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# Beneficial laggards: multilevel selection, cooperative polymorphism and division of labour in Threshold Public Good Games

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## Abstract

**Background:** The origin and stability of cooperation is a hot topic in social and behavioural sciences.

A complicated conundrum exists as defectors have an advantage over cooperators, whenever cooperation is costly so consequently, not cooperating pays off. In addition, the discovery that humans and some animal populations, such as lions, are polymorphic, where cooperators and defectors stably live together – while defectors are not being punished–, is even more puzzling. Here we offer a novel explanation based on a Threshold Public Good Game (PGG) that includes the interaction of individual and group level selection, where individuals can contribute to multiple collective actions, in our model group hunting and group defense.

**Results:** Our results show that there are polymorphic equilibria in Threshold PGGs; that multi-level selection does not select for the most cooperators per group but selects those close to the optimum number of cooperators (in terms of the Threshold PGG). In particular for medium cost values division of labour evolves within the group with regard to the two types of cooperative actions (hunting vs. defense). Moreover we show evidence that spatial population structure promotes cooperation in multiple PGGs. We also demonstrate that these results apply for a wide range of non-linear benefit function types.

**Conclusions:** We demonstrate that cooperation can be stable in Threshold PGG, even when the proportion of so called free riders is high in the population. A fundamentally new mechanism is proposed how laggards, individuals that have a high tendency to defect during one specific group action can actually contribute to the fitness of the group, by playing part in an optimal resource allocation in Threshold Public Good Games. In general, our results show that acknowledging a multilevel selection process will open up novel explanations for collective actions.

## Background

The intriguing phenomenon of cooperation has fascinated experimental and theoretical researchers for decades, as it is essential for understanding the complexity of life, and life itself [1-5]. A dilemma derives from the fact that selfish individuals have an advantage over those who act cooperatively, by which we mean a costly act that can benefit others [1,6,7]. Although selfish ‘defectors’ interacting with their own kind have a lower ‘pay-off’ than cooperators, defectors would eventually totally replace cooperators in the population [8]. However a

wide variety cooperative behaviour can be observed in nature [7,9]. Moreover, it is a common observation that humans [10-12] and some animal populations such as lions (*Panthera leo*) [13,14] are polymorphic. Individuals that have a high tendency to cooperate live together with those that have a high tendency to defect. The proportion of these ‘laggards’ can be high in certain societies and they are not being punished, as in the case of lions [14] or in a number of human hunter-gatherer societies [11,15]. Observations suggest that the average tendency for cooperation in these populations appears to be stable in the long term. This is a perplexing set of observations, not yet fully understood. Existing explanations rely either on the snowdrift game [16,17] with homogeneous population structure, punishment [18], or spatially explicit population structure [19]. None of

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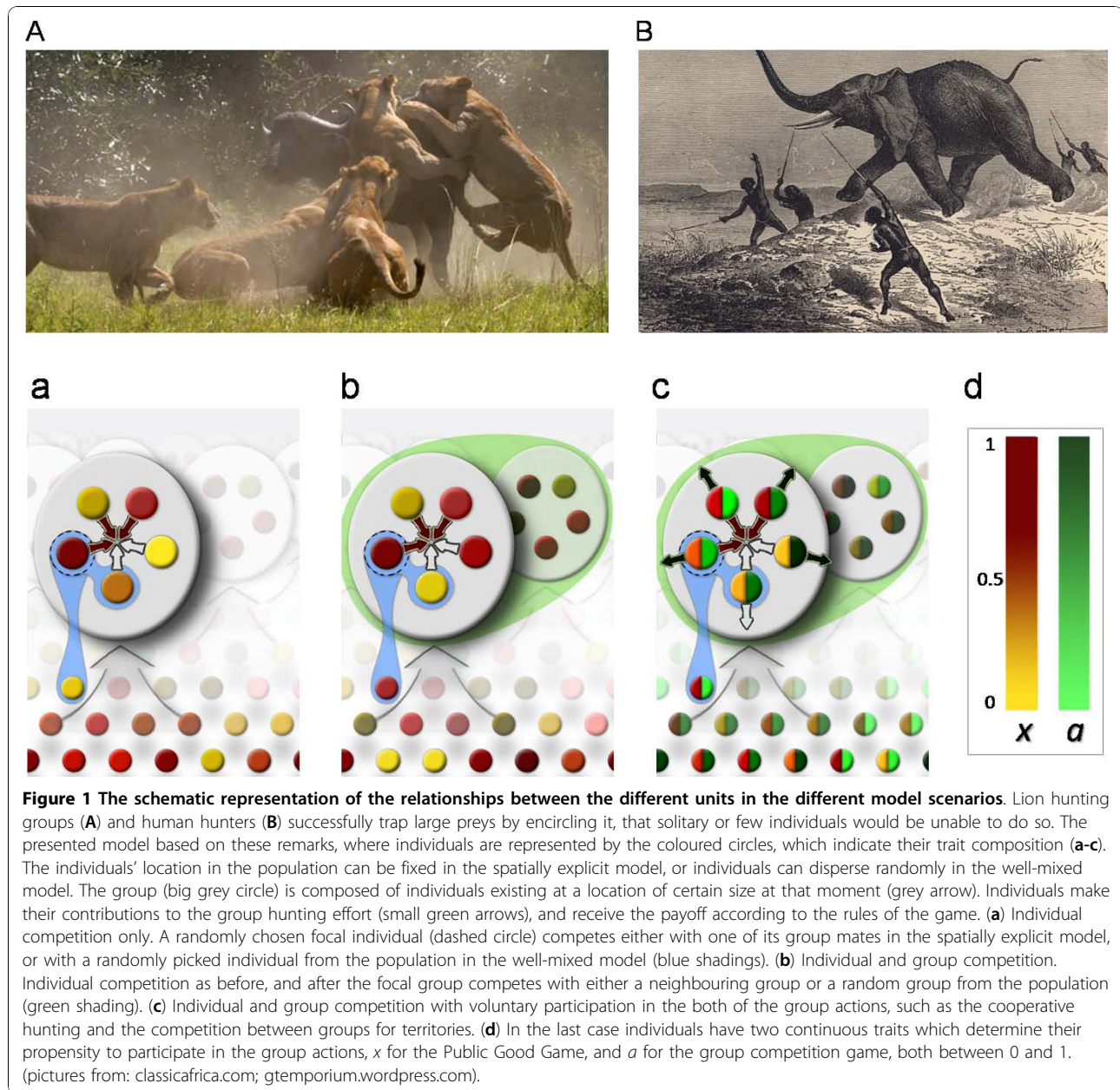
these explanations can be applied perfectly here as for example lion and human populations are neither completely well-mixed, nor spatially explicit in a sense as sedentary organisms, and punishment is also not common in these instances.

