Compact representations of positional knowledge in short and long words for letters and features

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Single-letter statistical measures providing values for each letter-position and word-length combination are too unwieldy for use in working letter-recognition models; more compact tables are needed. Compact tables collapsing word length to short or long words and letter positions to first, last, or middle letters are presented for the frequency and versatility of single letters. Letter-position and word-size differences are preserved in this reduced format. To test awareness of these values, subjects rate the commonness of letters in each letter position. Their responses indicate high intersubject agreement and correlate highly with the frequency and versatility measures. A LISP program that translates the letter knowledge for each letter into a corresponding knowledge for each feature in a feature set is described. Distinctiveness values for each feature (see Shimron & Navon, 1981) are computed.

Single-letter statistical measures such as frequency and versatility have been tabulated for various wordlength and letter-position combinations (e.g., Mayzner & Tresselt, 1965; Solso, 1979; Solso & King, 1976). These tables provide a powerful source of knowledge but may be too unwieldy, or too detailed, for working models of letter recognition. Although it is not difficult to store large tables with a machine, it does seem incredible that humans would retain information in such detail. Rawlinson (1976) expressed a similar reservation regarding bigram frequency tables and provided a new, more compact table of bigram frequency with only three letter-pair positions: first, last, and other, Here, the same distinction is applied to single-letter statistics. Wordlength divisions are limited to short (three-five letters) and long (six-eight letters) words. Source values before collapsing were taken from Solso (1979) and Solso and King (1976) for four- to eight-letter words. Threeletter word values were compiled from the Kučera and Francis (1967) word-frequency count. Two statistical measures were compiled in this collapsed format: the frequency and the versatility of letters. Whereas frequency is the number of times a letter appears in a given position, versatility is the number of times it appears in that position in different words.

Conspicuously absent from most papers tabulating letter-frequency information is some indication of how

well the measures reflect people's actual knowledge. Although the primary purpose was the production of more compact, yet still precise, tables of positional letter information, people's knowledge is still of interest. A demonstration of knowledge of statistics would not indicate when, how, or even if, people use the knowledge to aid letter recognition, but it would show that the knowledge is available for use. The absence of demonstrated knowledge may indicate only covert awareness, not ignorance. Still, the presence of subjects' knowledge of the statistical properties of letters would be reassuring to most letter-recognition theorists. Consequently, the subjects here were asked to rate the commonness of letters for the three letter positions in both short and long words.

METHOD

The basic tables in this paper list the frequency and versatility measures for short and long words in the first, middle, and last letter positions. The middle-position value is an average for the middle positions in a word. For example, the middle frequency value in a five-letter word is the average of the second, third, and fourth positions. The average is taken so that longer words do not have artificially larger middle values. Similarly, the values for short and long words are averages for their constituent sizes: three-, four-, and five-letter words for short words and six-, seven-, and eight-letter words for long words.

The source values for frequency and versatility for four- to eight-letter words were taken from the tables provided by Solso (1979) and Solso and King (1976). The three-letter-word values were compiled from the Kučera and Francis (1967) count, since that was the source for the Solso and King tables. Words and abbreviations not listed in *Webster's New Collegiate Dictionary* (1976) were not used in the frequency and versatility calculations. Once the middle positions had been averaged, the values for each position (i.e., first, middle, and last) were averaged for each set of three word sizes to obtain a value for each letter position in both short and long words.

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Frequency							
		Short			Long		
	First	Middle	Last	First	Middle	Last	
Α	16796	20646	755	5431	5940	68 0	
В	6315	501	253	4285	747	27	
С	4643	2373	265	6708	2592	834	
D	3188	1278	19941	3344	1542	11045	
E	2258	15803	45948	3339	10828	10092	
F	9161	761	578	3403	725	516	
G	3001	1089	1892	1763	1534	5623	
Н	10817	32842	6534	2462	2043	1823	
I	1713	12332	93	1942	6749	125	
J	1093	36	0	496	68	2	
K	1092	857	2697	386	590	245	
L	4670	5889	5260	2501	4100	3349	
М	6375	1793	3143	4032	1732	1048	
N	4143	15548	8732	1651	5357	5517	
0	5457	17424	2967	1552	5803	295	
Р	3188	740	1026	6371	1510	126	
Q	197	14	1	287	97	0	
R	2420	8076	11136	4205	5914	5804	
S	9736	3363	16400	9195	2901	11995	
Т	39403	4697	17506	3572	5036	5718	
U	1349	6647	1134	773	3247	49	
v	826	2013	4	1032	927	14	
W	16429	1387	2659	2410	551	330	
Х	4	156	317	0	234	88	
Y	2493	459	7507	140	444	6053	
Z	43	87	59	18	9 7	23	

