unique deformation source locations or volume changes in stored magma. However, we can estimate source depths and volume changes by assuming an isotropic point source and a given horizontal distance from the ISA observatory to the ground deformation epicenter.

We estimated source parameters using the following procedure. Strain changes are defined as differences between the averages of observations made during the 10 minutes immediately prior to the beginning of each event and immediately following each event. The determined strain changes associated with both sub-Plinian eruptions and the magma effusion event are listed in Table 1. The strain

Table 1. Observed changes in strain (unit: 10^{-9}) during sub-Plinian eruptions (SP1–3) and estimated isotropic point source parameters, together with estimation errors due to possible uncertainties in the observed values^{*1}.

Event (duration)	Observed strain change			Estimated source parameters and errors		
	E1 ($\times 10^{-9}$)	E2 ($\times 10^{-9}$)	E3 ($\times 10^{-9}$)	Azimuth ^{*2} (deg)	Depth ^{*3} (km)	Volume change ($\times 10^6$ m ³)
SP1 (15:30–18:50, Jan 26)	111 \pm 5	−68 \pm 5	25 \pm 5	+2.9 \pm 2.4	4.2 \pm 1.3	0.89 \pm 0.07
SP2 (01:50–05:00, Jan 27)	135 \pm 5	−84 \pm 5	30 \pm 5	+2.7 \pm 1.9	4.4 \pm 1.0	1.10 \pm 0.07
SP3 (16:30–17:50, Jan 27)	71 \pm 5	−44 \pm 5	16 \pm 5	+2.7 \pm 3.7	3.9 \pm 2.2	0.57 \pm 0.07
Magma effusion (Jan 28–30)	333 \pm 20	−239 \pm 20	39 \pm 20	+2.7 \pm 3.0	5.7 \pm 1.2	3.07 \pm 0.26

^{*1}Errors in observed values during magma effusion are assumed to be larger than those for SP1–3, as the duration of the effusive event was considerably longer than the duration of the sub-Plinian eruptions; this leads to changes in non-volcanic strain.

^{*2}Azimuth values are measured anticlockwise from the E1 direction.

^{*3}Depth and volume change values are estimated by assuming the horizontal distance to the source is 11.6 km, as inferred from GPS data analysis (GSI, 2011).

changes calculated using this approach may involve uncertainties associated with non-volcanic crustal deformation during meteorological disturbances, and the presence of noise within the observation system. Short events have small errors, whereas longer events have larger errors; in addition, the E1 and E3 components have low error values, whereas the E2 component has higher inherent errors. We assume an explicit error value for each component and for each event, as given in Table 1. One of the axes of principal horizontal strain is regarded as the azimuth from the ISA observatory towards the source. Using the estimated azimuth and the assumed horizontal distance from the ISA observatory to the ground deformation epicenter, it is possible to estimate the dip angle (i.e., the angle between a horizontal plane and a direct line from the ISA site toward the source) and the volume change using the Mogi model formula of Yamakawa (1955).

The estimated source parameters are listed in Table 1, together with possible errors. The source depth for the magma effusion stage is estimated to have been slightly deeper than the source for the sub-Plinian eruptions, although these estimates are within error. These differences are likely to relate to a contribution from the volcanic conduit, where explosive (sub-Plinian) eruptions could have involved a shallow part of the magma chamber plus the conduit, yielding a shallower source depth. Note that the total volume change during the magma effusion event is larger than the sum of the volume changes during the three sub-Plinian eruptions.

These extensometer-based source parameter estimates are somewhat different from GPS-based estimates. For example, the azimuth from the site to the source is estimated to be 18° by GPS, whereas the extensometer-based estimate gives an azimuth of 2°–3°. The discrepancy in azimuth from ISA is 15°–16° as illustrated in Fig. 4. In addition, the GPS-based estimate of the source depth is about 6.2 km (e.g., GSI, 2011), whereas all extensometer-derived source depth estimates are <5.7 km (Table 1). Furthermore, the entire GPS-based volume change estimate is larger than the total of the extensometer-based volume changes for all four major events, with the GPS-based analysis yielding a volume change of 7.2×10^6 m³, whereas the extensometer-based estimate was $5.63 \pm 0.07 \times 10^6$ m³. Source parameters for the total amount of deflation during the three sub-Plinian eruptions and the magma effusion are also estimated by Ueda *et al.* (2013) and Nakao *et al.* (2013) by using geodetic

