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Characteristics of volumetric losses and efficiency of axial piston pump with respect to displacement conditions*

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Abstract: A good efficiency performance of a pump over a wide range of displacement conditions is crucially important for variable pump control systems to save energy. However, according to the literature, less attention has been paid to the understanding of the efficiency, leakage flow, and compression flow characteristics of the pump with respect to displacement conditions. In this study, a test bench was built, and a novel explicit volumetric loss model was proposed to investigate these problems. The overall efficiency is found to drop considerably with the decreasing displacement. The volumetric losses range from 13% to 47% of the total power losses of pump at the rated speed, under the conditions of pressure ranging from 5 to 35 MPa and displacement ranging from 13% to 100% of full displacement. The highest proportion of compression flow losses in the total volumetric losses of pump at the rated speed can reach up to 41% when the pressure and displacement are greater than 30 MPa and 88% of full displacement, respectively; after that, the proportion gradually decreases with decreasing displacement. However, the leakage flow generally increases with decreasing displacement, or may decrease first and begin to increase after the minimum with the further decrease of displacement. In the components of leakage of slipper/swash plate pair, the squeeze leakage is found to reach a magnitude equal to that of the Poiseuille leakage. The findings can guide the further research and design of pumps with better efficiency performance.

Key words: Axial piston pump, Efficiency, Leakage, Compression flow, Displacement condition http://dx.doi.org/10.1631/jzus.A1500197 **CLC number:** TH13

1 Introduction

Efficiency performance is a major sales argument of axial piston pumps today in a majority of industrial markets. Volumetric losses are one of the important factors responsible for efficiency decrease of a pump. Such losses can be generated in the lubricating gaps of pump, known as leakage flow losses, and in the pump displacement chamber, known as

compression flow losses. So far, a large number of studies related to the leakage flow in the lubricating gaps of pump have been carried out. The involved lubricating gaps in the pump include piston/cylinder interface, slipper/swash plate interface, valve plate/cylinder interface, and piston/slipper spherical bearings.

Traditionally, Poiseulle equation and Couette equation are used to evaluate the leakage via piston/cylinder interface (Ivantysyn and Ivantysynova, 2001; Ma *et al.*, 2010b; Guan *et al.*, 2014). A more precise way is via using the 2D Reynolds equation of lubrication (Xu *et al.*, 2013; Mizell and Ivantysynova, 2014; Wegner *et al.*, 2014; Lin and Hu, 2015). Pistons in some pumps often have several grooves cut along the axis in order to increase stability, decrease friction, and reduce lateral forces. Some attempts have been

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made to find the leakage flow theoretically taking into account the effect of grooves (Kumar and Bergada, 2013).

A detailed review and discussion on the study related to the leakage via slipper/swash plate interface since 1962 and cylinder/valve plate gap since 1974 was made by Bergada *et al.* (2012a). On the basis of the discussion of previous studies, they found that no study was performed on the slippers with nonvented grooves. Therefore, in their studies they carefully derived the equations to calculate the leakage via the slipper/swash plate interface, in which the slipper had non-vented grooves. They also derived the explicit equations to compute the leakage and pressure distribution between the cylinder and valve plate (Bergada *et al.*, 2012a; 2012b).

The leakage of piston/slipper spherical bearing is very small compared with other leakages of the pump. Therefore, most of the studies done on the piston/slipper spherical bearing are related to friction torque (Kazama, 2008). Recently, the equations for calculating the leakage through the piston/slipper spherical bearing were derived by Bergada *et al.* (2012a).

From the review of the previous studies, it can be found that studies on the leakage of each individual lubricating gap of the pump are specific. However, little attention has been paid to the variation characteristics of leakage flow of the pump versus the displacement conditions. With the fast development of the technology related to pump control system, variable displacement pumps are getting wider employment in various fields. Variable displacement pumps usually have to work under the displacement conditions varying within a large range, to improve the power matching between the pump and the load to save energy. Therefore, a deeper insight of the variation characteristics of various volumetric losses versus displacement conditions is indispensable. By reviewing the leakage equations derived in the previous studies, it can also be found that the previous equations to calculate the leakage via slipper/swash plate gap, which is the uppermost leakage source directly related to the displacement conditions, are merely linked with the differential pressure effect. However, there are other factors affecting the leakage, for instance, the micro squeezing motion of slipper, the spin motion of slipper, etc. Therefore, a deeper insight into the leakage mechanism of slipper/swash plate pair is necessary.

According to the literature, the compression flow characteristic of pump over wide operating ranges is not fully known as well. A comparison of the flow ripple of pump, which was simulated from a verified model with compressible and incompressible fluids, was made by Ma et al. (2010a). The comparison shows that the flow ripple is one order of magnitude larger when the simulation employed the compressible hydraulic oil. The computation results with the compressible fluid better agree with the experimental results. Recently, the power losses due to compressibility of oil in the pump under two cases of full displacement conditions were measured by Zecchi et al. (2013). They found that the power losses due to oil compressibility at full displacement conditions are an important source of power losses of a pump.

In this study, a series of experiment-based studies on the efficiency and losses of a typical axial piston pump over wide operating ranges are performed. Furthermore, a novel model capable of providing an explicit insight into the volumetric losses of pump is proposed to analyze the mechanism of leakage and deepen the understanding of the variation of volumetric losses with the displacement conditions.

2 Simulation modeling

A novel explicit volumetric losses model of a pump is developed, as shown in Fig. 1. The transient pressure of oil in a certain piston chamber can be represented by (Edge and Darling, 1989)

$$\frac{\mathrm{d}p_{\mathrm{c}}}{\mathrm{d}t} = \frac{q_{\mathrm{sp}}K_{\mathrm{e}}}{V_{\mathrm{c}}},\tag{1}$$

$$q_{\rm sp} = q_{\rm r} - q_{\rm i} - q_{\rm lp} - q_{\rm ls} - q_{\rm lv},$$
 (2)

where $p_{\rm c}$ denotes the transient pressure of oil in piston chamber, $V_{\rm c}$ stands for the volume of oil in piston chamber, $q_{\rm sp}$ represents the flow rate via the single piston chamber, $q_{\rm lp}$, $q_{\rm ls}$, and $q_{\rm lv}$ denote the leakage flow of piston/cylinder pair, slipper/swash plate pair, and valve plate/cylinder pair, respectively, $q_{\rm i}$ is the discharge and intake flow, and $q_{\rm r}$ denotes the flow rate generated by the reciprocating motion of piston, as

Eq. (3) describes. The compressibility of oil is considered by the elastic modulus of the oil, K_e .

$$q_{\rm r} = A_{\rm p} v_{\rm p},\tag{3}$$

where $A_{\rm p}$ is the piston crosssection area, $v_{\rm p}$ stands for the velocity of piston, derived from the dynamics module, which models the kinematics and dynamics of the pump parts, and transmits the kinematics parameters to the hydraulic module in real time, including the displacement $d_{\rm vdp}$ and the velocity $v_{\rm vdp}$ of the stroking piston, as well as the velocity of each piston. The stroking piston module supplies the driving force for the variable displacement piston of the pump in dynamics module to achieve different displacement conditions.

