RILEM TECHNICAL COMMITTEE



Recommendation of RILEM TC 237-SIB on complex Poisson's ratio characterization of bituminous mixtures

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Abstract This recommendation describes how to characterize the isotropic three-dimensional linear viscoelastic behaviour of bituminous mixtures through the simultaneous measurement of the complex Young's modulus (E^*) and the complex Poisson's ratio (v^*). The guidelines given herein are based on the results of a RILEM round robin test organized by the RILEM Technical Committee 237-SIB "Testing and characterization of sustainable innovative bituminous

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materials and systems" and focus on the testing procedure, measurement setup, data analysis and presentation of results. Indications for the preparation of a tests report are also given.

Keywords Complex Young's modulus · Complex Poisson's ratio · Three-dimensional characterization · Linear viscoelasticity · Bituminous mixture

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Fig. 1 Axial test on a cylindrical specimen: a identification of stress and strain principal directions; b time-domain representation of stress and strain sinusoidal signals

1 Scope

This recommendation gives guidance for the characterisation of the three-dimensional (3D) linear viscoelastic (LVE) behaviour of bituminous mixtures considered as isotropic. Specifically, it refers to the simultaneous measurement of the complex Young's modulus (E^*) and the complex Poisson's ratio (v^*) by means of sinusoidal axial tests on cylindrical specimens.

The recommendations are based on the results of a RILEM round robin test (RRRT) organized by the RILEM Technical Committee 237-SIB "Testing and characterization of sustainable innovative bituminous materials and systems". This document contains guidelines on testing procedure, measurement setup, data analysis and presentation of results. Additional details on the results of the RRRT may be found in Perraton et al. [1] and Graziani et al. [2].

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2 Definition of complex Young's modulus and Poisson's ratio

Let us consider a cylindrical specimen of an isotropic, linear viscoelastic (LVE) material subjected only to a steady-state sinusoidal loading in axial direction (Fig. 1a). Although the stress state is uniaxial $[\sigma_1(t) \neq 0, \sigma_2(t) = \sigma_3(t) = 0]$, the response strain field is tree-dimensional and is characterized by two independent strains: $\varepsilon_1(t)$ and $\varepsilon_2(t) = \varepsilon_3(t)$. Hence, the steady-state stress–strain response of the material can be described by the following complex exponentials (or phasors):

$$\sigma_1^*(\omega) = \sigma_{01} \exp[\mathbf{j}(\omega t + \varphi_1)] \tag{1}$$

$$\varepsilon_1^*(\omega) = \varepsilon_{01} \exp(j\omega t) \tag{2}$$

$$\varepsilon_2^*(\omega) = \varepsilon_{02} \exp[j(\omega t + \varphi_2)] \tag{3}$$

where j is the imaginary unit, ω is the angular frequency, σ_{01} is the stress amplitude, ε_{01} and ε_{02} are the amplitudes of axial and transverse strain, respectively, and φ_1 and φ_2 are phase angles. Since phase shifts between phasors actually represent time shifts between the corresponding time domain signals $(\varphi_i = \omega \Delta t_i), \varphi_1$ and φ_2 represent the time shifts of $\sigma_1(t)$ and $\varepsilon_2(t)$ with respect to $\varepsilon_1(t)$, which was customarily assumed as the reference signal (Fig. 1b).

The complex Young's modulus and the complex Poisson's ratio are defined as follows [3]:

$$E^*(\omega) = \frac{\sigma_1^*(\omega)}{\varepsilon_1^*(\omega)} = \frac{\sigma_{01}}{\varepsilon_{01}} \exp(j\varphi_E)$$
(4)

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$$v^{*}(\omega) = -\frac{\varepsilon_{2}^{*}(\omega)}{\varepsilon_{1}^{*}(\omega)} = \frac{\varepsilon_{02}}{\varepsilon_{01}} \exp(j\varphi_{v})$$
(5)

where $|E^*| = E_0 = \sigma_{01}/\varepsilon_{01}$, $|v^*| = v_0 = \varepsilon_{02}/\varepsilon_{01}$ are the norms (or absolute values) and $\varphi_E = \varphi_1$, $\varphi_v = \varphi_2 - \pi$ are the phase angles. The complex quantities described by Eqs. 1–5 are depicted in Fig. 2.

It is also possible to use the following notations:

$$E^*(\omega) = E_1(\omega) + jE_2(\omega) \tag{6}$$

$$v^*(\omega) = v_1(\omega) + jv_2(\omega) \tag{7}$$

where E_1 , E_2 are the real and imaginary parts of the complex Young's modulus, also called storage modulus and loss modulus, respectively, whereas v_1 , v_2 are the real and imaginary parts of the complex Poisson's ratio.