Table 1

Table 2 Versatility

	Short			Long		
	First	Middle	Last	First	Middle	Last
Α	127	310	96	353	577	161
В	178	29	24	436	88	8
С	163	56	21	555	187	75
D	122	53	145	335	160	878
Е	63	283	333	225	857	690
F	121	17	20	285	67	17
G	99	41	47	242	121	491
Н	112	51	77	242	144	107
I	35	221	35	147	590	51
J	46	2	0	67	6	0
K	50	31	79	72	81	64
L	125	149	103	222	394	225
М	128	50	51	323	152	181
N	54	129	160	119	462	464
0	52	254	68	130	455	85
P	139	41	56	448	133	23
Q	9	1	1	25	10	0
R	107	170	116	352	489	413
S	250	74	431	752	253	1307
Т	139	91	179	318	365	371
U	21	141	13	91	270	14
v	41	29	3	108	72	7
W	85	29	24	193	54	29
Х	2	8	17	0	18	16
Y	20	25	186	22	48	478
Z	9	10	11	11	23	11

These tables are more compact, but less precise, representations of the same information resident in the Solso and King (1976) tables. They are more compact because there are fewer letter-position and word-length combinations, and they are less precise because of the averaging. The term "same information" is used because averaging for the middle position took place at the level of individual word size before the data were collapsed to short- or long-word categories. The word-size categories are, then, somewhat deceptive. First, the sizes included in each category resulted from an arbitrary decision. Second, a true twocategory distinction would not average before collapsing to obtain the category values. Therefore, although there are fewer letter-position and word-length combinations, the more detailed information from the larger number of combinations is retained, but in an admittedly less precise form.

Eight volunteers ranked the letters of the alphabet in descending order of commonness for each letter-position and wordlength combination as found in the tables described above.

RESULTS

The basic tables for the statistical measures in reduced letter-position and word-length form are presented in Tables 1 and 2. The average correlation over positions between frequency and versatility is .914. The near identity is present for individual letters in long words but not for those in short words. Anomalies exist between frequency and versatility for individual letters in short words. The mismatches do not involve the same letters over all letter positions. For example, the first position shows mismatches for B and C, but the middle and and last positions show identity between frequency and versatility for the two letters. The identity of the most frequent and versatile letters also differs over letter positions for both short and long words. For example, the most frequent letters for short words are T. H. and E. for the first, the middle, and the last positions, respectively. Similar differences exist for the versatility of letters in words. Figure 1 shows the similarities and differences between the two statistics; letters have been graphed according to their standing within the alphabet in standard deviation units for the frequency and versatility measures.

The frequency-versatility mismatches in short words involve mainly letters that are highly versatile but not very frequent (e.g., B, C, D, L, M, P, and S in the first letter position). Some mismatches involving a very frequent but not very versatile letter (i.e., the reverse relationship) can be removed by discounting the effects of only a few words. For example, discounting the word "THE" greatly narrows the gap between frequency and versatility for T, H, and E, since the word's frequency count is by far the highest in the corpus (see Kučera & Francis, 1967), at 69,000 occurrences. Other frequent words, or frequent prefixes and suffixes, could have the same effect on their constituent letters. Drewnowski and Healy (e.g., Drewnowski, 1978, 1981; Drewnowski & Healy, 1977, 1980; Healy, 1976, 1980; Healy & Drewnowski, 1983) have shown that high-frequency short words and suffixes are treated differently from the way words or letter groups are treated.



Figure 1. Z-scores of frequency and versatility for short words (top three panels) and long words (bottom three panels.

The average intercorrelations of the eight subjects are shown in Table 3. The level of agreement between subjects is high, but long words tend to produce weaker correlations, as do the first positions for both word lengths. Each subject's responses were correlated with the two statistical measures. The averages over subjects are presented in Table 3. In long words, there is no difference between frequency and versatility, but in short words, a difference does exist for the first and middle positions.

In summary, long words show no mismatches between frequency and versatility, although the particular identity of high-scoring letters does vary over letter positions. Short words show a similar variation in letter identity over letter positions but also a high number of frequency-versatility mismatches. These results are compatible with a short- and long-word distinction and show that the reduction of letter-position categories to first, middle, and last letter positions has preserved positional

	Tabl Average Co	e 3 orrelations		
	·	First	Middle	Last
	•	Between Su	bjects	
	Short	0.72	0.80	0.81
	Long	0.67	0.77	0.78
	Betwee	n Subjects	and Measure:	8
Short Words	Frequency	0.66	0.75	0.83
	Versatility	0.77	0.86	0.81
Long Words	Frequency	0.74	0.85	0.86
	Versatility	0.72	0.83	0. 79

variability. The subjects show a high degree of agreement with each other, with the level of agreement at the first letter position being slightly lower. Again, short words show a difference between the frequency and versatility measures.