Expression for modeling the discharge and intake flow represented by the variable q_i in Eq. (2) for the piston might be given by the classical orifice equation, which is based on the Bernoulli principle, described in a form of (Manring, 2000; Ericson and Palmberg, 2012; Mandal *et al.*, 2012; Huang *et al.*, 2014; Xu *et al.*, 2015a; 2015b)

$$q_{\rm i} = C_{\rm r} A_{\rm r} \sqrt{2 |p_{\rm kp} - p_{\rm c}|/\rho} \cdot {\rm sign}(p_{\rm kp} - p_{\rm c}),$$
 (4)

where $C_{\rm r}$ is the discharge coefficient, ρ is the oil density, and $p_{\rm kp}$ is the pressure in the kidney port, which

repeatedly changes between the discharge pressure and intake pressure with the cylinder block rotating around the shaft. The flow area $A_{\rm r}$, which is integrated in the hydraulic module as valve plate model shown in Fig. 1, is described by a piecewise function divided into eight sections. The flow area over one revolution of shaft is portrayed in Fig. 2, where ODC is the outer dead center.

On the basis of the clearance flow theory between two parallel disks, the leakage flow via the constant valve plate/cylinder gap can be derived as

$$q_{\rm lv} = \frac{\alpha_{\rm f} \delta_{\rm v}^3}{12\mu} \left[\frac{1}{\ln(R_2/R_1)} + \frac{1}{\ln(R_4/R_3)} \right] (p_{\rm c} - p_0), \quad (5)$$

where α_f is the angle of the complete opening of the outlet opening in valve plate, δ_v is the oil film depth

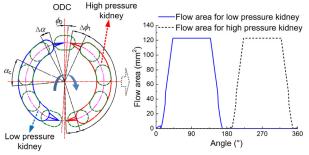


Fig. 2 Variation of flow area

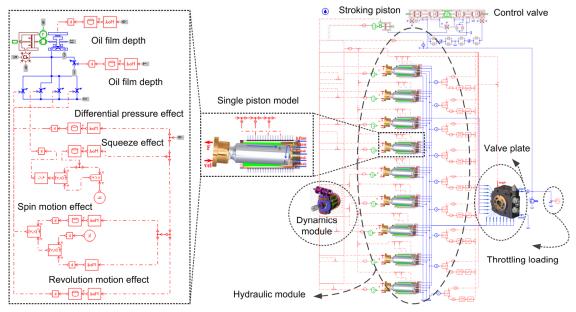


Fig. 1 Explicit volumetric losses model of the pump

of valve plate/cylinder pair, R_1 , R_2 , R_3 , and R_4 are the structure parameters of valve plate, μ is the dynamic viscosity of oil, and p_0 is the pressure of oil in the pump case.

The variation of pump displacement conditions directly influences the leakage flow via the piston/cylinder gap and slipper/swash plate gap. Therefore, the considerable emphasis in this study is mainly placed on the leakage of the piston/cylinder pair and slipper/swash plate pair. The leakage via the piston/cylinder gap is affected by the Poiseuille flow, which is linked with the differential pressure, and the Couette flow, which is linked with the piston velocity, as Eq. (6) describes:

$$q_{\rm lp} = \frac{\pi d_{\rm p} \delta_{\rm p}^3}{12 \mu l_{\rm p}} (1 + 1.5 \varepsilon_{\rm p}^2) (p_{\rm c} - p_{\rm 0}) - \frac{\pi d_{\rm p} \delta_{\rm p} v_{\rm p}}{2},$$
 (6)

where d_p is the diameter of piston, l_p is the gap length between piston and bush, δ_p is the oil film depth of piston/cylinder pair, and ε_p is the eccentricity of piston in cylinder bore.

The leakage flow via the slipper/swash plate gap consists of Poiseuille flow, Couette flow, and squeeze flow. The Poiseuille flow is linked with the differential pressure between slipper chamber and pump case; the Couette flow is linked with the revolution motion velocity and spin motion velocity of slipper; the squeeze flow is related to the squeeze velocity of the slipper.

The fluid continuity equation can be generally described in the form of Eq. (7), where z stands for the direction of oil film depth of slipper/swash plate pair, and r stands for the length in the radial direction.

$$\frac{\partial v_r}{\partial r} + \frac{1}{r} \frac{\partial v_\theta}{\partial \theta} + \frac{\partial v_z}{\partial z} + \frac{v_r}{r} = 0.$$
 (7)

With the Navier–Stokes equation and fluid continuity equation, Eq. (8) can be derived, where ω_{sm} is the spin angular velocity of the slipper, and δ_s is the oil film depth of slipper/swash plate pair. More detail of the derivation procedure of Eq. (8) can be found in Appendix A.

$$\frac{1}{\mu} \frac{\partial p}{\partial r} = \frac{\partial^2 v_r}{\partial z^2} + \frac{\rho \omega_{\rm sm}^2 r z^2}{\mu \delta^2}.$$
 (8)

Since the oil film depth is generally several micrometers, the variation of pressure in the direction of oil film depth is very small and can be neglected. Therefore, the pressure distribution of oil film of slipper/swash plate pair can be considered only a function of the variable r. The boundary condition of Eq. (8) can be described as

$$\begin{cases} z = 0, & \upsilon_r = 0, \\ z = \delta_s, & \upsilon_r = 0. \end{cases}$$
 (9)

By substituting the boundary condition shown in Eq. (9), Eq. (10) can be derived via the integration of Eq. (8) over the oil film depth:

$$\upsilon_{r} = \frac{1}{2\mu} \frac{\mathrm{d}p}{\mathrm{d}r} z(z - \delta_{s}) - \frac{\rho \omega_{sm}^{2} r}{12\mu} \left(\frac{z^{4}}{\delta_{s}^{2}} - z \delta_{s} \right). \tag{10}$$