For an isotropic material, the following relations for the description of the 3D LVE behaviour are also valid:

$$K^* = \frac{E^*}{3(1-2\nu^*)} \tag{8}$$

$$G^* = \frac{E^*}{2(1+\nu^*)}$$
(9)

where K^* is the complex bulk modulus and G^* is the complex shear modulus. It has been remarked that the practical applications of Eqs. 8 and 9, requires that the source functions be determined simultaneously on the same specimen, in order to guarantee identical initial and boundary conditions [4].

3 Simultaneous measurement of complex Young's modulus and complex Poisson's ratio

It is recommended that the simultaneous measurement of E^* and v^* of bituminous mixtures is carried out by means of sinusoidal axial tests on cylindrical specimen. The general test setup should be based on those currently adopted for the measurement of E^* [5, 6]. Measurement of the transverse (either diametral or circumferential) strain is also required in order to calculate v^* and obtain a 3D isotropic characterization. Such a test configuration provides homogeneous stress and strain fields in the central part of the specimen, which allows the calculation of v^* through the direct comparison of axial and transverse strains according to Eq. 5.

Although for bituminous mixtures the phase angle of v^* is very small, generally less than 10°, its determination is highly recommended. Assuming $\varphi_v = 0$ (i.e. assuming axial contraction/dilation is in counterphase with transverse contraction/dilation) may lead to inconsistencies in the description of the 3D response. For example, from Eqs. 8 and 9 it would follow that bituminous mixtures have the same loss angle in bulk and shear deformation modes. In addition Poisson's ratio value would be real and constant.

3.1 Specimen preparation

Cylindrical specimens should be prepared following accepted standards for complex Young's modulus testing. It is remarked that specimens prepared with

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different compaction equipment (e.g. gyratory compactor, slab compactor) or cored in different directions relative to the compaction direction, may show a different degree of anisotropy in the LVE response. Hence, it is recommended to clearly report the compaction method, the coring direction and the direction(s) used for the measurement of transverse strain.

3.2 Small strain domain

The simultaneous measurement of E^* and v^* of bituminous mixtures shall be carried out within the LVE domain. For bituminous mixtures this requires the application of "small" axial strain amplitudes, generally lower than 100×10^{-6} m/m. It is remarked that such a linearity limit was established based solely on the measurement of E^* [7–9] and therefore linearity tests should be performed in case of doubt.

It is worth noting that the selection of such a low value for the axial strain amplitude ε_{01} has practical consequences on the transverse strain amplitude ε_{02} occurring during the test. For example, if the Poisson's ratio norm is $v_0 = 0.2$, the transverse strain amplitude will be in the order of 10×10^{-6} m/m. This should be considered when selecting the transverse strain measuring system.

3.3 Testing modality

It is recommended to apply a sinusoidal, i.e. tension/compression (TC) loading history. An haversine loading history, i.e. cyclic compression (CC) or cyclic tension, may also be applied. In the latter case, only the sinusoidal component of time-domain excitation and response functions shall be analysed to calculate both E^* and v^* [10].

Testing may be carried out either in strain or stress controlled mode. In the latter case the axial stress amplitude σ_{01} shall be set to obtain the target steady-state strain amplitude ε_{01} .

It is to be underlined that due to rather low applied frequencies (less than about 10 Hz) inertia effects are negligible. The considered tests are quasi-static cyclic tests and should not be called "dynamic tests" as sometimes stated. Dynamic tests considering back analysis from waves propagating in the specimen can also be used to obtain E^* and v^* [11–13].



3.4 The steady-state

The calculation of frequency-domain material LVE functions should be made during steady-state regime. From a practical point of view, a minimum number of loading cycles should be applied in order to allow the progressive fading away of transient effects due to initial rest conditions. Two to three cycles seems enough to obtain this regime [14]. On the other hand, the number of loading cycles should be limited, so that heating and damage due to repeated loading is limited [9, 15] and, for CC testing, hardening (or softening) due to creep deformation is negligible.

Generally the number of loading cycles applied should be selected with some judgment, considering test temperature and frequency. Moreover, evolution of the material response during the test should be carefully checked.

3.5 Testing temperature and frequency

Similar to complex Young's modulus testing, the range of testing temperature and frequency shall consider potentiality and limitations of available laboratory equipment.

Generally, the sinusoidal excitation is produced using a closed-loop control system, therefore it is recommended to check the quality of the sinusoidal excitation, either stress or strain, applied to the specimen. Hence, the data acquisition system should give access to the raw (unprocessed) values of stress and strain.

3.6 Stress and strain measurement systems

Measurement of axial stress and strain should be carried out following accepted standards for complex Young's modulus testing.

It is recommended to measure axial and transverse strain locally on the specimen. In particular, transverse strain should be measured at mid-height of the specimen using traditional glued strain gauges or non-contact sensors. It is remarked that in the first case an average circumferential strain is measured, whereas in the second case a localized diametral strain is detected. It is also recommended to use a unique data acquisition unit, in order to obtain perfectly synchronized data and avoid systematic errors in the measurement of phase lags. Given the small amplitude of the transverse strain (Sect. 3.2), high accuracy and precision of the strain measuring system is mandatory.

