ORIGINAL ARTICLE



Permeability testing of radiation shielding concrete manufactured at industrial scale

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Received: 15 December 2017/Accepted: 13 June 2018/Published online: 16 June 2018 \tilde{C} The Author(s) 2018

Abstract The effect of the composition of industrial concrete designed for radiation shielding structures on the air permeability and the diffusion of moisture was studied. The mix design for heavyweight concrete of bulk density 3168–3317 kg/m³ was developed using barite and magnetite aggregate and cements blended with fly ash and blastfurnace slag. Structural elements, like columns of a height of 4 m and massive blocks made of mixtures with different cements were manufactured using ready mixed concrete pumped into the formwork. Core specimens were taken from the elements at different locations. The air permeability index was tested using Autoclam device. Evaluation of the quality of concrete on the basis of API results varied from "very good" to "good". The moisture distribution inside concrete specimens was equilibrated to RH = $60 \pm 5\%$. Observation of RH changes allowed to determine the moisture diffusion coefficient. Significant differences of the permeability and moisture diffusion coefficient depending on the location of the core specimens drilling and mix design of

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Faculty of Civil Engineering, Mechanics and Petrochemistry, Warsaw University of Technology, 17 Łukasiewicza St., 09-400 Plock, Poland e-mail: wojciech.kubissa@pw.edu.pl concrete were found. The D coefficient provided a good reflection of the different quality of heavyweight concrete in structural elements.

Keywords Air permeability · Autoclam · Barite · Blended cement · Cracking · Heavyweight aggregate · Magnetite · Moisture diffusion · Radiation shielding concrete · Relative humidity

1 Introduction

The criteria for selection of ingredients and concrete mix design for radiation shielding structures include both mechanical and physical properties, the shielding against ionizing radiation, and also the impermeability to liquids and gases [1, 2]. The concrete in the cover of the nuclear reactor should be impermeable to potentially radioactively contaminated air and water (due to, for example, the leakage of the reactor cooling system). A low permeability concrete can also prevent the penetration of harmful substances to the inside of the structure. This reduces the risk of corrosion of the reinforcement or the destruction of the concrete. It is important for example in the storage pools for spent fuel [3]. For the design and production of radiation shielding concrete usually the special heavy aggregates are used, such as barite, magnetite, hematite [4]. The significance of cement selection for radiation shielding concrete was discussed by Baran et al. [5]. Therefore there is a risk of segregation of the components of the mixture with inadequate production, transport or compaction of the mixture [6–8]. Abnormal heterogeneity of concrete can lead to local radiation surges and such cases should be effectively prevented.

The measurement of permeability of shielding concrete used in nuclear power plants is carried out by various methods. Three methods of determining the air permeability of concrete are recommended by IAEA [9], i.e. the Torrent method, the Autoclam method and the surface airflow method. The air permeability depends on the pore system but also largely on the water content in pores [10, 11]. Therefore, coefficients or correction charts are used to determine approximately the surface moisture of concrete based on the measurement of electrical resistance [12]. The relationship is difficult to establish because of the presence near-surface moisture gradients [13]. The electrical resistivity measurement is less accurate and the scatter of results is greater in comparison to the direct RH measurement. It is also highly sensitive to the cement type as a result of the variance in electrical conductivity of the pore solution, caused by the clinker phase composition, addition of supplementary cementitious materials like blastfurnace slag [14].

The air permeability determination of concrete at partial water saturation conditions corresponds to the operating conditions of radiation shielding structures. As Oxfall demonstrated [15], the representative environmental conditions are determined by the temperature of concrete from 50 to 65 °C and the relative humidity RH from 40 to 60%. The RH of concrete is maintained at this level even after many years of operation of nuclear reactor. An exception is the concrete layer in the immediate vicinity of the reactor. The air permeability of laboratory specimens of shielding concrete in a specific moisture state was investigated in [16]. Using the Autoclam method both significant effects of type of cement and aggregate type were demonstrated. Also the essential effects of equalization of the humidity distribution in the cross section of specimens were shown. Similar methodological observations resulted from [17], although related to the normal weight concrete. The method of preparation of 100 mm cylindrical specimens with



uniformly distributed RH, using the surface RH measurement, is also shown in [18].

In the undamaged zones of a structure the low permeability of concrete allows to prevent any significant leakage through containment building walls [19]. However, the permeability can be significantly influenced by cracks [20], therefore the effects of micro cracking on the air permeability of concrete are relevant to the integrity of containment [21]. Such effects can be experimentally studied only in the industrial scale, not on small laboratory-manufactured specimens.

The moisture movement in concrete can cause different types of volume changes. The drying shrinkage is especially important in radiation-shielding concrete because it results in tensile stresses which can cause cracking. Large cracks could reduce the performance of radiation shields [22, 23]. Excessive moisture diffusion coefficients are unfavourable, they can lead to faster drying of concrete. This may have an adverse effect on the shielding performance.