Majority of the current evolutionary game theoretical studies that shed light on the mechanism behind many cooperative phenomena in biological systems concentrated on pair-wise interactions between individuals [3,6-8,10,16,20][but see for e.g. [21]]. Arguably numerous examples of group interactions found in nature however can be described as  $n$ -person games [22-25,21], in which more than two 'players' interact with each other at the same time in the form of group actions [26-30]. During group interactions individuals typically invest into common goods or common goals [31]. In most of the cases this is available for everyone, that is the common good is non-monopolizable (or non-excludable, non-exclusive) and non-rival (synonym of joint in supply, non-diminishable) [32-35]. This raises a collective action problem, where non cooperators, often termed as free riders, can reap the benefit of the common good without investing into it [24,34,35].

In many cases of a collective action the achieving the group goal, for example capturing prey depends on the number of encircling hunters [36,37], and not necessarily on their individual efforts (Figure 1). During numerous instances of cooperative hunting several individuals simply fill the position of blocking, diverting, flushing the prey. This threshold effect is documented for cooperative hunting situations in various social carnivores including lions [36,37], African wild dogs (*Lycaon pictus*) [38-40], chimpanzees (*Pan troglodytes*) [41], Harris' Hawks (*Parabuteo unicinctus*) [42] and humans [43,44]. For example when lions are hunting small prey, each lion pursues its own animal. However with larger, faster or more difficult prey [45] the cooperation of a group of hunters is needed to encircle, split the herd, to spot, surround and kill the animal [36,37,46]. In order to make the hunt successful several lions have to work together (about 4-7) [36,37,47,48], get close to the prey before starting the attack (30-50 m) [36,37,46,49] and cut off its escape routes by encircling the prey from different points and filling the roles of "centers" and "wings" [36,37]. Below a threshold group size it is not only hard to capture the prey but to defend it against hyenas [50]. Chimpanzees [41,51] or wild dogs [39] sometimes use similar encircling tactics. Harris' Hawks either perform surprise attacks on lagomorphs from different directions, or use flush-and-ambush tactics to capture hidden prey [42]. Some other bird species also hunt cooperatively larger prey, such as Brown-necked Raven (*Corvus ruficollis*) on Egyptian Mastigure (*Uromastix aegyptius*), in which case two birds fill the tasks