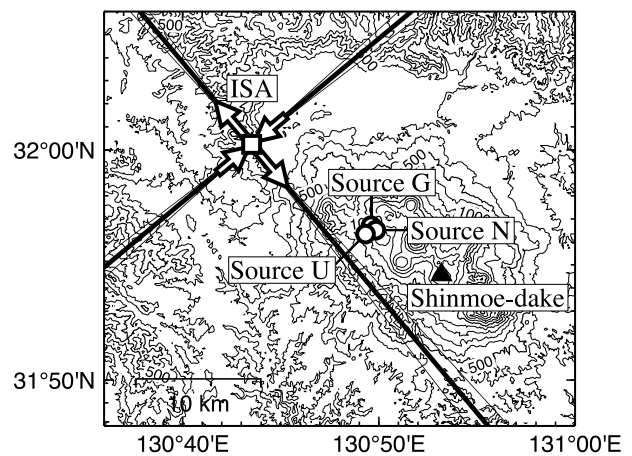


Fig. 4. Geometrical relationship between the principal strain axes (thick lines) at ISA determined for the first sub-Plinian eruption on 26 January, 2011, and the location of Shinmoe-dake crater. Arrows show the direction (i.e. compression or depression) in each direction. Thin lines show the range of the estimation error. Open circles with text labels (Source G, Source U, and Source N) indicate the horizontal locations of deflation point sources during the sub-Plinian and the magma effusion event estimated by GSI (2011), Ueda *et al.* (2013), and Nakao *et al.* (2013), respectively.

data. By their analysis, depths of the source are estimated to be 9.8 km and 8.35 km, and volume changes are estimated to be 13.2×10^6 m³ and 13.35×10^6 m³, respectively. Both of these values are larger than the extensometer-based estimate. The extensometer-based estimate highly depends on the assumed horizontal distance. If we assume the horizontal distance is 15 km, the depth and total volume changes estimated by extensometers are up to 7.4 km and 12.32×10^6 m³, respectively, which are smaller than those estimated by Nakao *et al.* (2013), and Ueda *et al.* (2013), but larger than that estimated by GSI (2011).

In general, estimating the location and size of deformation sources using data obtained from a single observatory may introduce significant errors, as the data obtained at this observatory may be distorted, for example by variations in local elastic properties around the site. An approach using model idealization that ignores possible contributions from a finite-length conduit may also introduce errors. As documented above, estimates based on strain data obtained