Moisture movement phenomena in cement-based porous materials are quite complex because of both physical and chemical interactions between water molecules and solid phases. The development of a holistic model of the transport phenomena is a serious challenge [24]. The transport of water is generally dominated by the molecular water diffusion. Theoretical models of moisture movement in porous media are usually based on the Fick's law [25]. New calculation models are developed for the analysis of movement of moisture in concrete [25, 26]. Magnetic resonance imaging (MRI) and other modern testing techniques allow for a better understanding of the occurring phenomena. Experimental data is used as a proof of conformity of theoretical models with the actual moisture movement in concrete [27].

The moisture diffusion coefficient in concrete is highly variable and depends on many factors. Bažant [28] draws attention to the relationship between the coefficient D and the RH gradients, not specifying the resulting differences. Depending on the age of concrete the coefficient D can vary by up to two orders of magnitude [29]. The influence of temperature is also very important [30]. The assumed computational model and its parameters can also cause significant differences in D coefficient calculated from the same experimental data. The purpose of the research undertaken by the authors is to evaluate the effects of mix design of heavyweight concrete manufactured in industrial scale, intended for radiation shields, on the air permeability and the diffusion of moisture through concrete. The investigation was carried out on the specimens cut from structural elements made of concrete manufactured at a ready-mix concrete plant.

2 Experimental

2.1 Materials and preparation of structural elements

Concrete mixes were made in a Stetter concrete mixing plant with a filling capacity 0.75 m³. Using the truck mixer the mix was transported to the place of concreting. Concrete columns with a diameter of 400 mm and a height of about 4.0 m in the steel formwork were cast. Concrete mix was fed using a pump vehicle, the compaction was achieved using a poke vibrator. Large concrete blocks $1.0 \times 1.0 \times 0.8$ m were cast in prepared molds with thermal insulation on the side walls and at the bottom. Concrete mixture was fed directly from the hopper of truck mixer and compacted using a poke vibrator. The composition of the concrete mixtures used for making the columns and the blocks is given in Tables 1 and 2. Two types of heavyweight aggregates were applied for concrete mixes: crushed magnetite (the density of 4.80 kg/dm^3 , the content of Fe₃O₄ of about 89.7%) supplied in two fractions 0/5 and 0/16 mm, and crushed barite aggregate (the density of 4.20 kg/dm^3 , the content of BaSO₄ of about 92%) supplied as 0/16 mm fraction. Common cements, manufactured according to the European standard PN-EN 197-1, were used, both Portland cement and blended cements. The basic properties of cements are given in Table 3.

European standard methods were used to test fresh concrete properties: the consistency, the bulk density and the temperature. Fresh mix properties are also given in Tables 1 and 2. No signs of mixture segregation were observed during mixing and fresh concrete testing. Companion standard specimens were manufactured for the compressive strength determination and for the drying shrinkage evaluation. The 150 mm cube specimens and prismatic $100 \times 100 \times 500$ mm specimens were manufactured and cured following the respective procedures.

2.2 Specimens and test methods

Basic concrete properties were determined using European standard procedures. The compressive strength of concrete was determined on 150 mm cubes in accordance with PN-EN 12390-3. The specimens were stored in the high moisture temperature controlled cabinet (20 ± 2 °C, RH > 95%) until

Table 1The composition (kg/m^3) and properties of	Components and properties	Mixture ID	
fresh concrete mixes used to		В	А
height of 4 m	Cement CEM II/B-S 32.5 R	314	
	Cement CEM III/A 42.5N-HSR/NA		342
	Sand 0/2 mm	567	363
	Crushed magnetite 0/5 mm	786	-
	Crushed magnetite 0/16 mm	1437	-
	Crushed barite 0/16 mm	_	2298
	Water	194	164
	Plasticizer	2.35	0.61
		Lubet C	Fluid optima 100
	Bulk density (kg/m ³)	3300	3168
	Slump (cm)	21.0	11.0
	Temperature (°C)	12	19
	<i>w/c</i> ratio	0.62	0.48

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Table 2The composition(kg/m³) and properties offresh concrete mixes T49–T51 used to make massiveblocks

Components and properties	Mixture ID	Mixture ID						
Type of cement	T49 CEM I 52.5 R	T50 CEM II/B-V 32.5 R	T51 CEM II/B-S 32.5 R					
Cement	405	399	402					
Water	201	198	199					
Sand 0/2 mm	555	547	551					
Crushed magnetite 0/5 mm	634	625	629					
Crushed magnetite 0/16 mm	1520	1498	1508					
Plasticizer (%m.c.)	0.5	0.5	0.5					
Bulk density (kg/m ³)	3317	3269	3291					
Slump (cm)	13.0	11.0	11.0					
Temperature (°C)	22	22	22					
<i>w/c</i> ratio	0.50	0.50	0.50					