of blocking the escape routes of the prey while several others attack it from several directions, always performing the direct attack on the most exposed part of the lizard [52]. Many sea mammal species, such as killer whales (*Orcinus orca*), humpback whales (*Megaptera novaengliae*), bottlenose dolphins (*Tursiops truncatus*) and spotted dolphins (*Stenella frontalis*) chase school of fish into a tight ball, sometimes driving it into a rock or to the water surface with coordinated group action, some performing tail slaps, creating a curtain of air around the fish ball or performing feeding bouts [27,53-56]. Moreover some whales may use their acoustic "trumpets" creating a "wall sound" combined with the bubble net, as recently suggested by Leighton and colleagues, to trap the fish inside the curtain [57]. Cooperative hunting in human hunter-gatherers societies has been common, as coordinated action of several hunters was necessary to chase larger preys into a natural trap and to hunt them down (consider for example the buffalo jump sites) [58,59]. There are numerous examples of threshold effects in the operation of modern human societies and in economics [60]. Take as an example the requirement of a minimum number of hunters on the boat during traditional whale hunting [44] or the necessity of collective mass for successful employee strikes [61,62]. Finally, threshold effects in group cooperation can appear not only in human and animal hunting societies. There are well documented examples of a lower group size threshold in some cooperatively breeding species [40,63,64]. Evidence from microbial cooperation suggests, that in some cases a threshold number of cooperators, that is bacteria which produce extracellular chemical components, is crucial in producing a public good [65,66]. Also, at the dawn of life the first protocells were most probably composed of cooperative elements, RNA molecules, which could have controlled the metabolism of the protocell acting like enzymes, and the complete metabolism most probably required the cooperation of sufficient number of elements, or at least the elements of an autocatalytic core [5,67].

Models of Public Good Game nicely capture the main features all of the above described cooperative phenomena. But the traditionally used linear benefit return function is insufficient in capturing the threshold effect for the optimal number of individuals that is necessary to perform the given group action, as close to the threshold joining one or few more cooperators disproportionately increases the success of the group action [43,68,69]. So instead a nonlinear return paradigm is more appropriate [68,70-72], such as in the  $n$ -player Threshold Public Good Game [71]. In this version of the Public Good Game (PGG) a successful cooperative effort is achieved only if the number of cooperating individuals reaches a given threshold, just like in the above



described situations. Different levels of cooperation can be evolutionary stable outcome in such games, depending on the cost of cooperation, and the proportion of initial cooperative decisions in the population [71].

While these situations assume that groups of individuals engage in an interaction which may or may not end in successful cooperation these groups themselves often compete with each other [35]. For example, in one of the most studied group behavioural biological systems lioness form a pack to hunt together yet they are in direct competition with other lion packs with which they share common borders [13,14,47,73,74]. The same holds for all group hunting territorial species from

hyenas through whales, African wild dogs to humans [75-78].

Here we study the interaction of selection acting on the level of individuals engaged in a threshold PGG and selection acting on these groups while competing for territories. Thus, our model differs from previous models of TPGGs [71,72] and that of multi-level selection [77] by explicitly integrating these two components. We do so first by giving analytical solutions for the evolutionarily stable level of cooperation for various group sizes and threshold levels at first assuming only individual selection; then by studying the interaction of individual and group level selection with a series of computer

simulations validated by the numeric results. We study 3 basic setups in the computer simulations: (i) individual selection only (Figure 1.a), (ii) group selection only, (for comparison), and (iii) the combination of both, in which case first we assume that (iii/a) all individuals are obliged to participate in group defense (Figure 1.b), then we relax this assumption by allowing (iii/b) voluntary participation (Figure 1.c). Individual selection in our model allows individuals to compare their success with other individuals, or compete for resources, while group selection based on the idea that stronger groups may outcompete weaker ones by overtaking their territories. The structure of the game is described in the Methods section.