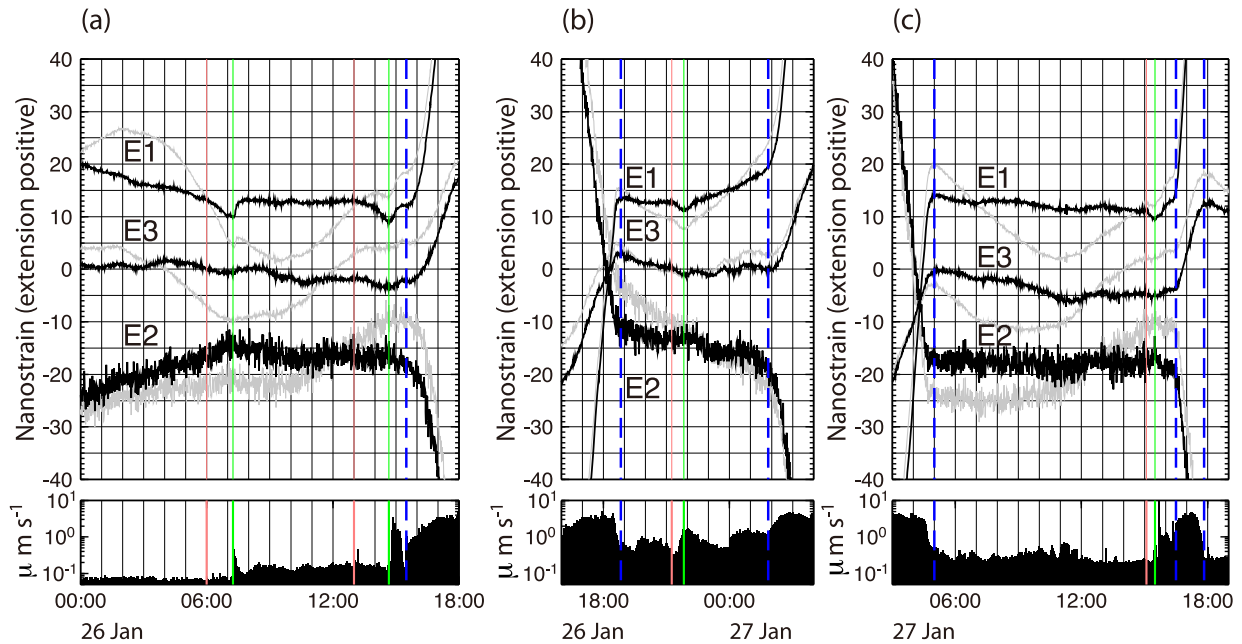


Fig. 5. Detailed views of strain time series prior to each sub-Plinian eruption. Time ranges in a–c correspond to the gray bars in Fig. 3 (i.e., 00:00–18:00 on 26 January, 16:00 on 26 January to 04:00 on 27 January, and 03:00–19:00 on 27 January, respectively). Black lines represent strain time-series after tidal components are removed, with gray lines representing the original time series. Shaded graphs at the bottom represent ground velocities at the Takachihogawara seismic station (Fig. 1). Vertical lines in red and green indicate onsets of inflation and deflation, respectively.

from the ISA observatory differ from estimates based on data from multiple stations. However, the differences are rather small.

The volumes of lava and tephra produced between 26 and 31 January, 2011, were also estimated by other means. Field measurements suggest that 24×10^6 kg of tephra was produced during the three sub-Plinian eruptions (National Institute of Advanced Industrial Science and Technology (AIST) and Asia Air Survey Co., Ltd., 2011), and assuming a density of 2500 kg/m^3 yields a dense rock equivalent volume of $9.6 \times 10^6 \text{ m}^3$. Additional estimates used a photograph taken on 31 January, 2011, which suggests the volume of lava accumulated in the Shinmoe-dake summit crater was $14 \times 10^6 \text{ m}^3$ (Earthquake Research Institute *et al.*, 2011). The magma extruded as lava is approximately 1.4 times larger than that ejected as tephra. The volume change estimated from extensometer records is $2.56 \times 10^6 \text{ m}^3$ and $3.07 \times 10^6 \text{ m}^3$, respectively, for the three sub-Plinian eruptions and magma effusion (Table 1) and the ratio of magma effusion to sub-Plinian eruptions is 1.2. Both field and photograph-based measurements are larger than the extensometer-based volume estimates presented here, but the ratio approximately coincides with each other. This indicates that the strain data obtained at the ISA observatory can detect more detail volcanic process and may provide approximate but reasonable depth and volume change estimates for other volcanic events.

4. Subtle Changes in Strain Prior to the Sub-Plinian Eruptions

In addition to the major strain changes that occurred simultaneously with the major eruptive events, subtle strain changes can be detected before each sub-Plinian eruption by visual inspection of the extensometer data. Figure 5 gives

a detailed view of the strain time-series data for the periods covering several hours before each sub-Plinian eruption. Before the start of the first sub-Plinian eruption at around 15:30 on 26 January, 2012, pairs of gradual decreases and rapid increases in the E1 component of strain (i.e., contraction and subsequent extension) with amplitudes of $\sim 3 \times 10^{-9}$ were recorded at approximately 6:00–7:40 and 13:00–15:10 on 26 January (Fig. 5(a)). Subtle strain variations were also seen at 21:15–22:20 on 26 January and 15:05–16:00 on 27 January, prior to the second and third sub-Plinian eruptions (Fig. 5(b and c)), and the amplitudes of these precursory strain changes were approximately 2×10^{-9} , somewhat smaller than those associated with the first eruption. The magnitudes of these subtle deformations (i.e., $\sim 1 \times 10^{-9}$) are two orders of magnitude smaller than the strain changes observed during each sub-Plinian eruption (i.e., $\sim 100 \times 10^{-9}$).