The flow rate of fluid film flowing via the clearance between slipper and swash plate in the radial direction can be derived by integrating Eq. (10) over the oil film depth along the circumferential direction, as shown as

$$q_{\text{tem1}} = \int_0^{\delta_s} 2\pi r \upsilon_r dz = q_{\text{pde}} + q_{\text{sme}}, \tag{11}$$

$$q_{\rm pde} = -\frac{\pi r \delta_{\rm s}^3}{6\mu} \frac{{\rm d}p}{{\rm d}r},\tag{12}$$

$$q_{\rm sme} = \frac{\pi \rho \delta_{\rm s}^3 \omega_{\rm sm}^2 r^2}{20 \,\mu},\tag{13}$$

where $q_{\rm pde}$ is the Poiseuille flow, and $q_{\rm sme}$ is the Couette flow caused by the centrifugal force of a certain representative elemental mass of oil film in the lubricating interface between the slipper and swash plate, due to the spin motion of slipper. Integrating Eq. (12) over the radius r yields

$$q_{\text{pde}} = \frac{\pi \delta_{\text{s}}^3 \Delta p_{\text{s}}}{6 \mu \ln(R_{\text{s}}/r_{\text{s}})},\tag{14}$$

where Δp_s stands for the differential pressure between slipper chamber and pump case, and R_s and r_s denote the radius of slipper and slipper chamber, respectively. Integrating Eq. (13) over the radius r yields

$$q_{\rm sm} = \int_{r_{\rm s}}^{R_{\rm s}} q_{\rm sme} dr = \frac{\pi \rho \delta_{\rm s}^3 \omega_{\rm sm}^2}{60 \,\mu} (R_{\rm s}^3 - r_{\rm s}^3), \tag{15}$$

where $q_{\rm sm}$ is the leakage flow caused by the centrifugal force of oil film in the lubricating interface between slipper and swash plate, due to the spin motion of slipper.

As Fig. 3 shows, the slipper slides on the swash plate plane along an elliptical locus at the angular speed of $\omega_{\rm rm}$. The oil film in the clearance between slipper and swash plate is distributed in the annular area between the outer radius $R_{\rm s}$ and the inner radius $r_{\rm s}$ of the slipper. The oil film field is divided into four quadrants by the established coordinate system o-xy, as shown in Fig. 3, where S_1 , S_2 , S_3 , and S_4 stand for the quadrants divided by the o-xy coordinate system.

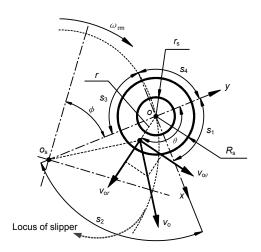


Fig. 3 Diagram for the derivation of Couette flow caused by the revolution motion of slipper

Taking a certain representative elemental volume dv of oil film as the analytical object, the corresponding tangential velocity v_0 of the representative elemental volume can be derived as (Xu *et al.*, 2012)

$$v_{o} = \frac{z\cos\beta\sqrt{l^{2} + r^{2} - 2lr\cos(\pi - \theta)}}{\delta_{s}(\cos^{2}\phi + \cos^{2}\beta\sin^{2}\phi)}\omega_{p}, \qquad (16)$$

$$l = R_{\rm p} \sqrt{\sin^2 \phi + \left(\frac{\cos \phi}{\cos \beta}\right)^2}, \tag{17}$$

where l is the distance between the points o_s and o, ω_p is the angular speed of pump, β is the swash plate

angle, R_p is the pitch circle radius of piston, and ϕ is the angular position of shaft. The radial velocity component v_{or} of the representative elemental volume is derived from Eq. (16) as

$$v_{or} = v_{o} \sin \theta. \tag{18}$$

The Couette flow caused by the revolution motion of slipper can be derived by the integration of the radial velocity of the representative elemental volume over the total volume of oil film field, as shown by Eq. (19), where the subscripts 1, 2, 3, and 4 stand for the number of quadrants, as shown in Fig. 3.

$$q_{\rm m} = \int_{r_{\rm s}}^{R_{\rm s}} \int_{z=0}^{\delta_{\rm s1}} \int_{\theta=0}^{\pi/2} \upsilon_{\rm or1} dr dz d\theta + \int_{r_{\rm s}}^{R_{\rm s}} \int_{z=0}^{\delta_{\rm s2}} \int_{\theta=\pi/2}^{\pi} \upsilon_{\rm or2} dr dz d\theta + \int_{r_{\rm s}}^{R_{\rm s}} \int_{z=0}^{\delta_{\rm s3}} \int_{\theta=\pi}^{3\pi/2} \upsilon_{\rm or3} dr dz d\theta + \int_{r_{\rm s}}^{R_{\rm s}} \int_{z=0}^{\delta_{\rm s4}} \int_{\theta=3\pi/2}^{2\pi} \upsilon_{\rm or4} dr dz d\theta.$$
(19)

For a certain representative annular elemental area $2\pi r dr$ of the oil film, the initial flow rate without squeezing is described by Eq. (12). However, actually due to the squeezing movement of slipper, the squeezed oil film will give rise to a variation of the flow rate, which can be calculated by Eq. (20) derived from Eq. (12):

$$dq = -2\pi d \left(\frac{\delta_{\rm s}^3}{12\mu} r \frac{dp}{dr} \right). \tag{20}$$

The variation of the flow rate is equal to the extrusion flow along the annular surface of the representative annular elemental area $2\pi r dr$ of oil film, given by

$$2\pi r dr \left(-\frac{d\delta_{s}}{dt} \right) = -2\pi d \left(\frac{\delta_{s}^{3}}{12\mu} r \frac{dp}{dr} \right). \tag{21}$$

By substituting the boundary condition described in Eq. (22), Eq. (23) can be derived by the integration of Eq. (21) over the radius r.

$$\begin{cases} r = r_{s}, & p = p_{s}, \\ r = R_{s}, & p = p_{0}, \end{cases}$$

$$p = (p_{s} - p_{0}) \frac{\ln(r_{s}/r)}{\ln(R_{s}/r_{s})}$$

$$+ \frac{3\mu}{\delta^{3}} \frac{d\delta_{s}}{dt} \left[(r^{2} - r_{s}^{2}) - (r_{s}^{2} - R_{s}^{2}) \frac{\ln(r_{s}/r)}{\ln(R/r)} \right] + p_{s},$$
(23)

where p_s is the pressure of oil in slipper chamber. The second term on the right of Eq. (23) represents the pressure caused by the squeezing effect of the oil film. Based on Eq. (23), we can obtain

$$\frac{dp}{dr} = \frac{(p_{s} - p_{0})}{\ln(R_{s}/r_{s})} (-r^{-1}) + \frac{3\mu}{\delta_{s}^{3}} \frac{d\delta_{s}}{dt} (2r)
+ \frac{3\mu}{\delta_{s}^{3}} \frac{d\delta_{s}}{dt} (R_{s}^{2} - r_{s}^{2}) \frac{-r^{-1}}{\ln(R_{s}/r_{s})}.$$
(24)