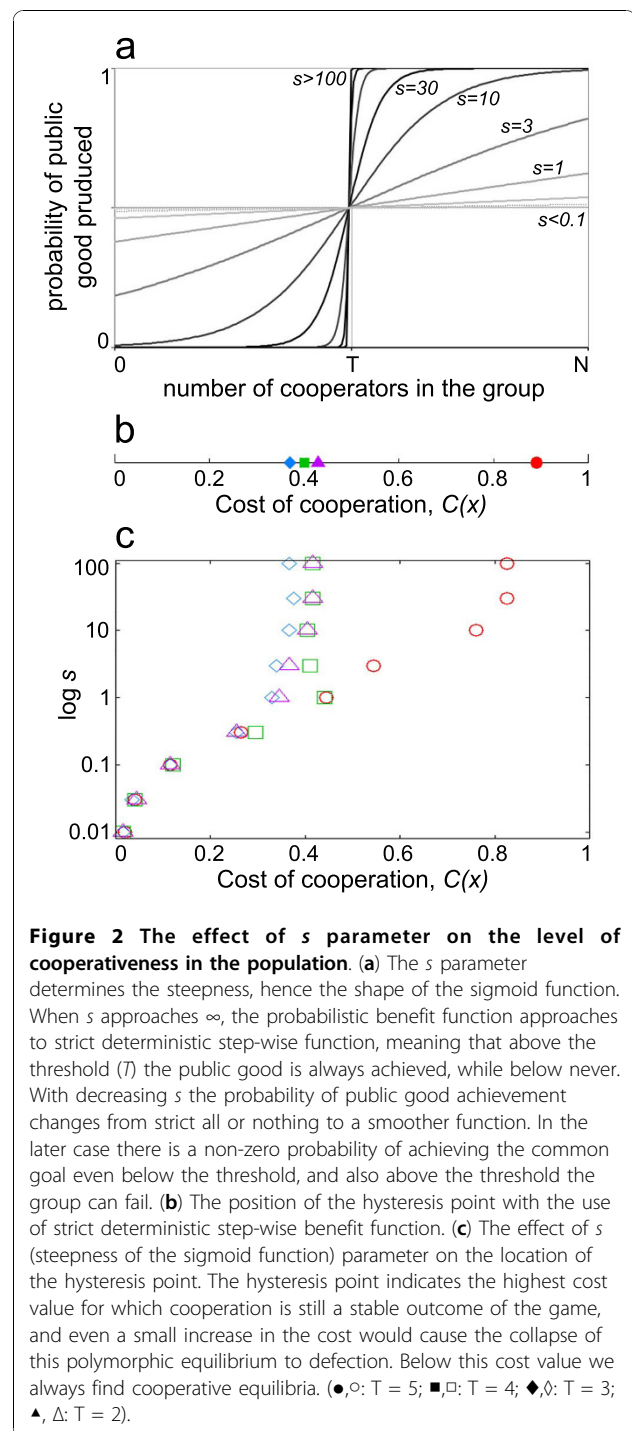
## Results

### Effect of different threshold functions

First we study the effect of the benefit function shape on the level of cooperation in the population (Figure 2) by means of IBM simulations (see Methods). For this we substitute the threshold benefit function with a sigmoid function ( $s$ -shape function), which gives the probability of achieving the group goal, that is receiving the benefit for different levels of cooperative effort. A good indicator of the cooperativeness in the system is the position of the hysteresis point [71], which above the proportion of cooperators drops to zero in all cases. Below the hysteresis point, we always find a stable level of cooperation, while if the cost of cooperation moves above the hysteresis point the population rapidly evolves to zero cooperativeness. The positions of the hysteresis points for different threshold values assuming sigmoid functions (Figure 2.a) don't change significantly for a wide range of  $s$  parameter (steepness of the benefit function). For high values of  $s$  ( $1 < s < 100$ ), the hysteresis point appears at the same cost values ( $C(x)$ ) for cases  $T \neq N$  (Figure 2.c), as with the strict deterministic step-wise function (Figure 2.b). For  $T = n$ , this parameter range is narrow ( $10 < s$ ), and a slight change in the steepness of the benefit function results in major changes in the cooperative equilibrium. Our results indicate that the dynamics of the system remains the same for relatively steep sigmoid functions than for a step-wise function. In the following we will use the later one in our simulations.

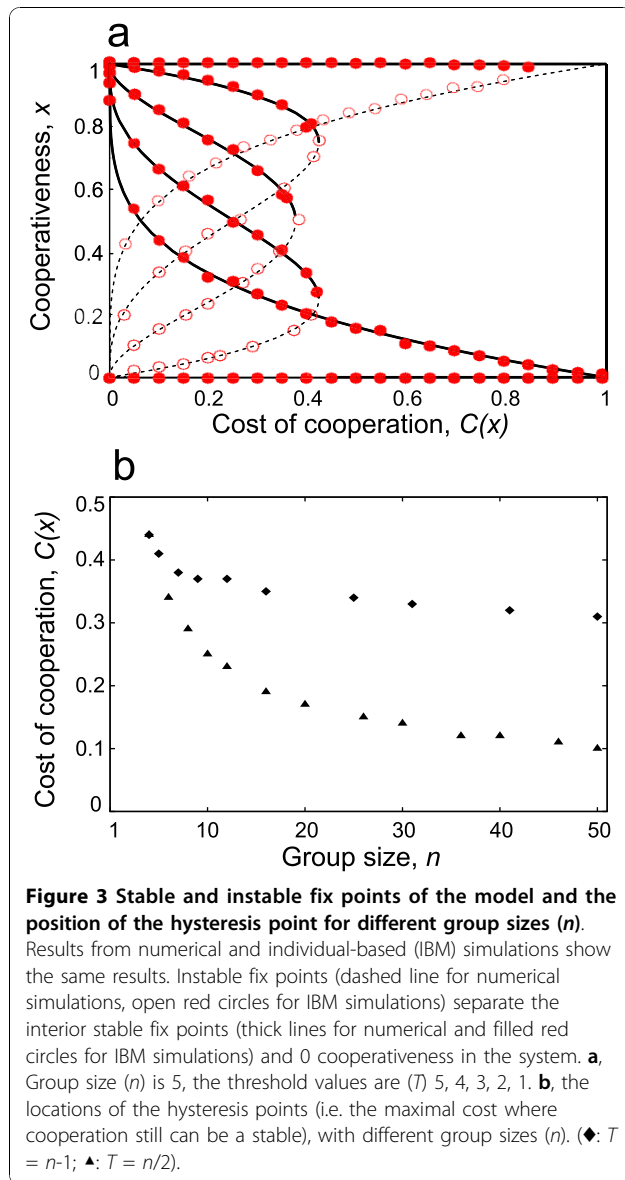
### Results for individual level selection