The subtle inflation followed by rapid deflation recorded during each event seems to be associated with a causal process associated with each sub-Plinian eruption. However, it is unclear whether this hypothesis is plausible, as similar-sized strain variations that are not associated with volcanic processes may have also been measured. Further research is needed to determine whether similar strain changes are only recorded before the three sub-Plinian eruptions that form the focus of this study. We investigated this possibility by analyzing the rate of variation in the E1 component strain. To obtain the strain rate values, the derivative of the smoothed time series trend was calculated. The smoothed time series trend was obtained following Tamura *et al.* (1991), with ABIC used to determine the optimum parameter that controls the smoothness of the trend. Because of the smoothing process, phenomena with time scales less than 30 minutes are ignored; however, it does not affect the

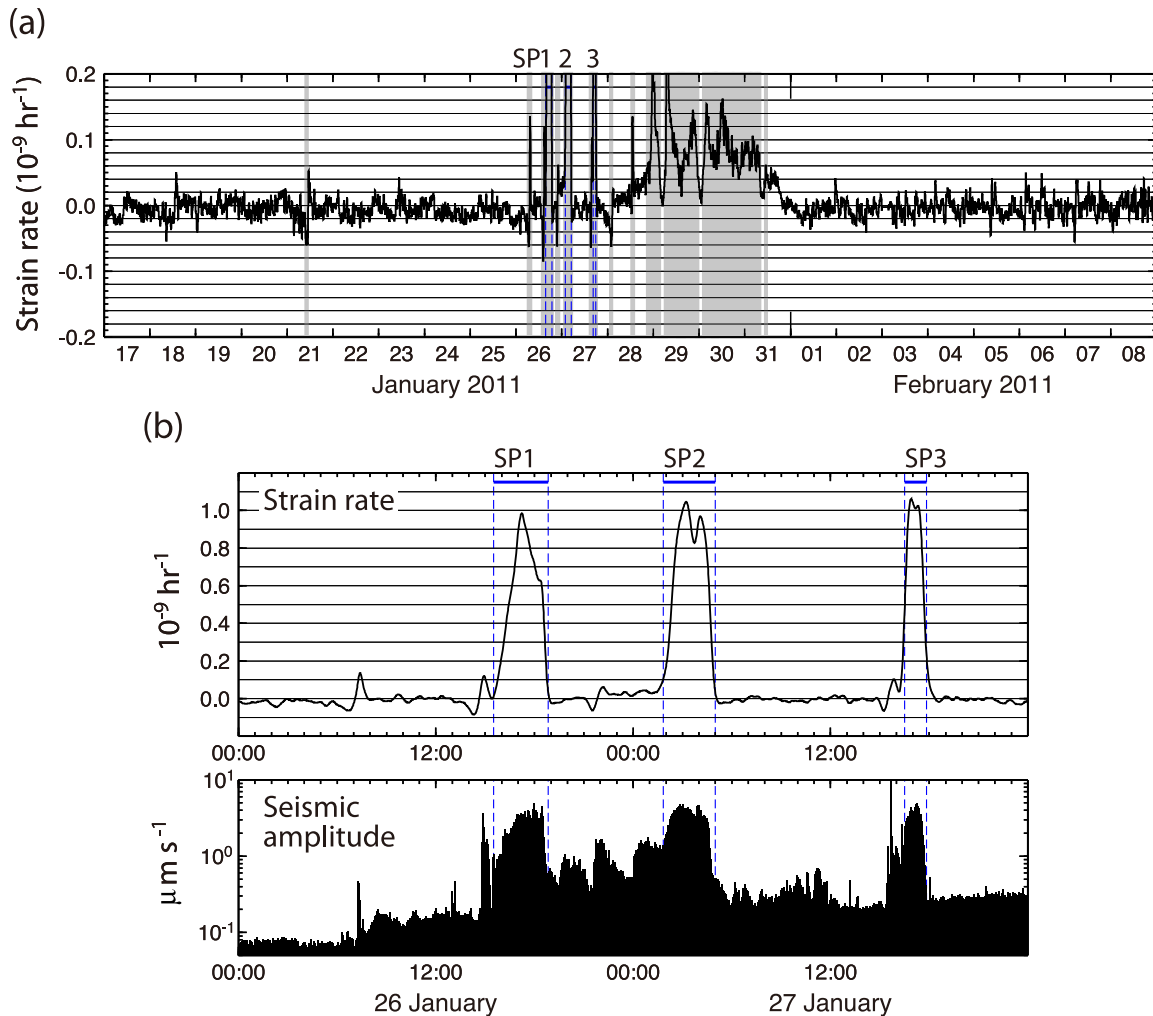


Fig. 6. (a) E1 component strain rates between 17 January and 8 February, 2011; SP1, 2, and 3 denote the first, second, and third sub-Plinian eruptions, respectively, that form the focus of this study, and the shaded gray area indicates periods with strain rates of $>0.6 \times 10^{-9}$. (b) E1 component strain rates between 26 and 27 January, 2011, with the lower panel showing simultaneous ground velocity changes at the Takachihogawara seismic station (Fig. 1).

following discussion.