DISCUSSION

More compact tables of positional letter knowledge are now available for use in working letter-recognition models. The word-length distinction is useful, especially in consideration of frequency-versatility mismatches. In short words, both the frequency and versatility of letters should be considered. The subjects' responses support this conclusion.

Some recent papers investigating the source of familiarity effect in letter recognition (e.g., Appelman & Mayzner, 1981; Wandmacher, Shapiro, & Mohr, 1981) have concluded that letter familiarity is not utilized in the identification, per se, of at least single letters or in feature extraction. These studies fail to show that letter familiarity is not used in identification when some confusion might exist, as in a multielement display, or in the localization of letters in a display. Butler (1980a, 1980b, 1981) suggested that identification and localization are independent processes but that recognition depends on both (see also Bridgeman, Lewis, Heit, & Nagle, 1979; Kent, 1981; Krumhansl & Thomas, 1976; Milner, 1974). These tables are useful, then, even in the face of such recent findings.

Shimron and Navon's (1981) study of feature information within letters indicates that all features are not equally informative. Specifically, distinctiveness and uniqueness of features is important for letter recognition. The frequency and versatility of features may also be important and may contribute to the unevenness. Using Tables 1 and 2, or tables of another letter statistic in the same format, a simple computer program could produce corresponding feature information for any feature set desired and thus supply useful knowledge bases for feature extraction.

A COMPUTER PROGRAM TO TRANSLATE THE LETTER DATA BASE TO A FEATURE DATA BASE

A LISP program has been developed to translate the frequency and versatility values of letters from Tables 1 and 2 into similar values for features. Suppose we had an alphabet of four letters (e.g., A, B, C, and D) and a feature set of four features that describe the letters (e.g., f_1, f_2, f_3 , and f_4). Table 4 shows the feature definition for each of our hypothetical letters and also shows a set of letter values for a hypothetical statistic. In Table 4, the letter A has the features f_1 and f_2 , B has f_1 and f_3 , and so forth for C and D. Table 4 also has values for first, middle, and last character positions of 2, 4, and 6 for short words and 3, 4, and 5 for long words (similarly for B, C, and D). In addition, Table 4 lists the values calculated by the computer program, which translates the hypothetical values for the letter statistic into corresponding values for features. The program simply sums the letter values for each letter that contains the feature being calculated. For example, f₁ belongs to A, B, and C. The values for f_1 are the sums for the A, B, and C values. If the frequency values from Table 1 had been used, the values for f, would have been 27,754, 23,520, 1,273, 16,424, 9,279, and 1,541.

		Hy	pothetical Examp	le		
		Short			Long	
	First	Middle	Last	First	Middle	Last
			Positional Value	es for the Letters		
Α	2	4	6	3	4	5
В	3	4	5	3	4	5
С	4	4	4	6	4	8
D	8	2	6	4	2	4
			Positional Value	s for the Features		
f,	9	12	15	12	12	18
f_2	10	6	12	7	6	9
$\tilde{f_3}$	11	6	11	7	6	9
f	4	4	4	6	4	8

Table 4

Note-Feature definitions: $A = f_1 f_2$; $B = f_1 f_3$; $C = f_1 f_4$; $D = f_2 f_3$. Overall distinctiveness values: $f_1 = 0.267$; $f_2 = 0.600$; $f_3 = 0.660$; $f_4 = 0.800$.

The user can select one of four feature sets supplied with the program (e.g., Briggs & Hovecar, 1975; Geyer & Dewald, 1973; Keren & Baggen, 1981; Lindsay & Norman, 1972), and either the frequency or the versatility statistic can be chosen. User-defined feature sets and statistics can be employed, but the user must produce the files in the same format as that of the default files supplied. The user can build his own alphabet as well. Positional values for the statistic selected are computed for each feature in the feature set. A nonpositional statistic is calculated by averaging the positional values, and a total is computed over word-length distinctions, one for each character position.

In addition to calculating the positional and nonpositional statistics for each feature, the program accomplishes two other goals. First, it calculates distinctiveness values (Shimron & Navon, 1981) for each feature. Second, all values calculated by the program are placed under appropriate indicators, or name tags, on property lists in the LISP environment.

The distinctiveness (Shimron & Navon, 1981) of a feature of two letters is the degree of feature overlap between two letters after the feature has been removed. The distinctiveness is, then, the overlap of the fragments. The range is from zero, or minimal distinctive value, to one, or maximal distinctive value. The program calculates the overall average distinctiveness value for each feature. For a particular feature, say f_1 in Table 4, the distinctiveness values would be calculated for every letter that contained f_1 compared with all other letters in the alphabet. For our hypothetical alphabet values would be calculated for: A compared with B, C, and D; B compared with A, C, and D; and C compared with A, B, and D. Values would not be calculated for D, since it does not contain f_1 . The average of all these values is placed on the property list. Although the individual values for each letter comparison, and the average for each feature for each letter that it belongs to, are not retained in the LISP environment, they are available through the TRACE function in LISP as the values are being calculated. Table 4 shows the distinctiveness values calculated for the hypothetical statistic and alphabet.