Next we employ the method described in Bach *et al.* 2006 [71] to find the stable and instable equilibria of the model for individual selection only (see Figure 1.a; further details in the Methods). We also run a series of simulations in our individual based model (IBM) for comparison with the analytical model (i.e. to "calibrate" the IBM simulations). The equilibrium level of cooperation depends both on the size of the group ( $n$ ) and on



the threshold level ( $T$ ) (Figure 3). Figure 3.a depicts the resulting fixed points of the system for given group size and for increasing  $T$ , from the analytical model (solid curves for stable and dashed curves for instable fix points), and from individual based simulations (dots), which show a close fit. The higher the threshold value the higher is the ratio of cooperators at a given group





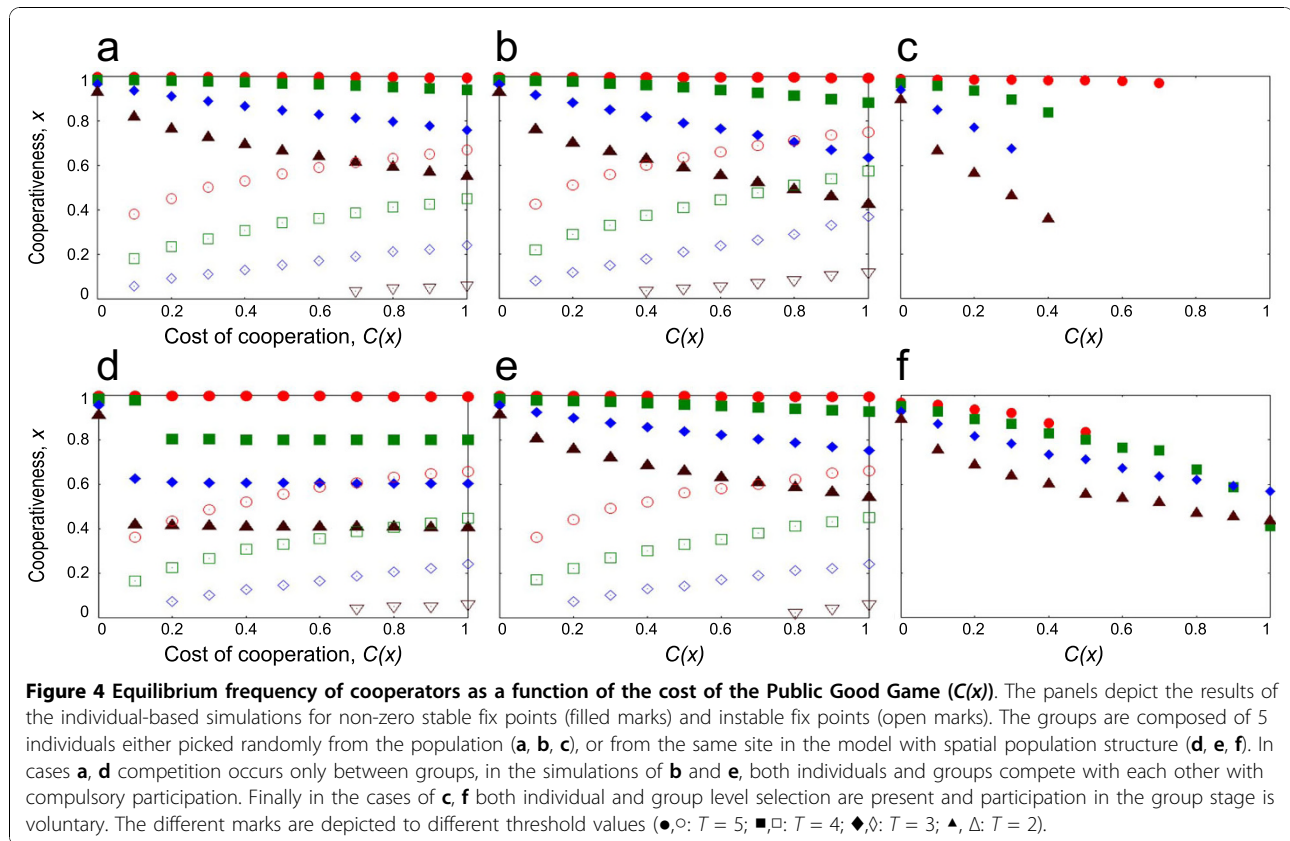
size (Figure 3.a). Not surprisingly the highest level of cooperation can be achieved when the threshold value equals the size of the group, and for small group sizes, the average level of cooperation is higher (Figure 3.b). The unstable fix points separate the attractors of the interior stable fixed points of cooperation from the attractors of zero cooperativeness (Figure 3.a). Above the separatrix, cooperation prevails, below this boundary, cooperation diminishes. All results from IBM model show a perfect fit for the predictions of the analytical model.