Figure 6(a) shows strain rates together with periods with strain rates greater than the rates associated with the subtle changes that precede sub-Plinian eruptions (i.e., $0.6 \times 10^{-9} \text{ h}^{-1}$). The figure shows only one example of a sizable change in strain rate in the E1 direction that was not associated with sub-Plinian eruptions or subsequent magma effusion. This change was recorded on 21 January, 2011, and was followed by a minor eruption event on 22 January, 2011. This observation indicates that subtle changes in strain are commonly followed by sub-Plinian eruptions, although the relationship between eruptions and preceding deformation is not exactly one-to-one. In other words, these strain changes are a kind of precursory phenomenon associated with sub-Plinian eruptions. Similar precursory ground deformation has already been identified for Vulcanian eruptions at Sakurajima (Ishihara, 1990) and Montserrat (Voight *et al.*, 1998, 1999), and the data presented here suggest that these precursory phenomena are also present before other types of eruption.

Contraction and subsequent extension in the E1 direction are probably associated with inflation and subsequent

deflation of the point source. However, the amplitudes of the subtle precursor changes are small and have low signal/noise ratios, meaning that accurately determining the parameters of the source of these changes is impossible, unlike the changes associated with the sub-Plinian eruptions and the magma effusion event. Nevertheless, we can obtain a possible range of source locations for the first subtle strain change using the following procedure. This approach is similar to that discussed in Section 3, in that we assume that the deformation was generated by an isotropic point source that was located approximately in the same direction as the orientation of the E1 vault within the ISA observatory, meaning that the E1 and E2 components are approximate radial and transverse strain components, respectively. The first subtle strain change was associated with an E1 component strain change of -4×10^{-9} , with an E2 component change of up to $+2 \times 10^{-9}$. The significant noise and fluctuations within the E2 component signal mean that this value is not very precise. However, it is apparent by visual inspection that even if we assume that the possible error in the E1 component is $+0.5 \times 10^{-9}$, the E2/E1 ratio is unlikely to be less than -0.7 . This value of -0.7

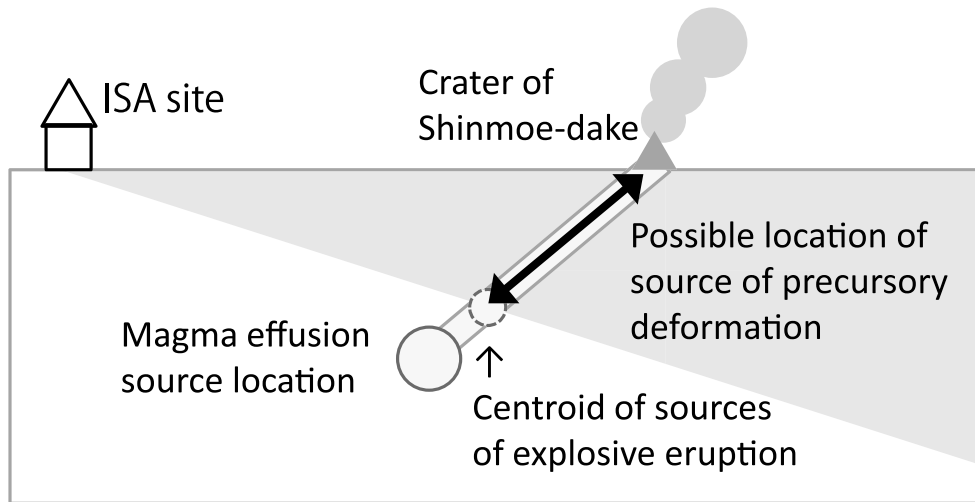


Fig. 7. Schematic geometry of the ISA observatory, showing the relative locations of Shinmoe-dake volcano, the eruption-related magma chamber, the centroid for the explosive eruptions, and possible source locations associated with the precursory deformation. The shaded area indicates potential source areas for these subtle strain changes.

is comparable to the $E2/E1$ ratios obtained for the major events, indicating that the dip angle to an isotropic point source should be smaller than the dip angle for the precursory subtle strain change should be smaller than that for the major sub-Plinian events (Fig. 7).