For LISP modelers, the property-list feature is the real utility of the program. The presence of values on property lists leaves an enriched LISP environment ready for use by a working model of letter recognition. For LISPers, the names and descriptions of the propertylist indicators follow. The indicators for letters are: (1) features—a list of the letter's component features; (2) 1-knowledge—the average, or nonpositional, statistic; (3) short—a list of the three positional statistics for the letter in short words; (4) long—a list of the three positional statistics for the letter in long words; (5) all—a list of the three positional statistics totaled for short and long words. Each feature in the feature set has the indicators 1-knowledge, short, long, and all, which contain the information calculated from the letter values under Table 5 Sample Dialogue for a Program Run

```
.R LISP
(SYSIN 'SETUP.LSP')
(TRANSLATE NIL)
PROGRAM TRANSLATE
BY IAN MORRISON
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THE PROGRAM TRANSLATES A LETTER DATA-BASE INTO
```

A FEATURE DATA-BASE. MAKE APPROPRIATE SELECTIONS FROM THE FOLLOWING MENUS.

CHOOSE A LETTER DATA-BASE:

- 1. FREQUENCY
- 2. VERSATILITY
- 3. USER DEFINED STATISTIC
- 9. EXAMPLE STATISTIC
- 9

CHOOSE ONE OF THE FOLLOWING FEATURE SETS

1.	BRIGGS & HOVECAR	1975
2.	GEYER & DEWALD	1973
з.	LINDSAY & NORMAN	1972
4.	KEREN & BAGGEN	1981
5.	USER~DEFINED FEAT	FURE-SET
9.	EXAMPLE FEATURE-S	SET

-	
a	

SELECT DISTINCTIVENESS OPTION (NAVON & SHIMRON, 1981):

- 1. NOT NECESSARY
- 2. READ FROM FILE
- 3. CALCULATE
- 4. CALCULATE TRACING ROW-V
- 5. CALCULATE TRACING CELL-V
- 6. CALCULATE TRACING ROW-V AND CELL-V

3

SELECT PRINT OPTION:

- 1. CALCULATE ONLY
- 2. CALCULATE AND PRINT TO FILE
- 2

Table 5 ContinuedSample Dialogue For Program Run

```
USE DEFAULT ALPHABET <Y/N>? N
ENTER A LIST OF CHARACTERS:
--- (A B C D)
```

FILENAME FOR OUTPUT: 'TESTO.OUT'

Note-Intermediate results and file input echoed to the terminal in LISP has been omitted for clarity.

Table 6						
Program	Output	From	Example	in	Table 5	

```
FEATURE-BASED EXTRACTION KNOWLEDGE
NONPOSITIONAL VALUES:
(F1 13)
(F2 8)
(F3 8)
(F4 5)
POSITIONAL VALUES:
(F1 9 12 15 12 12 18)
(F2 10 6 12 7 6 9)
(F3 11 6 11 7 6 9)
(F4 4 4 4 6 4 8)
POSITIONAL VALUES FOR BOTH WORD-SIZES:
(F1 21 24 33)
(F2 17 12 21)
(F3 18 12 20)
(F4 10 8 12)
CONFUSION-SETS:
(F1 A B C)
(F2 A D)
(F3 B D)
(F4 C)
DISTINCTIVENESS VALUES:
(F1 0.2666667E-01)
(F2 0.600000E-01)
(F3 0.600000E-01)
(F4 0.800000E-01)
```

those indicators. Two additional indicators are supplied for each feature: (1) confusions—a list of the letters that contain the feature; (2) distinctiveness—the overall distinctiveness value.

Table 5 shows an example of the dialogue for a program run. The example feature set and statistic are the hypothetical ones used earlier. Since the distinctiveness values need considerable processing time for evaluation, they can either be omitted on a run or accessed from a file designated by the user (i.e., they need only be calculated once). The distinctiveness values, positional and nonpositional statistics, and confusion sets for each feature can be printed to a file named by the user. Letter values are retained in the LISP environment but are not printed. Table 6 shows the output for the hypothetical feature set and statistic produced by selecting the example options.

Availability

The program is implemented in RT-11 LISP on a PDP-11 computer (RT-11 LISP was written by Jeffrey Kodosky in 1977 and is available from the Decus Librarian for copy costs). A limitation of 5,000 words of free space demands a slow algorithm. For speedier use on a larger machine, the program can be translated into another dialect of LISP with a minimum of effort by a LISP programmer. The original version of the program was written in FRANZ LISP on a VAX 11/750. The author will supply a hardcopy listing on request and/or a copy to an 8-in. floppy diskette if supplied. Disks will be returned in double-density format from an RX02 drive.

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