### Introducing multilevel selection

In the following we explore the individual based model with well-mixed and spatial population structure. In the

first step, we introduce group level selection to the individual based model (see Figure 1.b) keeping the participation in the group defense compulsory. Figure 4 depicts the cases of only group selection (a,d), and the combination of group and individual selection when group defense is compulsory (b,e). The most striking effect of introducing group level selection is that the hysteresis effect disappears in all cases. In the well-mixed case (Figure 4.a) the level of cooperation is higher than without group selection, however, aside from the case  $T = n$ , the population is still polymorphic. It means that groups with higher number of cooperators do not necessarily enjoy a competitive advantage. Groups in general respond in proportional manner to the threshold value, i.e. they optimize resource allocation. This can be best seen from the spatially explicit simulation with only group selection (Figure 4.d) as in this case the average equilibrium level of cooperation is exactly the threshold level. This implies that any deviation from the optimal group composition results in a disadvantage for the group, not only if the number of defectors is higher, but also if the ratio of cooperators and defectors differs from the optimal in any ways (i.e. groups that optimize their allocation this way have higher fitness than groups that do not, see for further details in Additional file 1 figures from S.3 to S.4). Introducing individual level selection decreases the level of cooperation in the well-mixed case (Figure 4.b vs. 4. a), however interestingly and somewhat counter intuitively it increases the level of cooperation in the spatially explicit case (Figure 4.e vs. 4.d). Equilibrium populations are still polymorphic aside the case  $T = n$ . Figure 4.c and 4.f depicts the case when participation at the group competition stage is voluntary. When group defense is cost-free ( $C(a) = 0$ ) the level of cooperation in the Public Goods Game is the same as in the previous cases (result not shown). When group defense is costly ( $C(a) = 1$ ) then the level of cooperation in the PGG is lower (Figure 4.c and 4.f) and the hysteresis effect reappears in the well-mixed case (Figure 4.c), but not in the spatially explicit model (Figure 4.f). Note, however, that when cooperation is present the polymorphic nature of the equilibria is preserved (aside  $T = n$  in the wellmixed model), that is, resource allocation is still optimized, groups with higher number of cooperators do not win out by default.

Finally Figure 5 depicts the results as a function of the two kinds of costs and the initial number of the cooperators in the PGG when both the participation in the hunt and in the group defense is voluntary (see Figure 1.c). We can observe four types of dynamics in our simulations (Figure 5.a-d). If the costs of cooperation ( $C(x)$ ,  $C(a)$ ) are high, individual willingness to cooperate evolves to zero (Figure 5.a). Individuals willingly



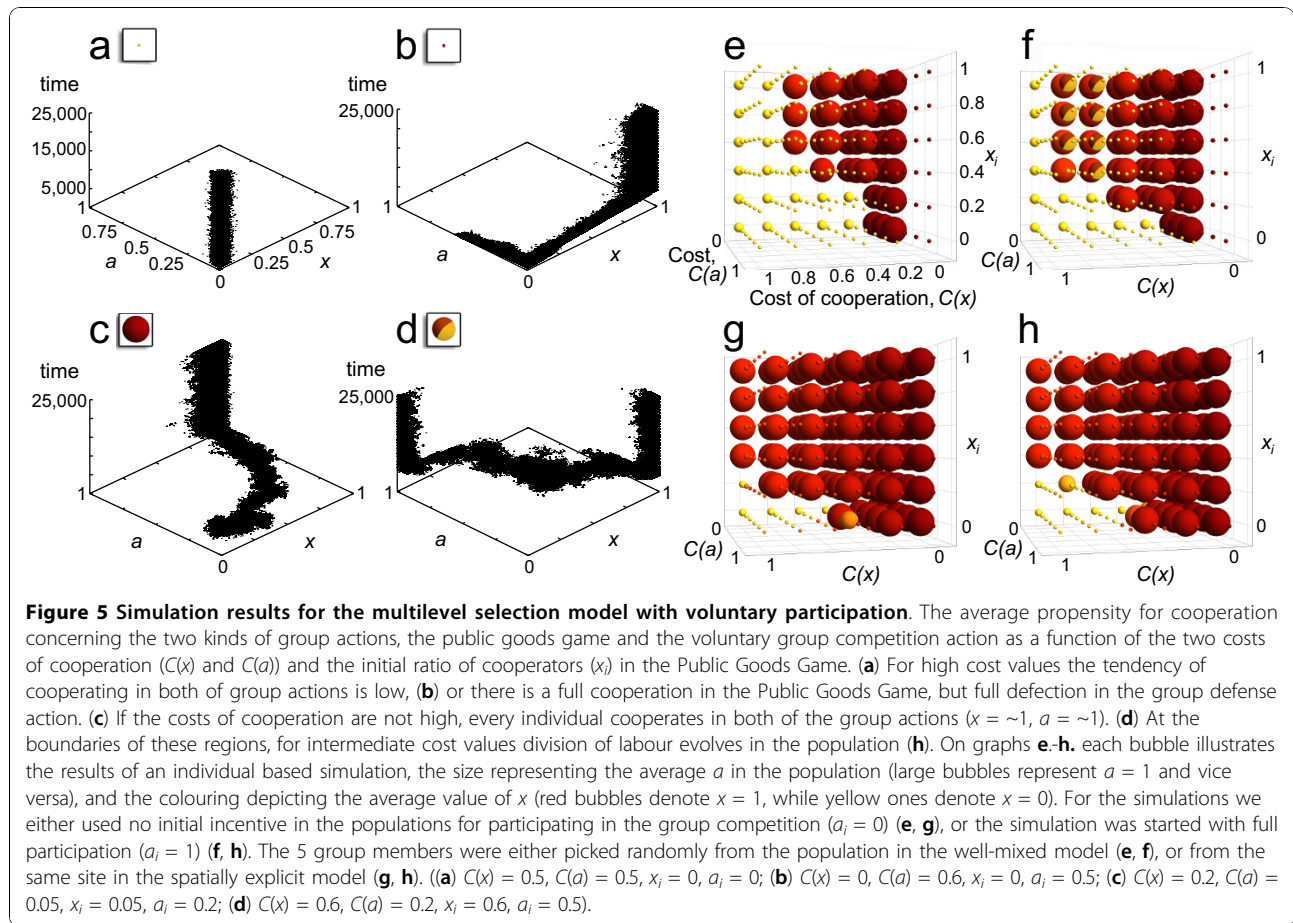
cooperate in group defense (i.e. large bubbles, that is high values of  $a$ , close to 1) only if there are high levels of cooperation with regard of group hunting (i.e. the colours of the large bubbles ranges from orange to red ( $\sim 0.7-1$ ) on Figure 5.e-h, Figure 5.c). However, cooperation in the Public Goods Game can stay at high levels even if the propensity to participate in group defense is low (i.e. there are small red bubbles when the cost of group defense is high) (Figure 5.b). Polymorphism of different cooperative efforts in the Public Goods Game is still present at many of the equilibria (i.e. lighter shade of red), and interestingly division of labour evolves at medium values of costs in the well-mixed case (Figure 5.f red/yellow bubbles). In these cases, polymorphism occurs on the population level, where individuals cooperate strictly in one of the collective actions, but never both (Figure 5.d).