The above discussion further indicates that if the horizontal distance from the ISA site to the source epicenter was the same for both the precursory deformation and the sub-Plinian eruptions, the source depth of the precursory deformation would have been shallower than the source depth of the magma chamber, at least for the first subtle strain event that was recorded at around 6:00–7:40 on 26 January, 2011. Even if this horizontal distance to the source is not fixed, the source depth is still likely to be shallow unless the horizontal distance is very large (Fig. 7).

Other geophysical acquisition techniques (e.g., Kato and Fujiwara, 2012; Maehara *et al.*, 2012), including eyewitness reports, provided several other records of phenomena prior to the sub-Plinian eruptions. In the case of the first sub-Plinian eruption, for example, an increase in seismic amplitudes was observed at about 7:15 (Fig. 5(a)), coincident with the onset of a rapid extension recorded in the $E1$ direction (Fig. 5(a)). A minor ash eruption with increased amounts of volcanic smoke was observed at this same time, and was followed by a further increase in the amount of volcanic smoke venting at around 7:50. At about 14:50, seismic amplitudes increased again (Fig. 5(a)), which corresponds to the subtle deformation just before the first sub-Plinian eruption. At this time, steam emissions were also observed (Maehara *et al.*, 2012). Increases in seismic amplitudes were again observed in association with the subtle deformations before the second and third sub-Plinian eruptions, although the exact timings of the onset of these two sets of phenomena are not exactly the same (Fig. 5(b and c)).

5. Discussion

The precursory deformation associated with each of the sub-Plinian eruptions documented in this study can be in-

terpreted as follows: a gradual $E1$ component contraction corresponds to the accumulation of volcanic gases at depth, and a rapid extension of the $E1$ component corresponds to decreasing pressure during the release of volcanic gases within the crater. The shallow source depth estimates for these precursory deformation events is consistent with this interpretation. If this interpretation is correct, temporal changes in strain will be important factors in any further investigation of these processes.

Similarities between the subtle strain changes (indicated by variations in strain rates from negative to positive) prior to each of the sub-Plinian eruptions are also evident in the strain rate graph shown in Fig. 6(b). The shapes of subtle strain changes for each of the sub-Plinian eruptions are similar, suggesting that the precursory phenomena corresponding to each sub-Plinian eruption involve similar processes.

Figure 6(b) also shows, however, that the relationships between subtle changes in strain and the eruptions are not simple. For example, the first eruption on 26 January was associated with two subtle changes in strain: one approximately 8 hours before the eruption and a second at 15:00–15:30, immediately prior to the eruption. The second eruption occurred around 3 hours after the subtle strain change at 21:20–22:20 on 26 January. The last sub-Plinian eruption was almost simultaneous with the ending of this period of subtle strain change. In summary, the time interval between the beginning of the subtle strain change and each sub-Plinian eruption decreased over time. It may also be noted that variations are also apparent in the speeds of deflation during sub-Plinian eruptions

The variations in the timing relationships between subtle strain changes, increases in seismic amplitudes, and the onset of sub-Plinian eruptions, together with the increasing rate of deflation during each eruption may be related to changes either in the magma properties or in the magma supply system (e.g., magma viscosity, expansion of a magma conduit as a result of repeated eruptions, or gradual magma ascent). Additional discussion requires at least a quantitative estimation of the location and magnitude of

subtle strain changes.

Further investigation requires other geophysical datasets. Because the direct measurement of strain of the order of 10^{-9} was performed at only one site, some other approach is required to investigate the precursory deformation more fully. The use of broadband seismograms may be a promising way to deduce tilt changes at particular points (e.g., Aoyama and Oshima, 2008). In fact, tilt changes prior to the sub-Plinian eruptions of Shinmoe-dake were indicated by data from a broadband seismogram positioned about 1 km from the crater of Shinmoe-dake (Maehara *et al.*, 2012). Combining such a result with direct measurements of strain would make it possible to estimate the sizes and locations of the sources of precursory crustal deformation more accurately, which, in turn, would improve our understanding of the processes involved in the sub-Plinian eruptions.

6. Conclusions

Subtle (order 10^{-9}) strain changes were recorded prior to sub-Plinian eruptions during the activities of Shinmoe-dake in January 2011 by using vault-housed extensometers installed approximately 18 km away from the summit crater of the volcano. Each subtle strain change can be accounted for by an inflation followed by a deflation at depth. The depth of the source is estimated to be shallower than the magma chamber that produced most of the effusive material during the eruptions of Shinmoe-dake. This may indicate that the movement of magma or volcanic gas from the main magma chamber towards the ground surface occurred not only during the sub-Plinian eruptions but also before these eruptions. The observed subtle changes in strain provide significant constraints on the possible mechanisms of the sub-Plinian eruptions of Shinmoe-dake, although further studies using other geophysical datasets are required if we are to investigate the processes more fully.