Table 3 Physical properties of cements used for heavyweight concrete mixes

Properties	CEM I 52.5R	CEM II/B-V 32.5R	CEM II/B-S 32.5R	CEM III/A 42.5N-HSR/NA ^a
Compressive strength (MPa) at				
2 days	36.9	16.1	18.9	25.1
28 days	67.7	43.8	51.6	60.1
Initial setting time (min)	164	325	224	212
Water to the standard consistency (%)	30.0	27.9	28.4	28.2
Soundness (mm)	0.5	0.7	0.6	0.4
Specific surface area (Blaine) (cm ² /g)	4558	3360	3751	3702

^aSulphate resistant, low alkali cement $Na_2O_{eq} = 0.63\%$ according to PN-B 19707

testing. The compressive strength of concrete was determined at the age of 28 and 90 days (Table 4). Only for the series T49, T50 and T51 the compressive strength was also determined at the age of 630 days.

The shrinkage tests were performed in accordance with ISO 1920-8 modified following prEN 12390-16. Specimens were demoulded at 24 h after casting and placed in the drying room at the temperature of 20 ± 2 °C and the relative humidity of $60 \pm 5\%$. The length change was recorded until 90 days (Table 5).

A significant strength increase was noted at the age of almost 2 years for concrete specimens manufactured with CEM II/B-V and CEM II/B-S cements and magnetite aggregate. The observed drying shrinkage results are consistent with the trends presented in [31]. A larger shrinkage was observed in concrete with

Table 4 The compressive strength of concrete (MPa) tested on 150 mm cube specimens (the average value and the standard deviation of 3 specimens)

Age (days)	Concrete mix for	column	Concrete mix for	Concrete mix for large blocks				
	В	А	T49	T50	T51			
28	35.2 (± 1.6)	45.3 (± 2.1)	54.4 (± 1.4)	49.6 (± 1.8)	48.3 (± 1.9)			
90	40.5 (± 1.5)	48.6 (± 1.9)	57.1 (± 2.6)	65.0 (± 1.1)	62.6 (± 1.6)			
630	-	-	59.2 (± 1.7)	77.2 (± 2.4)	71.5 (± 2.2)			



Concrete designation	Drying time (days)							
	7	14	21	28	35	42	56	90
В	0.167	0.27	0.33	0.389	0.426	0.434	0.463	0.513
	0.021	0.046	0.045	0.043	0.047	0.051	0.054	0.053
A	0.212	0.298	0.353	0.426	0.461	0.491	0.517	0.612
	0.062	0.059	0.053	0.061	0.063	0.042	0.049	0.077
T49	0.117	0.211	0.289	0.342	0.371	0.388	0.415	0.471
	0.039	0.057	0.053	0.078	0.084	0.079	0.077	0.084
T50	0.151	0.239	0.291	0.311	0.357	0.357	0.494	0.537
	0.045	0.049	0.042	0.048	0.051	0.040	0.084	0.092
T51	0.200	0.346	0.383	0.412	0.422	0.446	0.461	0.510
	0.020	0.039	0.031	0.024	0.020	0.008	0.006	0.013

Table 5 Drying shrinkage of concrete (mm/m) in time (the average value and the standard deviation of 3 specimens)

barite aggregate as compared to shrinkage of concrete with magnetite aggregate.

Specimens for air permeability testing were taken as drilled cores from manufactured structural members made of ready mix concrete. The concrete columns were first laid down and sliced to obtain two thick disks ϕ 400 by 170 mm from the top and the bottom part of a column. The location of the disks along the column height was at the distance of about 3.4 m. The specimens A and B were drilled from these slices at the top and the bottom of manufactured columns. The companion cores drilled form these thick concrete slices were taken to make polished plane sections for aggregate grain distribution evaluation. The specimens T49, T50 and T51 were cored from three large blocks perpendicular to the top surface. The cores of 150 mm in diameter and about 450 mm in height were sectioned to obtain two cylindrical specimens of 150 mm high out of each core rejecting about 30 mm upper layer of the core All the core specimens were trimmed using water-lubricated diamond saw to obtain flat ends.

The relative humidity (RH) in concrete was measured using Vaisala HMP44 probes with HM40 indicator. Autoclam device from Amphora Company was used to measure the Air Permeability Index (API) [32]. The modification of the API test procedure involves applying of an annular seal, between the base ring and the concrete surface, made of microgum with a thickness of 8 mm, and also clamping a steel ring with G-clamps instead of using expansion anchors in the bored holes. The side surfaces of cylindrical core specimens were covered with a resin layer, which was impermeable to water and air. The indices API were determined at the center of each opposite, non-isolated specimen end surface. The RH and temperature probes were inserted in plastic tubes placed into drilled holes with a diameter of 16 mm at a certain depth from the specimen surface: 30 and 75 mm below the nonisolated surface of the specimens. The assumed specimen preparation procedure and the unidirectional moisture movement ensured the uniformity of specimen drying on both sides. For the analysis and calculations a symmetrical distribution of RH was assumed with respect to the plane passing through the center of the specimen parallel to the unprotected walls. This permitted a determination of the RH distribution in a specimen based on measurements at three points.