By substituting Eq. (24) into Eq. (12), Eq. (25) can be derived:

$$q = \frac{\pi \delta_{s}^{3}}{6\mu} \frac{(p_{s} - p_{0})}{\ln(R_{s}/r_{s})} - \pi r^{2} \frac{d\delta_{s}}{dt} + \frac{\pi}{2} \frac{(R_{s}^{2} - r_{s}^{2})}{\ln(R/r)} \frac{d\delta_{s}}{dt}.$$
(25)

The leakage flowing from slipper chamber to the pump case can be calculated from Eq. (25) by substituting the variable r with the value of r_s , as given by Eq. (26). The first term on the right of Eq. (26) represents the leakage flow caused by the differential pressure effect, and the second and third terms represent the leakage flow caused by the squeeze effect.

$$q = \frac{\pi \delta_{s}^{3}}{6\mu} \frac{(p_{s} - p_{0})}{\ln(R_{s}/r_{s})} - \pi r_{s}^{2} \frac{d\delta_{s}}{dt} + \frac{\pi}{2} \frac{(R_{s}^{2} - r_{s}^{2})}{\ln(R_{s}/r_{s})} \frac{d\delta_{s}}{dt}.$$
(26)

The variation of the flow rate caused by the change of volume of slipper chamber due to the squeezed oil film is given by

$$q_{\text{tem2}} = \pi r_{\text{s}}^2 \frac{\text{d}\delta_{\text{s}}}{\text{d}t}.$$
 (27)

From Eqs. (26) and (27), the composite extrusion flow of slipper/swash plate pair caused by the squeeze effect of oil film can be derived as

$$q_{\rm se} = \frac{\pi}{2} \frac{(R_{\rm s}^2 - r_{\rm s}^2)}{\ln(R_{\rm s}/r_{\rm s})} \frac{{\rm d}\delta_{\rm s}}{{\rm d}t}.$$
 (28)

With Eqs. (14), (15), (19), and (28), the leakage flow via the clearance between the slipper and swash plate can be finally derived as

$$q_{ls} = \frac{\pi \delta_{s}^{3} \Delta p_{s}}{6\mu \ln(R_{s}/r_{s})} + \frac{\pi \rho \delta_{s}^{3} \omega_{sm}^{2}}{60\mu} (R_{s}^{3} - r_{s}^{3})$$

$$+ \frac{\pi}{2} \frac{(R_{s}^{2} - r_{s}^{2})}{\ln(R_{s}/r_{s})} \frac{d\delta_{s}}{dt}$$

$$+ \int_{r_{s}}^{R_{s}} \int_{z=0}^{\delta_{s1}} \int_{\theta=0}^{\pi/2} \nu_{or1} dr dz d\theta$$

$$+ \int_{r_{s}}^{R_{s}} \int_{z=0}^{\delta_{s2}} \int_{\theta=\pi/2}^{\pi} \nu_{or2} dr dz d\theta$$

$$+ \int_{r_{s}}^{R_{s}} \int_{z=0}^{\delta_{s3}} \int_{\theta=\pi/2}^{3\pi/2} \nu_{or3} dr dz d\theta$$

$$+ \int_{r_{s}}^{R_{s}} \int_{z=0}^{\delta_{s4}} \int_{\theta=3\pi/2}^{2\pi} \nu_{or4} dr dz d\theta.$$
(29)

The output flow rate of pump is equal to the sum of the discharge flow of all piston/cylinder pairs of pump as

$$Q_{\rm ol} = \sum_{i=1}^{z_{\rm p}} q_{\rm spi}, \tag{30}$$

where z_p stands for the number of pistons in the high-pressure discharge side of the pump. The flow rate via the throttling valve of throttling loading module portrayed in Fig. 1 can be determined by

$$Q_{o2} = c_{q} A_{tl} \sqrt{\frac{2}{\rho} \Delta p_{tl}}, \qquad (31)$$

where c_q is the flow coefficient, A_{tl} is the throttling area, and Δp_{tl} is the differential pressure. Due to fluid continuity and fluid compressibility of oil in the output pipeline between the output port of pump and the throttling valve, we can obtain

$$Q_{o1} - Q_{o2} = \frac{V_{op}}{K_{o}} \frac{\mathrm{d}p}{\mathrm{d}t},$$
 (32)

where $V_{\rm op}$ is the volume of oil in output pipeline between output port of pump and throttling valve. Finally, the fluid character of the pump can be represented by Eq. (33), derived from Eqs. (30)–(32):

$$\frac{V_{\text{op}}}{K_{\text{e}}} \frac{dp}{dt} + c_{\text{q}} A_{\text{tl}} \sqrt{\frac{2}{\rho} \Delta p_{\text{tl}}} = \sum_{i=1}^{z_{\text{p}}} q_{\text{sp}i}.$$
 (33)

3 Experimental

A test bed to measure the efficiency and losses of pump was built, which is shown in Fig. 4. A typical axial piston pump widely used in the industry is chosen as the test pump, whose displacement is 90 cm³/r, with the rated pressure of 35 MPa and rated speed of 2100 r/min. Experiments were carried out over a range of working conditions varying from 13% to 100% of full displacement, with four groups of speeds varying between 1000 and 2100 r/min, as well as seven groups of pressure levels, from 5 to 35 MPa in increments of 5 MPa.

The variable-displacement servo piston of test pump was fixed by the stopper bolt to control the displacement stably. The hydraulic oil in the circuit was exchanged by using an additional pump to control the oil temperature. Pressure sensors and pressure gages were mounted on the input port, output port, and the leakage drain pipeline of the pump to monitor the pressure; also flow sensors were mounted at theses points to monitor the flow rate. A speed sensor and a torque sensor were mounted on the driving shaft

of pump to measure the input speed and torque of the pump. The speed of pump was adjusted by a variable-frequency motor. The load of the test pump was changed by adjusting the relief valve. The test data output by all the sensors with the standard signal were directly collected by the NI data acquisition card and transferred to the computer with the aid of data acquisition software. The volumetric losses P_{Vtp} and the hydro-mechanical losses P_{Mtp} of test pump could be derived by Eqs. (34) and (35) from the measured data. The overall efficiency η_{ov} , volumetric efficiency η_{V} , and mechanical efficiency η_{M} can be calculated by Eqs. (36)–(38), respectively. The total leakage flow q_{I} and compression flow q_{cp} of pump can be derived by Eqs. (39) and (40), respectively.