Our results also indicate, in line with the general conclusion of previous models that spatial structure favours cooperation [6,8,19,79], as high values of cooperation evolve for both public actions (hunting and group defense, see large red bubbles) even at high cost values (Figure 5.g and 5.h). We observe division of labour in the spatially explicit model only under given circumstances (see Additional file 1 for further details), which suggests that this outcome is unstable in these cases

with small group size. Note that when  $C(x) > 0$  cooperation evolves only if the initial proportion of cooperation is not zero in the population with well-mixed structure, which indicates a separatrix in the system. However, spatial population structure promotes cooperation and it allows cooperators to invade at higher cost values with regard of both types of costs (i.e. compare 5.e with 5.g and 5.f with 5.h).

## Discussion

Here we show that multilevel selection in threshold PGG can maintain stable levels of polymorphism (i.e. a stable mixture of cooperators and defectors) without the need of punishment or spatially explicit population structure. We give a primary demonstration that the described dynamics holds not only for step-wise benefit function (strict threshold function), but for a wide range of sigmoid curves between the step-wise and the linear benefit functions (s-shape function). Our results further indicate that polymorphism in group hunting and defense can be adaptive in case of multilevel selection, and to our knowledge, we provide a pioneer report on the division of labour in multiple Public Good Games. We conclude that what was regarded as cheating at the individual level is in fact can play a significant part in the optimization at the group level, which optimization



is provided by the described mechanisms working on behavioural polymorphism.

Many of the collective actions produce goods that are non monopolizable, meaning that no one can be excluded from benefiting [33-35], thus free riders can exploit this collective good without paying the cost of production [28]. Threshold effects in Public Good Games can provide an often neglected, yet powerful explanation for the observed polymorphism in the population, as an alternative to punishment [18], spatial structure [19] or various payoff functions [16,17].

Population level polymorphism is a stable outcome in Threshold Public Good Games, where cooperators and free riders stably live together in the population [71,72], as long as the cost of cooperation doesn't exceed a limit cost value, the hysteresis point. Our model predicts that for an increased group size this hysteresis, that is a sudden drop from cooperation to defection, appears at lower cost values, compared to smaller groups (see Figure 3.b). To put it in a different way, with large groups cooperation can be maintained only if the cost of cooperation is relatively low. Also for higher cost values the instable fix points move closer to the stable fix points,

which means that the invasion of cooperators in a population of defectors becomes harder, while the invasion of defectors into a cooperative population becomes more likely.