2.3 Specimen conditioning and API, RH measurements

In comparison to the research described in [16], a modified specimen preparation procedure was applied with a specified target RH, uniformly distributed in specimens. The specimen conditioning and API, RH measurements were performed in several steps, including:

- a. the hole drilling for placing the tubes for RH probe insertion,
- b. the placement of moisture barrier on lateral sides of cylindrical specimens,
- c. the initial measurement of API and RH of concrete before drying,

- d. the drying of specimens in the thermostatic chamber with weekly RH measurements, until the target RH achieved,
- e. the placement of moisture barrier around specimens and storage of moisture-insulated specimens at controlled laboratory conditions until the moisture equilibrium achieved,
- f. the measurement of API at stabilized target RH of concrete,
- g. the oven drying of specimens at 105 °C and subsequent measurements of API.

The side surface of the specimens was secured by an impermeable resin in order to provide an unidirectional transport of moisture during the drying and stabilization. The measurements of RH at the specimen surface were carried out using the device shown in Fig. 1a. The instrument consisted of a plastic plate of dimensions $100 \times 100 \times 10$ mm and an embedded tube of 12 mm internal diameter for the insertion of the Vaisala probe. The plate was fixed to the surface of concrete by blu tack mass. The area of specimen surface covered with RH measurement device was approximately 80 cm^2 . The distance between the plate surface and the specimen surface was 3 mm and the volume of air in the measuring chamber was about 24 cm³. The ratio of the volume of the measuring chamber to the test area of concrete specimen is 0.30 cm and it is close to the ratio of 0.25 cm that is characteristic when using the Vaisala instrument in a hole of 16 mm diameter, according to the manufacturer guidelines. In comparison to the surface RH test described in [16], the increased surface of concrete specimen covered with RH measurement and the reduced volume of the measuring chamber improve the precision of concrete RH representation and reduce the effect of external air access during the assembly/removal of the probe.

The continuous monitoring of the surface RH of the specimen during the stabilization process was applied. It allows for a precise determination of time needed to reach the assumed level of RH alignment in the specimen volume. It has been assumed that the stabilization of RH continues until the RH difference between the surface and 30 mm below the surface is less than 5%. If the stabilization time was 1.5 times longer than the drying period, the difference limit in RH was increased to 10%.

Drying of concrete specimens in fixed temperature of 65 °C was conducted in a laboratory thermostatic chamber with a forced air flow. The relative humidity of air inside the thermostatic chamber was below 10%. Before start of drying the RH measurements in concrete specimens at different depths were made. During the drying process RH was recorded in weekly intervals. Before the weekly RH measurements the specimens were cooled down in the laboratory for 24 h to the temperature of 20 ± 2 °C.

At the time of achieving the target RH below 65% in concrete at a depth of 30 mm from the surface the drying was terminated. After cooling to room temperature of 20 ± 2 °C the specimens were tightly wrapped in three layers of aluminium foil and additional layer of stretch film. The humidity stabilization process in the specimens was carried out in a laboratory at the air temperature of 20 ± 2 °C and RH $50 \pm 10\%$. After API measurements in stabilized moisture state, the specimens were dried to a constant mass at a temperature of 105 °C. Measurements of the API in heavyweight concrete were carried out in an antural RH state, after RH stabilization period and after drying at 105 °C.

3 Test results

3.1 Results of measurement of RH distribution in concrete

The evolution of RH distribution in the specimen B during concrete drying and RH stabilization period is shown in Figs. 2 and 3. The data obtained at three locations are presented assuming the symmetrical drying conditions at two ends of cylindrical specimens.

During the drying period, a rapid reduction of RH in the concrete surface layer by about 30% can be seen, followed by a gradual decrease of RH in the remaining part of the specimen. During the moisture stabilization period it can be observed that the rate of RH change in different specimen layers is well correlated with RH gradients. With larger RH differences in the initial stabilization period, the movement of moisture is much faster than in the later period when the gradients are lower.

Figure 4 shows the distribution of RH in specimens B and T49 before the drying period, just after the





Fig. 1 The set of devices for RH measurement during concrete drying and moisture stabilization: \mathbf{a} RH measurement at the specimen surface, \mathbf{b} set of tubes at prescribed locations for insertion of Vaisala probes

drying and after the moisture stabilization period. It can be seen that after the full procedure of specimen conditioning, the RH decreased evenly by approximately 25% across the specimen.