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Appendix A.

Here, we consider the procedure of evaluating minimum sizes of subsurface volumetric changes that can be resolved by GPS and by extensometers.

First, the detection limit of GPS is considered. Only horizontal displacements are considered here because the vertical component of GPS data is generally less accurate. In the case of a point source model (i.e., a Mogi model), the horizontal displacement in a radial direction from the source, denoted by u_r , is expressed as

$$u_r(r) = \frac{\lambda + 2\mu}{2\pi(\lambda + \mu)} \Delta V \frac{r}{(r^2 + f^2)^{3/2}}, \quad (\text{A.1})$$

where λ and μ are Lamé constants, r is the horizontal distance, and f is the source depth. Assume u_{\min} is the minimum displacement that GPS can resolve. A volume

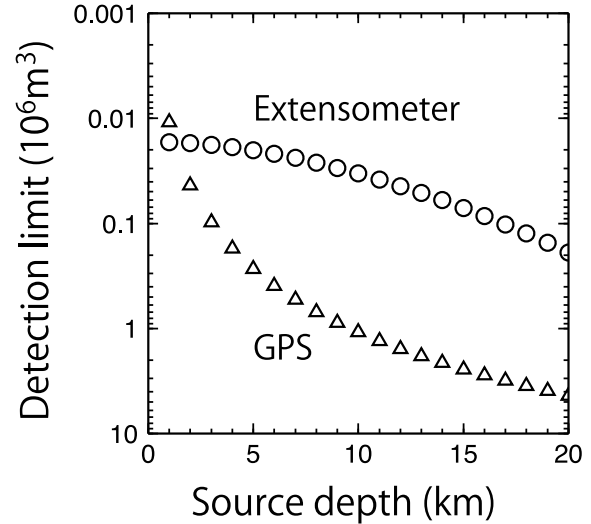


Fig. A.1. Detection limits of subsurface volume changes by using extensometers at 20 km away from the epicenter (circles), and by using GPS installed at an optimum point (triangles). The extensometer is assumed to be set in the radial direction from the source. GPS measures the horizontal displacement. Resolutions of extensometers and GPS are assumed to be 1.0×10^{-9} (dimensionless) and 1.0 mm, respectively.

change ΔV can be detected by GPS if (A.1) is larger than u_{\min} . This condition is expressed by

$$\Delta V \geq \frac{2\pi(\lambda + \mu)}{\lambda + 2\mu} \frac{(r^2 + f^2)^{3/2}}{r} u_{\min}. \quad (\text{A.2})$$

The right-hand side of (A.2) is minimized when $r = f/2^{1/2}$. Provided that GPS stations are installed with a sufficient spatial density, we can choose r so that the right-hand side of (A.2) is minimized. Therefore, in the case of $\lambda = \mu$, we derive the following condition

$$V \geq 2\sqrt{3}\pi f^2 u_{\min}. \quad (\text{A.3})$$

This provides the minimum size of the subsurface volume change (ΔV) that can be monitored by the GPS array.

Next, the detection limit of extensometers is considered. Let us consider the extension in a radial direction from the source, denoted by E_r . It is expressed as

$$E_r = \frac{\partial}{\partial r} u_r(r) = \frac{\lambda + 2\mu}{2\pi(\lambda + \mu)} \Delta V \frac{-2r^2 + f^2}{(r^2 + f^2)^{5/2}}. \quad (\text{A.4})$$

Assume E_{\min} is the minimum displacement that GPS can detect. Similar to GPS, a volume change ΔV can be detected by extensometers if (A.1) is larger than E_{\min} . This condition is expressed by

$$\Delta V \geq \frac{2\pi(\lambda + \mu)}{\lambda + 2\mu} \frac{(r^2 + f^2)^{5/2}}{-2r^2 + f^2} E_{\min}. \quad (\text{A.5})$$

In contrast to the case of GPS, the data from the extensometers are not expected to be available at arbitrary points. Therefore, a fixed value of r should be used to evaluate the minimum size of the detectable volume change by using (A.4).

An example of an evaluation using (A.3) and (A.5) is shown in Fig. A.1.

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