3.7 Temperature control and measurement

Similar to complex Young's modulus measurements, the use of a suitable thermal chamber to control the temperature of the specimen during the test is recommended. Temperature readings should be performed using probes installed on the specimen surface, e.g. platinum resistance thermometers (PT100) or K-type thermocouples. Temperature sensors should be adequately coated in order to avoid fluctuation due to air temperature variations.

When strain is measured using strain gauges, adequate temperature compensation circuits should be used. This normally requires the use a dummy specimen placed inside the thermal chamber.

3.8 Calculation of E^* and v^*

The calculation of E^* and v^* should be carried out, for each testing temperature and frequency, through the direct application of Eqs. 4 and 5. It is recommended to determine the source parameters ($\sigma_{01}, \varepsilon_{01}\varepsilon_{02}, \phi_1, \phi_2$) by performing a sinusoidal regression analysis of the measured discrete-time signals (stress and strains).

Due to the small value of the transverse strain and because of the small phase lag between axial and transverse strain, additional uncertainties due to the numerical regression procedure may have a significant

Fig. 3 Example complex Poisson's ratio measurements on asphalt concrete with continuous grading curve: **a** Black diagram; **b** Cole–Cole diagram. *L* (*H*) indicates the domain with lower (higher) temperatures

3.9 Cole–Cole and Black diagrams for v^*

Similar to the current practice for E^* , Black and Cole– Cole diagrams are a very simple and practical way to plot and analyse v^* values. Different from E^* , the absolute value of v^* should be plotted on a linear scale. If v^* values can be represented by a unique curve in the Black or Cole–Cole diagrams, the time–temperature superposition principle can be considered valid.

As an example, data measured within the RRRT on two different mixtures are reported in Fig. 3 (asphalt concrete with continuous grading curve) and Fig. 4 (asphalt concrete with gap-graded curve). Values measured at lower temperatures are situated in the areas indicated with "L", whereas values measured at higher temperatures gradually plot towards the areas indicated with "H". The plotted results clearly show that the upper limit of the norm of v^* is not necessarily 0.5, as commonly assumed.

3.10 Master curves for v^*

Master curves for v^* components $(v_0, \varphi_v, v_1 \text{ and } v_2)$ can be obtained following the same procedures normally adopted for E^* . Upon selection of a reference temperature the measured values at all other test temperatures are shifted along the log-frequency axis until a unique curve is obtained. If the time-





Fig. 5 Master curves of the

components of complex

Poisson's ratio: a norm;

b phase angle



temperature superposition principle is valid, the same shift factors may be used for all v^* components.

Example master curves of v_0 and φ_v obtained within the RRRT are reported in Fig. 5. It can be noted that master curves of v_0 are not monotonic and that master curves of φ_v show a change of sign. The same shift factors were obtained for E^* and v^* as already stated by various authors [16–19].

3.11 Precision of testing

Results of the RRRT were not conclusive regarding repeatability and reproducibility of E^* and v^* values. However, the data plotted in Figs. 3, 4 and 5 may give an indication of the variability of v^* measured according to the present recommendation. In the RRRT the chosen axial strain level was 50×10^{-6} m/m, thus a variation of about 0.02 for the Poisson's ratio norm corresponded to a variation of 10^{-6} m/m in



the diametral or circumferential strain. For specimens with diameter of 100 mm, this corresponded to a change in diameter or approximately 0.10×10^{-3} mm or a change in circumference of about 0.31×10^{-3} mm. Clearly both the resolution and the precision of the measurement chain, as well as the accuracy of regression analysis are crucial in order to obtain good repeatability and reproducibility.

4 Concluding remarks

Sinusoidal axial tests on cylindrical specimens allow the simultaneous measurement of the complex Young's modulus (E^*) and the complex Poisson's ratio (v^*) and thus can be used to characterize the isotropic 3D LVE behaviour of bituminous mixtures.

According to the present recommendation, the test report should contain:

- The relevant mixture and specimen details, e.g. mixture type, compaction method, specimen dimensions, coring direction;
- The description of the test setup, including at least: load measuring system, axial and transverse strain measuring system, data acquisition frequency;
- The values of the following testing variables: temperature, loading frequency, number of loading cycles (for each temperature and frequency), target axial strain amplitude;
- The numerical technique adopted to calculate the sinusoidal stress and strain amplitudes and phase angles (Eqs. 1–3);
- The calculated values of the complex material functions E* and v*, expressed both in trigonometric form (Eqs. 4, 5) and algebraic form (Eqs. 6, 7) and the corresponding graphical representation in the Black and Cole–Cole diagrams;
- The graphical representation of norm and phase angle of E^* and v^* as a function of reduced frequency (master curves).

Compliance with ethical standards

Conflict of interest The authors declare that they have no conflict of interest.

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