3.2 API measurement results

Figure 5 shows the air permeability index of concrete specimens from the top and the bottom of columns A



Fig. 2 Change of the RH distribution in the specimen B during the drying period at the temperature $65 \text{ }^{\circ}\text{C}$



Fig. 3 Change of the RH distribution in the specimen B during the moisture stabilization period

and B and from the massive blocks. The average values and the standard deviation of 4 measurements are shown for each heavyweight concrete series. The data were obtained at natural RH (approx. 90%), after the moisture stabilization at the level of RH 60 \pm 5% and after the oven drying at 105 °C. For both columns a higher air permeability was observed in the upper parts than in the lower parts of the column. Such a difference at the state of stabilized RH was 31.5% for





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Fig. 4 RH distribution in the specimen before drying (natural state), after drying and after stabilization—the specimens B and T49

column A and 21.2% for column B. After oven drying at 105 °C such differences were 10.4 and 39.9%, respectively. In the case of massive concrete blocks, similar API values were obtained in both elements with CEM II cement. The air permeability index of concrete specimens in the block manufactured using CEM I 52.5R cement was much higher. Such an increase was 136.8 and 113.2% compared to the blocks T50 and T51 at the stabilized RH. After oven drying at 105 °C the air permeability index of the **Fig. 5** Air permeability index for concrete specimens cored from columns (a comparison of the top and bottom part of the column) and massive blocks (effects of the type of cement used)



specimens increased by about 20% in respect to the RH stabilized state, i.e. from 19.3% for T49 specimens to 21.9% for T51 specimens.

Evaluation of air permeability of concrete on the basis of API was performed for the state of stabilized RH. The quality of concrete in specimens from the lower part of the column A was evaluated as "very good", and in the remaining specimens from the columns and massive blocks as "good". If such a classification was performed on the basis of API after oven drying specimens at 105 °C, the quality of concrete in all specimens would be rated "good".

4 Analysis and discussion of results

4.1 Evaluation of air permeability through shielding concrete

Basheer [32] presented the criteria of concrete classification based on API results. The criteria are established for concrete specimens dried at a temperature of 105 °C. The concrete quality evaluation on the basis of Autoclam test was presented in [33]. The API tests were performed on containment walls of a nuclear reactor. Two structures made of pre-stressed concrete were investigated. The reactor was a part of a power plant built in 1997 in southern China. The API results allowed to classify the concrete quality as good and very good. The air permeability index in one of the structures was in the range from 0.05 to $0.17 \ln(\text{mbar})/\text{min}$, in the other one from 0.04 to $0.15 \ln(\text{mbar})/\text{min}$. The evaluation of the concrete quality could be seriously affected by omitting the effects of relative humidity of concrete and possible effects of carbonation.

The air permeability data obtained in the current investigation after RH stabilization were similar to results above, except T49 concrete specimens, characterized by much higher air permeability. The observed systematic difference of API between the lower and the upper part of the column (Fig. 5) can be associated with a better compaction of lower layers. The difference is more pronounced for a higher w/c ratio and a higher slump. Because of higher density of aggregates and higher w/c ratio in the column B, a certain degree of segregation could be possible. However no significant aggregate grain segregation was observed on the cut and polished sections of core specimens. The systematic difference of API of concrete in the massive blocks can be associated with certain degree of thermally inducted microcracking. Because of specific mould isolation the temperature field developed was favourable to enhance cracking in the case of cement of a high specific surface area and a high 2-days strength.

When comparing the air permeability test data with those obtained for the laboratory specimens made of shielding concrete with magnetite and barite [16], the following observations can be made. The API of concrete in the column B is significantly higher than in the lab-made concrete specimens of similar composition but 23% lower *w/c* ratio; the difference amounted to 45.9 and 21.1% in the upper part and in the lower part of column B, respectively. The air permeability index of concrete in the upper part of column A was very similar to the API of laboratory concrete B16 [0.129 and 0.130 ln(mbar)/min], while the API in the lower part of column A was 24.6% lower when compared to the result of laboratory concrete B16. The similar concrete mix behave as less air permeable when manufactured at an industrial scale, in particular when cast at the bottom of the column.

4.2 Calculation of moisture diffusion coefficient

Prediction of movement of moisture in porous media such as concrete is a complex matter, because the cementitious materials are known to have a wide range of pore sizes [34]. The pore dimensions, if assumed to be cylindrical, vary from radiuses 10^{-10} m (gel pores) to radiuses 10^{-2} m (air voids/capillary pores) [35]. The complex microstructure of pores is associated with their connectivity [36]. Depending on the pore size, the moisture movement takes place by diffusion, laminar flow and free molecular diffusion (Knudsen diffusion). In the case of greater RH when a part of the capillary system is filled with water there is an additional capillary transport. For the experimental determination of the moisture transport in concrete, it is usual to adopt simplified models in which one diffusion factor is used. Researchers point out that the diffusion coefficient is dependent on the RH of concrete [28, 37–39].