$$P_{\text{Vtp}} = (Q_{\text{i}} - Q_{\text{o}})(p_{\text{lo}} - p_{\text{drain}}),$$
 (34)

$$P_{\text{Mtp}} = 2\pi T n - (p_{\text{lo}} - p_{\text{li}})Q_{\text{o}} - (p_{\text{lo}} - p_{\text{drain}})(Q_{\text{i}} - Q_{\text{o}}), (35)$$

$$\eta_{\text{ov}} = Q_{\text{o}}(p_{\text{lo}} - p_{\text{li}}) / (2\pi T n),$$
(36)

$$\eta_{\rm V} = 1 - (Q_{\rm i} - Q_{\rm o})/Q_{\rm i},$$
(37)

$$\eta_{\rm M} = \eta_{\rm ov}/\eta_{\rm V},\tag{38}$$

$$q_1 = Q_{\text{drain}}, \tag{39}$$

$$q_{\rm cp} = Q_{\rm i} - Q_{\rm o} - Q_{\rm drain}, \tag{40}$$

where Q_i stands for the input flow rate of the pump, Q_0 is the output flow rate, p_{lo} and p_{li} stand for the output port pressure and input port pressure, respectively, p_{drain} is the drain pressure, Q_{drain} is the leakage flow of pump, T stands for the input torque, and n is the speed.

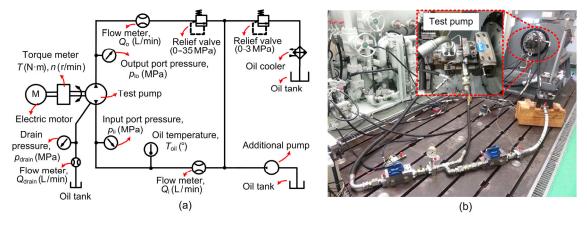


Fig. 4 Test circuit diagram (a) and test bed (b)

4 Results and discussion

4.1 Efficiency and comparison of losses

As shown in Figs. 5 and 6, the maximum overall efficiency of the test pump at a speed of 2100 r/min and 1000 r/min can reach 90%; nevertheless, with the decrease of displacement, the overall efficiency drops considerably. The highest overall efficiency of test pump can reach up to 90%, which demonstrates that the test pump works very well. Comparison between Figs. 5 and 6 shows that, with the decrease of speed from the rated speed (i.e., 2100 r/min) to 48% of the rated speed (i.e., 1000 r/min), the low-efficiency area of pump increases significantly, gradually extending from low displacement conditions to large displacement conditions. Correspondingly, the high-efficiency area of the pump gradually decreases, and moves from the middle-high pressure conditions to middle-

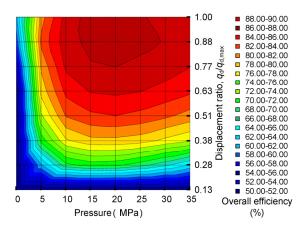


Fig. 5 Overall efficiency of pump measured by experiment at 2100 r/min pump speed

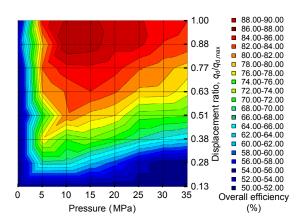


Fig. 6 Overall efficiency of pump measured by experiment at 1000 r/min pump speed

low pressure conditions. In Figs. 5 and 6, q_d and $q_{d,max}$ stand for a certain displacement and the full displacement of pump, respectively.

Comparison between volumetric losses and the corresponding hydro-mechanical losses of pump at the rated speed of 2100 r/min is shown in Fig. 7. The volumetric losses are found to be generally lower than the hydro-mechanical losses over a wide operating range. At the conditions of high pressure ranging from 30 to 35 MPa and large displacement ranging from 77% to 100% of full displacement, the volumetric losses can take the highest proportion, making up 47% of the pump's total power losses. After that, with the decrease of displacement or pressure, the proportion occupied by the volumetric losses gradually decreases. When the pressure decreases to 5 MPa and the displacement decreases to 13% of the full displacement, the proportion of volumetric losses in the total power losses of pump drops to 13%.

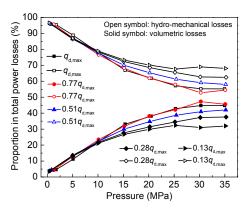


Fig. 7 Comparison of power losses of pump at the rated speed of 2100 r/min derived from the test data

Comparison of the proportion of leakage flow and compression flow in the total volumetric losses of pump at the rated speed of 2100 r/min is shown in Fig. 8. On the whole, the proportion of compression flow gradually decreases with the decrease of pressure or displacement. Under the condition of 13% of full displacement, the compression flow merely makes up several percent of the total volumetric losses. When the pressure is lower than 5 MPa or the displacement is lower than 38% of full displacement, the proportion of compression flow is lower than 20%. However, when the pressure is greater than 30 MPa and the pump displacement is greater than 88% of full displacement, the highest proportion of compression

flow losses in the total volumetric losses can reach up to 41%.

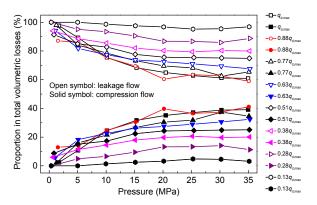


Fig. 8 Comparison between leakage flow and compression flow of pump at the rated speed of 2100 r/min, derived from the test data

4.2 Components analysis of leakage flow via the gap between slipper and swash plate

To obtain explicit insight into the mechanism of leakage flow of the pump by the constructed model portrayed in Fig. 1, there are several parameters that are needed to be determined, for instance, the oil film depth, the eccentricity of piston in cylinder bore, the spin motion velocity of slipper, the squeeze velocity of oil film, etc. These parameters are hard to measure and depend upon the different transient working conditions of the pump. One of the available solutions is to use a verified implicit numerical program to find out the value of the parameters. The implicit numerical program models are built by using the Reynolds

equation of lubrication, solved with the finite volume method (FVM), taking the influences of dynamic macro-motion and micro-motion of parts, the elastic deformation, the force equilibrium, and the pressure-viscosity effect into consideration. The details are given in the previous studies of the authors (Xu *et al.*, 2012; 2013).

The depth fields of oil film in piston/cylinder interface and slipper/swash plate interface are illustrated in Fig. 9. Generally, the depth fields are in non-uniform distribution. The angle axis in Fig. 9a stands for the angular position in circumferential direction around the piston, and the length ratio axis stands for the contact length ratio between the piston and bush.