Currently, the model proposed by Bažant and Najjar [28], adopted in Model Code 2010 is in common use [40–42]. It embraces a specific model for the corresponding diffusivity coefficient D_h . The corresponding field equation is presented in Eq. 1.

$$\partial h/\partial t = \operatorname{div} D_h \times \operatorname{grad}(\mathrm{RH})$$
 (1)

where D_h (cm²/day) is the diffusion coefficient (dependent on RH of concrete); RH is the relative humidity of concrete (%) (defined as the relative humidity (RH) of the gaseous phase in equilibrium with the interstitial liquid phase in the pore network of the material [43]) and *t* is time (days).

For the diffusion coefficient in isothermal conditions, it can be expressed as a function of the pore relative humidity 0 < RH < 1

$$D_{h} = D_{1} \left[\alpha + \frac{1 - \alpha}{1 + \left[(1 - \text{RH}) / (1 - \text{RH}_{C}) \right]^{n}} \right]$$
(2)

where D_1 (cm²/day) is the maximum value of D_h for RH = 1; D_0 (cm²/day) is the minimum D_h for RH = 0, $\alpha = D_0/D_1$, RH_c the relative pore humidity at D_h (RH) = 0.5 D_1 and *n* is an exponent. Three important parameters in the formula: α (= 0.05), RH_c (= 0.80) and *n* (= 15) are arbitrary assumed constants, given in MC2010 [44]. Assuming that in the RH range below 75% (and this is in our specimens), the relative humidity effect on the diffusivity coefficient is minimal. In our calculations we adopted the modified parameters values: $\alpha = 0.10$ and RH_c = 0.65. Simplified calculations with a constant *D* coefficient in the range of RH 20–75% were also performed.

$$\partial h/\partial t = D \times \operatorname{grad}(\mathrm{RH})$$
 (3)

when calculating the D coefficient, a one-directional distribution and movement of moisture and constant temperature 20 °C were assumed. It was assumed that the distribution and flow of moisture in the specimen is symmetric with respect to the plane passing through the center of the specimen, parallel to its unprotected sides. Calculations were made for the half of a specimen. The least squares method was used to determine the moisture distribution function, in the form of a polynomial of 4th degree, at the beginning and the end of the stabilization of RH (Fig. 4). An iteration number is set equal to the number of days corresponding to the moisture stabilization period in the specimen. The half of the specimen was divided into eight slices of 10 mm thickness. For each slice, the RH was calculated before and after stabilization. The RH gradients were calculated on each day between the individual slices $grad(RH)_{n,day} = RH_{n,-}$ $_{day}$ -RH_{*n*-1,day} (*n* from 2 to 8; day from 0 to the number of stabilization days-1, in this case day = 0.21). In each iteration a further moisture distribution was calculated assuming that the moisture flowed from the element of higher RH to the neighbouring one.

$$n = 1 \qquad \qquad \mathbf{RH}_{n=1}, \, \mathrm{day} + 1 = \mathbf{RH}_{n(=1),\mathrm{day}} \\ + D_* \mathrm{grad}(\mathbf{RH})_{n+1(=2),\mathrm{day}} \\ n = 2 \,\mathrm{do} \, 7 \qquad \mathbf{RH}_{n,\mathrm{day}+1} = \mathbf{RH}_{n,\mathrm{day}} \\ + D_* \mathrm{grad}(\mathbf{RH})_{n+1,\mathrm{day}} - D_* \mathrm{grad}(\mathbf{RH})_{n,\mathrm{day}} \\ \end{cases}$$



$$n = 8 \qquad \text{RH}_{n=8,\text{day}+1} = \text{RH}_{n(=8),\text{day}}$$
$$-D_* \text{grad}(\text{RH})_{n(=8),\text{day}}$$

The *D* coefficient was determined, minimizing the sum of the squared differences of the RH values after the stabilization determined from the matched function to the post-stabilization measurement (RH_{stab}) and the iteratively calculated (RH distribution day 22). Calculations were made using Microsoft Office Solver. An example of calculation of *D* shown in Table 6.

The calculation of D_1 was carried out in the similar way, however, taking into account the effect of RH on the result, using the formulas Eqs. 1 and 2. An iteration number was equal to the number of days corresponding to the moisture stabilization period. The D_1 coefficient was determined using the RH values after the stabilization, determined from the matched function and the post-stabilization measurements. The sum of squared differences between the above mentioned values was minimized in an iterative procedure. Calculations were also made using Microsoft Office Solver.

4.3 Comparison of moisture diffusion coefficients

A large compliance was found between the moisture diffusion coefficients determined on the basis of RH measurements and the distribution functions obtained from the iterations. The sum of squares of the difference in experimental and calculated values was from 0.8 in series B to 43.8 in series T51. The moisture diffusion coefficients D and D_1 are presented in Table 7. The maximum RH values and RH differences between the measured values in the 75 mm hole and the concrete surface, prior to the start of moisture stabilization in the specimens were also given. The D_1 coefficient is approximately $10 \times$ higher than D. In the RH range of 20–75%, which occurs at the beginning of moisture stabilization, the impact of the maximum RH and RH gradient on the D_1/D ratio is small. This ratio is largely influenced by the assumed coefficient α . The difference in moisture diffusion coefficients of the concrete in A and B specimens was pronounced. The D coefficient for concrete A (w/c = 0.48) was 0.094 cm²/day. For concrete B (w/c = 0.63), the D coefficient was 315% higher. Evaluation of concrete quality A and B, based on the API and D, is incompatible. The API differentiation in these

concretes (Fig. 5) was much lower. In the case of concrete specimens T49, T50 and T51, the API differentiation is larger (about $2\times$ the difference between the concrete T49 with CEM I 52.5R, and T50, T51 concrete with CEM II), however, differences of *D* coefficient are greater (more than $4\times$). The lowest value of *D* coefficient occurred in the concrete with CEM II/B-V 32.5R. For concrete with CEM II/B-S 32.5R and CEM I 52.5R, the *D* coefficients were 39 and 320% higher respectively. The *D* coefficient better reflects the different quality of concrete resulting from a different w/c ratio and probable microcracks than the API.

5 Conclusions

The performed investigation on radiation shielding concrete cast in structural elements resulted in the following conclusions:

The mix design for heavyweight concrete of bulk density $3168-3317 \text{ kg/m}^3$ was developed using barite and magnetite aggregate and cements blended with fly ash and blastfurnace slag. The use of CEM II/B-V and CEM II/B-S cements and *w/c* ratio of 0.5 resulted in the concrete compressive strength of 48–50 MPa at 28 days and its significant increase at the age of about 2 years, up to 72–77 MPa.

An original way of measuring the RH distribution in core specimens from concrete structural elements was developed, including both measurements inside of a specimen and on its surface. The method was used to determine the RH distribution in specimens subjected to accelerated, unidirectional drying at 65 °C and to observe changes in the RH distribution during storage of the specimens in sealed conditions.

The developed procedure for specimens conditioning to achieve the target RH using the surface measurement during moisture stabilization period allowed the specimen preparation time to be minimized. It was ensured by precisely determining the moment of decrease of the RH difference between the surface and the interior of the specimen to the assumed value.

The air permeability index determined on specimens with stabilized RH = $60 \pm 5\%$ showed a difference in the permeability of bottom and top part of the 4 m columns: the upper part of the columns