To consider the impact of the non-uniform depth field of oil film on the leakage flow, the non-uniform depth field is considered as the mean depth at each angular position of the piston. The mean depth of oil film is the mean value of the depth of each discrete nodes of oil film field, as described in Eqs. (41) and (42), where δ_{pm} and δ_{sm} denote the mean depths of oil film of piston/cylinder pair and slipper/swash plate pair, respectively, K_p and K_s are the total numbers of discrete nodes of oil film field of piston/cylinder pair and slipper/swash plate pair, and δ_{pk} and δ_{sk} are the depths of the kth discrete node of oil film field of the piston/cylinder pair and the slipper/swash plate pair, respectively. The discretization methods of oil film field of piston/cylinder pair and slipper/swash plate pair are introduced in detail in the previous studies undertaken by the present authors (Xu et al., 2012; 2013; 2015c).

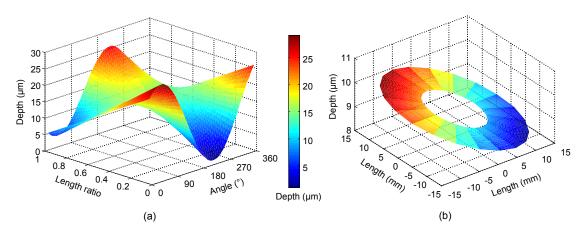


Fig. 9 Depth field of oil film obtained by simulation at 1500 r/min pump turning speed, 28 MPa pressure, and full displacement: (a) oil film of piston/cylinder pair, at the angular position of 159° relative to the outer dead point of piston; (b) oil film of slipper/swash plate pair at the angular position of 21° relative to the outer dead point of piston

$$\delta_{\rm pm} = \frac{1}{K_{\rm p}} \sum_{k=1}^{K_{\rm p}} \delta_{\rm pk}, \qquad (41)$$

$$\delta_{\rm sm} = \frac{1}{K_{\rm s}} \sum_{k=1}^{K_{\rm s}} \delta_{\rm sk}.$$
 (42)

The leakage of single slipper/swash plate pair is explicitly analyzed and shown in Fig. 10, consisting of four components: the Poiseuille flow caused by the differential pressure effect, the squeeze flow caused by the squeeze effect, the Couette flow caused by the spin motion, and the revolution motion of slipper. $q_{\rm cs}$ represents the leakage flow via the slipper/swash plate gap caused by the different effects discussed above. The spin motion velocity of slipper is approximately equal to the speed of the shaft, according to the experimental results measured by Fang and Ikeya (1992) and Tanaka *et al.* (2003). The squeeze velocity of slipper is shown in Fig. 11.

For a long time, in the conventional equation to calculate the leakage flow of slipper/swash plate pair, only the Poiseuille flow was considered. As Fig. 10 reveals, the Couette flow caused by the spin motion and revolution motion of slipper is much smaller than the Poiseuille flow and squeeze flow. Therefore, in the conventional calculation of leakage flow of slipper/swash plate pair, the Couette flow is allowed to be neglected. However, the result of calculation in Fig. 10 indicates that the squeeze flow might reach a magnitude equal to that of the Poiseuille flow. That means that squeeze flow should be taken into account when calculating the leakage flow of slipper/swash plate pair.

4.3 Variation characteristics of volumetric losses with displacement of pump

The mean depth of oil film and the inclined angle of piston or the overturning angle of slipper are the important factors reflecting the variation characteristics of leakage flow.

As shown in Fig. 12, the overturning angle α_s of slipper can be calculated by Eq. (43), where $\delta_{s,max}$ and $\delta_{s,min}$ stand for the maximum and minimum values of the depth of oil film of slipper/swash plate pair,

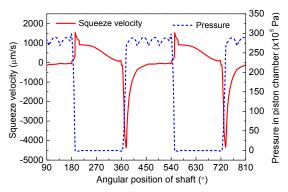


Fig. 11 Squeeze velocity of slipper obtained by simulation at 1500 r/min pump turning speed and full displacement

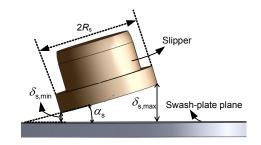


Fig. 12 Tilting state of slipper

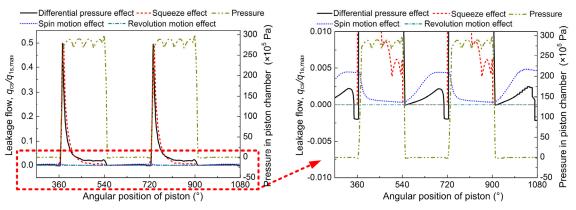


Fig. 10 Components analysis of leakage via the gap between slipper and swash plate obtained by simulation at 1500 r/min pump turning speed and full displacement

 $q_{\rm ls,max}$ represents the maximum instantaneous leakage flow via the slipper/swash plate gap

respectively, which can be determined by the verified implicit numerical program developed in the previous study of the authors (Xu *et al.*, 2012).

$$\alpha_{\rm s} = \arcsin \frac{\delta_{\rm s,max} - \delta_{\rm s,min}}{2R_{\rm s}}.$$
 (43)

As shown in Fig. 13, the inclined angle α_p of piston can be calculated by Eq. (44), where l_f is the contact length between the piston and bush, and e_1 , e_2 , e_3 , and e_4 are the eccentricity of piston section relative to cylinder bore at the position of the two end surfaces of bush, which can be determined by the verified implicit numerical program developed in the previous study of the authors (Xu *et al.*, 2013).

$$\alpha_{\rm p} = \arctan \frac{\sqrt{(e_1 - e_3)^2 + (e_2 - e_4)^2}}{l_{\rm e}}$$
 (44)

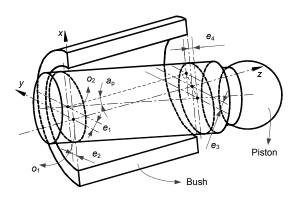


Fig. 13 Tilting state of piston in cylinder bore

Fig. 14 shows the variation of mean depth of oil film in the slipper/swash plate gap and the mean overturning angle of the slipper versus the displacement conditions of pump. With the decrease of displacement, the mean depth of the oil film increases, with a greater variation rate than the decrease rate of the overturning angle of slipper. According to Eq. (29), the variation of oil film depth and overturning angle finally yields the increase of leakage via the slipper/swash plate interface with the decreasing displacement of pump, as shown in Fig. 15, where $n_{\rm r}$ and $p_{\rm r}$ stand for the rated speed and the rated pressure, $\delta_{\rm sd,m}$, $q_{\rm lsd,m}$, and $\alpha_{\rm sd,m}$ are the mean value of the oil film depth, the mean value of the leakage flow of slipper/

swash plate pair, and the mean overturning angle of slipper at a certain displacement condition, and $\delta_{\rm sd,max}$, $q_{\rm lsd,max}$, and $\alpha_{\rm sd,max}$ are the maximum mean values of the oil film depth, the leakage flow of slipper/swash plate pair, and the overturning angle of slipper, respectively, under all the considered displacement conditions.