Table 6 Method of D coefficient calculation

			_		
Solver	variable	cell:	D =	0.39	

Slice number	1	2	3	4	5	6	7	8
RH _{init} day 0	27.3	44.6	56.3	63.8	68.3	70.8	71.9	72.2
grad(RH _{init}) day 0		17.3	11.7	7.5	4.5	2.5	1.1	0.3
RH distribution day 1	34.1	42.4	54.7	62.7	67.5	70.3	71.6	72.1
grad(RH) day 1		8.4	12.3	8.0	4.9	2.7	1.3	0.5
RH distribution day 2	37.3	44.0	53.0	61.5	66.7	69.7	71.3	71.9
grad(RH) day 2		6.6	9.1	8.4	5.2	3.0	1.6	0.6
RH distribution day 3	39.9	44.9	52.8	60.2	65.8	69.1	70.9	71.7
grad(RH) day 3		5.0	7.9	7.4	5.6	3.3	1.8	0.7
RH distribution day 4	41.9	46.0	52.6	59.5	64.9	68.5	70.5	71.4
grad(RH) day 4		4.2	6.6	6.9	5.4	3.6	2.0	0.9
RH distribution day 5	43.5	47.0	52.7	58.9	64.2	67.9	70.1	71.0
grad(RH) day 5		3.5	5.8	6.2	5.3	3.7	2.2	1.0
RH distribution day 6	44.8	47.9	52.9	58.6	63.6	67.3	69.6	70.7
grad(RH) day 6		3.0	5.0	5.7	5.0	3.7	2.3	1.1
RH distribution day 7	46.0	48.6	53.1	58.3	63.1	66.8	69.1	70.2
grad(RH) day 7		2.6	4.5	5.2	4.8	3.7	2.4	1.1
RH distribution day 8	47.0	49.4	53.4	58.2	62.7	66.2	68.6	69.8
grad(RH) day 8		2.3	4.0	4.8	4.5	3.6	2.4	1.2
RH distribution day 9	48.0	50.0	53.7	58.1	62.3	65.8	68.2	69.3
grad(RH) day 9		2.1	3.7	4.4	4.2	3.5	2.4	1.2
RH distribution day 10	48.8	50.6	54.0	58.0	62.0	65.4	67.7	68.9
grad(RH) day 10		1.9	3.3	4.0	4.0	3.3	2.3	1.2
RH distribution day 11	49.5	51.2	54.2	58.0	61.8	65.0	67.2	68.4
grad(RH) day 11		1.7	3.0	3.7	3.8	3.2	2.3	1.2
RH distribution day 12	50.2	51.7	54.5	58.0	61.5	64.6	66.8	68.0
grad(RH) day 12		1.6	2.8	3.5	3.5	3.1	2.2	1.2
RH distribution day 13	50.8	52.2	54.8	58.0	61.4	64.3	66.4	67.5
grad(RH) day 13		1.4	2.6	3.2	3.3	2.9	2.1	1.1
RH distribution day 14	51.3	52.7	55.0	58.1	61.2	64.0	66.0	67.1
grad(RH) day 14		1.3	2.4	3.0	3.1	2.8	2.0	1.1
RH distribution day 15	51.8	53.1	55.3	58.1	61.1	63.7	65.6	66.7
grad(RH) day 15		1.2	2.2	2.8	2.9	2.6	1.9	1.0
RH distribution day 16	52.3	53.5	55.5	58.2	60.9	63.4	65.3	66.3
grad(RH) day 16		1.1	2.1	2.6	2.8	2.5	1.9	1.0
RH distribution day 17	52.8	53.8	55.7	58.2	60.8	63.2	64.9	65.9
grad(RH) day 17		1.1	1.9	2.5	2.6	2.4	1.8	0.9
RH distribution day 18	53.2	54.2	56.0	58.3	60.7	62.9	64.6	65.5
grad(RH) day 18		1.0	1.8	2.3	2.5	2.2	1.7	0.9
RH distribution day 19	53.6	54.5	56.2	58.3	60.6	62.7	64.3	65.2
grad(RH) day 19		0.9	1.7	2.2	2.3	2.1	1.6	0.8
RH distribution day 20	53.9	54.8	56.3	58.4	60.5	62.5	64.0	64.8
grad(RH) day 20		0.9	1.6	2.0	2.2	2.0	1.5	0.8
RH distribution day 21	54.3	55.1	56.5	58.4	60.5	62.3	63.7	64.5



Table 6 continued

Solver variable cell: $D = 0.39$								
Slice number	1	2	3	4	5	6	7	8
grad(RH) day 21		0.8	1.5	1.9	2.0	1.9	1.4	0.8
RH distribution day 22	54.6	55.3	56.7	58.5	60.4	62.2	63.5	64.2
RH _{stab}	54.0	55.0	56.6	58.4	60.2	61.8	63.1	63.9
[(RH distribution day 22)-RH _{stab}] ²	0.3	0.1	0.0	0.0	0.0	0.1	0.2	0.1
Solver target cell: sum of [(RH distrib	ution day 22	$2)-RH_{stab}]^2$						0.8

The example—concrete specimens from column B

Table 7 Calculated moisture diffusion	Concrete ID	$D (\text{cm}^2/\text{day})$	$D_1 \text{ (cm}^2/\text{day)}$	D_1/D	Max RH (%)	RH difference (%)
coefficients D and D_1	A	0.094	0.938	9.98	65.2	45.4
	В	0.390	3.895	9.99	73.0	45.7
	T49	0.470	4.717	10.04	69.9	44.0
	T50	0.112	0.935	8.35	76.5	55.0
	T51	0.156	1.417	9.08	74.7	48.3

exhibited a greater air permeability than the bottom part by about 20–40%.

The concrete quality evaluation based on the air permeability index API, determined on specimens with uniform distribution of RH = $60 \pm 5\%$ and after drying at 105 °C, was dependent on the location of the core in element and the mix design; the concrete mixes were qualified from "very good" to "good".

A moisture diffusion model in heavyweight concrete during the stage of equalization of RH distribution in concrete specimens, developed using Microsoft Office Solver, allowed for estimation of the moisture diffusion coefficients D and D_1 .

The evaluation of concrete quality, based on the API and D coefficient, is found incompatible. The D coefficient reflects in a better way the different quality of concrete resulting from a different w/c ratio and probable microcracks.

The air permeability testing on cores from massive blocks revealed significant differences in API due to the change of cement composition: more than 100% increase was found for CEM I 52.5R in comparison with CEM II 32.5R. That could support a relationship with possible microcracking induced by high thermal gradients.

Acknowledgements The financial support from the National Center for Research and Development in Poland is gratefully

acknowledged (Project PBSII/A2/15/2014 "Durability and efficiency of concrete shields against ionizing radiation in nuclear power structures").

Compliance with ethical standards

Conflict of interest The authors declare that they have no conflict of interest.

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