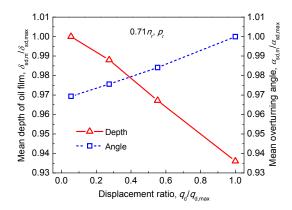


Fig. 14 Mean oil film depth of slipper/swash plate pair and overturning angle of slipper versus displacement obtained by simulation

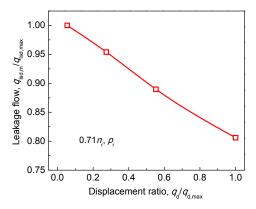


Fig. 15 Variation of leakage via slipper/swash plate gap versus pump displacement obtained by simulation

With the decrease of pump displacement, the variation of mean oil film depth of piston/cylinder pair and inclined angle of piston in cylinder bore are portrayed in Figs. 16 and 17, corresponding to the different pump speeds, where $\delta_{\rm pd,m}$ and $\alpha_{\rm pd,m}$ are the mean value of the oil film depth of piston/cylinder pair and the mean value of the inclined angle of piston at a certain displacement condition, and $\delta_{\rm pd,max}$ and $\alpha_{\rm pd,max}$ are the maximum mean value of the oil film

depth of piston/cylinder pair and the maximum mean value of the inclined angle of piston, respectively, under all the considered displacement conditions. At different speeds, the mean oil film depth of piston/cylinder pair presents different variation trends; however, the inclined angle of the piston in the cylinder bore gradually decreases with the decreasing displacement.

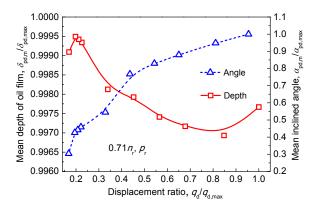


Fig. 16 Mean oil film depth of piston/cylinder pair and inclined angle of piston versus pump displacement obtained by simulation at $0.71n_{\rm r}$

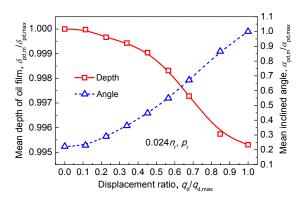


Fig. 17 Mean oil film depth of piston/cylinder pair and inclined angle of piston versus pump displacement obtained by simulation at $0.024n_{\rm r}$

As described in Eq. (6), the leakage flow through the piston/cylinder interface is proportional to the cube of oil film depth and the square of the eccentricity of piston, represented by the inclined angle of piston in the cylinder bore. The variations of oil film depth and inclined angle of piston portrayed in Figs. 16 and 17 give rise to the leakage flow through the piston/cylinder interface shown in Fig. 18, where

 $q_{\rm lpd,m}$ is the mean value of the leakage flow of piston/cylinder pair at a certain displacement condition, and $q_{\rm lpd,max}$ is the maximum mean value of the leakage flow of piston/cylinder pair under all the considered displacement conditions. At a relatively high speed of 71% of the rated speed, the corresponding leakage flow via the piston/cylinder interface first decreases with the decrease of displacement, and then increases with the further decrease of displacement. However, at a relatively low speed of 2.4% of rated speed, the leakage flow increases with decreasing displacement over the full range of the displacement conditions.

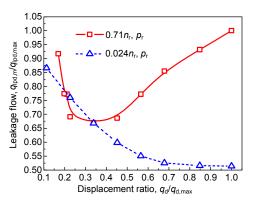


Fig. 18 Leakage flow of piston/cylinder pair versus pump displacement obtained by simulation

The typical variations of measured volumetric losses of pump versus displacement conditions are illustrated in Fig. 19. The compression flow is found to be almost proportional to the displacement of pump. However, Fig. 19 shows that the leakage flow takes on an increasing trend, with the displacement decreasing to a certain low displacement operating point. The leakage flow generally increases with the decrease of displacement, or may decrease with the decrease of displacement first, and then begin to increase after the minimum with the further decrease of displacement. The simulation-based variation trends of leakage flow illustrated in Figs. 15 and 18 are in accordance with the experimental variation trends of leakage.

However, it should be noticed that there are also a few exceptions that can be found at some operating points, as shown in Fig. 20. The compression flow is almost proportional to the displacement of pump, but the leakage flow first decreases with the decrease of pump displacement, and after the minimum, the leakage flow almost remains unchanged with further decrease of the pump displacement. The pulsation of leakage flow is mainly caused by the unstable actual pressure. It can be said that from the large number of measurement data, the few exceptions just indicate a

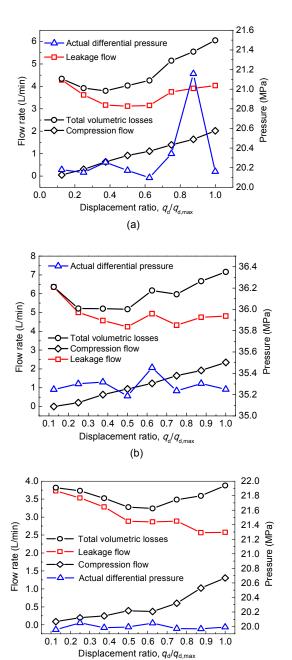


Fig. 19 Volumetric losses versus pump displacement (a) Under the conditions of 1700 r/min and 20 MPa; (b) Under the conditions of 1300 r/min and 35 MPa; (c) Under the conditions of 1000 r/min and 20 MPa

(c)

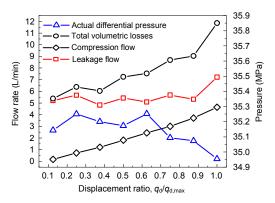


Fig. 20 Volumetric losses versus pump displacement under the conditions of 2100 r/min and 35 MPa

possible variation trend of leakage flow, but they cannot represent the general and typical variation characteristics of leakage flow with respect to displacement conditions, which are shown in Fig. 19.

5 Conclusions

In this study, a series of experiments were carried out to find the variation characteristics of efficiency, leakage, and compression flow of a pump over a wide operating range, especially for the displacement conditions. The mechanism of leakage via slipper/swash plate gap was further analyzed in detail by the proposed novel volumetric losses model, with a more complete equation to calculate the leakage via the slipper/swash plate gap. Compared with the previous models, the beauty of the novel model is that it allows explicit insight into the components of leakage flow. For the leakage of the slipper/swash plate pair, the squeeze leakage caused by the squeeze micromotion of the slipper is found to reach a magnitude equal to that of the Poiseuille flow caused by the differential pressure effect.

The overall efficiency of the pump is found to drop considerably with the decrease of displacement. With the speed decreasing from rated speed to 48% of the rated speed, the low-efficiency area of pump significantly increases. At the rated speed, the volumetric losses take a proportion ranging from 13% to 47% of the total power losses of pump, under the conditions of pressure ranging from 5 to 35 MPa and pump displacement ranging from 13% to 100% of

full displacement. The highest proportion of compression flow losses in the total volumetric losses of pump at the rated speed can reach up to 41% when the pressure is greater than 30 MPa and the pump displacement is greater than 88% of full displacement. After that, generally the proportion gradually decreases with the decrease of displacement or pressure. When the pressure decreases to less than 5 MPa or the displacement decreases to less than 38% of full displacement, the proportion decreases to less than 20%.

The compression flow decreases with the decrease of displacement. However, the leakage flow generally increases with the decrease of displacement, or may decrease with the decreasing displacement first, and then begin to increase after the minimum with the further decrease of displacement.

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Appendix A: Derivation of Eq. (8)

The following are the detail of the derivation procedure of Eq. (8) in the main text. Referring to a cylindrical coordinate system, in which the lubricating interface is defined in the (r, θ) plane, such that z is the direction of the film thickness. The velocity in the direction of θ -axis v_{θ} is determined by the following equation (A1), where ω is the angular velocity, z is the thickness, δ_s is the thickness of oil film.

$$v_{\theta} = r\omega \frac{z}{\delta_{s}}.$$
 (A1)

The lubrication theory allows the following assumptions to be made regarding fluid behavior in the thin film regime between slipper and swash plate:

- 1. Fluid inertial forces are small when compared with the viscous forces and can be negligible;
 - 2. Steady state is assumed;
 - 3. Body forces of the fluid are negligible;
- 4. Pressure is uniform along the film thickness *z*-axis direction. Similarly, fluid viscosity and density are assumed constant across the fluid film;
 - 5. The fluid flows along the r-axis direction.

Based on these assumptions, the Navier–Stokes equation strongly reduces to

$$\upsilon_{r} \frac{\partial \upsilon_{r}}{\partial r} - r\omega^{2} \frac{z^{2}}{\delta_{s}^{2}} = -\frac{1}{\rho} \frac{\partial p}{\partial r}
+ \nu \left[\frac{\partial^{2} \upsilon_{r}}{\partial r^{2}} + \frac{1}{r} \frac{\partial \upsilon_{r}}{\partial r} + \frac{\partial^{2} \upsilon_{r}}{\partial z^{2}} - \frac{\upsilon_{r}}{r^{2}} \right],$$
(A2)

where ν is the kinematic viscosity of fluid film. The fluid continuity equation reduces to

$$\frac{\partial v_r}{\partial r} + \frac{v_r}{r} = 0. \tag{A3}$$

Integrating Eq. (A3) over the radius r yields

$$\frac{1}{r}\frac{\partial v_r}{\partial r} - \frac{v_r}{r^2} + \frac{\partial^2 v_r}{\partial r^2} = 0.$$
 (A4)

Substituting Eq. (A4) into Eq. (A2) yields

$$\frac{1}{\mu} \frac{\partial p}{\partial r} = \frac{\partial^2 v_r}{\partial z^2} + \frac{\rho \omega^2 r z^2}{\mu \delta_s^2} - \frac{\rho v_r}{\mu} \frac{\partial v_r}{\partial r}, \tag{A5}$$

where dynamic viscosity $\mu = \rho v$. For the lubricating interface between slipper and swash plate, the following Eq. (A6) is true:

$$\frac{\partial v_r}{\partial r} \ll \frac{\partial p}{\partial r}$$
. (A6)

Therefore, Eq. (A5) reduces to the following Eq. (A7), i.e., Eq. (8) in the main text:

$$\frac{1}{\mu}\frac{\partial p}{\partial r} = \frac{\partial^2 v_r}{\partial z^2} + \frac{\rho \omega^2 r z^2}{\mu \delta_s^2}.$$
 (A7)

中文概要

題 目: 宽幅排量工况下轴向柱塞泵容积损失及效率变化 特征

日 的:宽幅排量工况下高效率性能对于作为变排量泵控 节能系统动力源的柱塞泵至关重要,而现有研究 对宽幅排量工况下泵效率及各容积损失变化特 征的认识尚为不足。本研究探索并阐明泵效率、 容积损失(泄漏损失及压缩流量损失)及各损失 所占比重随排量工况的变化特征。

创新点: 1.提出更完整的滑靴副泄漏计算方程,建立显式容积损失仿真模型,发现由滑靴挤压微运动造成的挤压泄漏的不可忽略性; 2.揭示泵压缩流量、泄漏流量及其造成的能量损失随排量工况的变化特征。

方 法: 1. 基于纳维-斯托克斯方程及流体连续性方程,推导出更完整的滑靴副泄漏计算方程,基于此方程建立显式容积损失仿真模型; 2. 在不同压力、转速及排量工况组合下对泵各损失进行 224 组大范围工况下的大量实验测试; 3. 基于仿真结果及实验结果对宽幅排量工况下泵效率及各容积损失变化特征进行分析讨论。

结 论: 1. 泵总效率随排量减小显著下降; 2. 在额定转速 工况下, 5~35 MPa 压力等级及 13%~100% 满排 量变化范围内, 泵容积损失在泵总损失中所占比 重在 13%~47% 幅度内变化; 3. 额定转速下泵压 缩流量损失在总容积损失中所占比重在 30 MPa 压力及88%满排量等级以上时最高可达41%,此 后随着排量减小而逐渐减小, 当排量降至低于 38%满排量或压力降至低于 5 MPa 时, 压缩流量 损失在泵总容积损失中占比低于 20%; 4. 压缩流 量随排量减小而减小,而在绝大部分工况下,泵 泄漏流量的典型变化特征是随着排量减小而逐 渐增大,或先随着排量减小而减小,但在当减小 到某一极小值时随着排量进一步的减小而逐渐 增大; 5. 由滑靴挤压微运动造成的滑靴副挤压泄 漏可以达到与由压差效应造成的滑靴副压差泄 漏相当的数量级。

关键词:轴向柱塞泵;效率;泄漏;压缩流量;排量工况