Introducing multilevel selection into the model is a logical step towards reality, as in many biological and human examples where collective hunting occurs inter-group conflicts can be also observed [35,74-77]. When group level competition introduced explicitly into the model population level polymorphism is stabilized both in well-mixed and spatially explicit populations. Thus, multilevel selection need not select for the groups with the highest number of cooperators as it is often assumed. Groups that optimize the number of hunters enjoy an advantage over those groups that hunt (cooperate) on a higher, unnecessary level. Thus, defection of a given proportion of individuals during one specific cooperative group action can be an adaptive strategy for the group depending on the cost values. Because group level performance (i.e. success in the PGG) determines both individual and group level success any deviation from the optimal group composition would cause a disadvantage in some way or other. If the number of

cooperators is lower than the threshold value then the collective action (i.e. hunting) is unsuccessful, thus neither cooperators nor defectors gain anything, and these groups are being replaced by successful groups. On the other hand, if the number of cooperators is higher than what is required for providing benefit for the whole group (in our example capturing the prey), the energy loss of unnecessary effort would cause a disadvantage when the group faces a conflict (fight for territory). Hence our novel result is that laggards, who were previously seen as exploiters of the common goods provided by cooperators [13,14], do actually contribute to the fitness of the group by keeping the group level allocation at the optimum level.

Our results also verify that if participation in two distinct collective actions which produce shared benefits is costly, such as hunting and territory defense, then selection pressure on cooperators can result division of labour to evolve, predicting that it will evolve only for a narrow range of cost values. Interestingly, behavioural polymorphism first appears at the individual level, that is all of the individuals participate in both collective actions with intermediate probabilities. However, this state is not stable and evolution drives the system towards division of labour at the population level, where individuals mostly participate only in one of the collective actions (i.e. polymorphism appears at the group level). This result is robust in our simulations at medium cost values, and turns out to be stable on the long term. Experimental support for this context dependent role specialization is poor yet [but see [56,80]], however the idea that cooperators and 'free riders' switch roles in different contexts is not obscure [28,35,56,81,80], as long as there is a trade off situation between two energy consuming group actions [81].

Our model has a simplistic assumption, that individuals have only two heritable traits that describe their behavioural decisions, this two are sufficient for maintaining polymorphism in the population. Obviously regularly many genes effect behaviour, which explains higher polymorphism, still there is evidence suggesting that some may play disproportionately important role in behavioural switches [82]. Accordingly, our model can provide a potential explanation for the observed polymorphism in lions in threshold game like situations [36,37,46] and the presence of laggards in the population [14,83].

The importance of intra group conflict in human evolution seems to gain a new currency [77,78], however since the technology of hunting humans changed a lot in the last 250,000 years (i.e. evolution of spear points, bows, arrows, etc. [84,85]), it is more difficult to evaluate whether a threshold effect existed in hominid plio-pleistocene group hunting. The conception of hunting large preys would inevitably suggest so and the fact that

hunting of medium-sized and large ungulates started long before stone-tipped and bone-tipped weapons were widely used strongly suggests that cooperation amongst hunters was essential for the capture of large games [85]. If it did so, then our model applies and has the potential to explain the observed polymorphism in humans as well. Interesting implication of our results is that once human societies become larger and more fluid in composition this polymorphism was no longer necessarily adaptive and definitely was not looked upon as desirable. This, in turn could have triggered the evolution of cultural norms and institutions that attempts to obtain an universally high level of cooperation from all the members of the society regardless of their predispositions.

## Conclusions

Here we present a multilevel selection model of interdependence in group living species, where cooperation is modelled as an  $n$ -player Threshold Public Good Game and where selection acts both at the individual and at the group level. We have found that the population can evolve into stable levels of cooperative polymorphism, where cooperators and free riders -laggards- can stably live together. Our results indicate: (i) that the described dynamics holds for a wide range of probabilistic sigmoid benefit functions, not only for strict deterministic step-wise function; (ii) that multilevel selection need not select for the highest number of cooperators within groups but instead it may selects for polymorphism depending on the details of the TPGG; (iii) that defectors contribute to the group fitness as much as they help the group to achieve the optimal amount of investment at the group level; (iv) that division of labour might evolve with regard of the participation in the two collective actions for medium cost values of cooperation; (v) and that spatial population structure promotes cooperation in TPGGs.

## Methods

### The game

The structure of the game is as follows: individuals of a group can engage in a cooperative activity (i.e. hunting, resource purchase) where every individual can play two strategies, either to cooperate with probability  $x$  or to defect with probability  $1-x$ . The cooperative players join in the group effort (group size is  $n$ ), and thus pay a fix cost of cooperation ( $c$ ). In contrast, defectors do not pay the cost of the game. If the number of cooperators is equal or above a given threshold value ( $T$ ), then all of the individuals within the group can acquire the benefit ( $b$ ) of cooperation regardless whether they cooperated or not. This derived from the non-rival, non-excludable features of the game [33-35], that is, no individual can be excluded from the acquired benefit of the hunt, and each consumer gains the same proportion without



depleting it. However if the number of cooperators does not reach the necessary number which is required for the successful achievement of the group action then no one gets the benefit, but cooperators still pay the cost. The fitness ( $W$ ) is calculated as the benefit minus the cost of the game.

### Analytical solutions

We use the method described in Bach *et al.* 2006 [71] to find the stable and instable equilibria of the model. According to the Bishop-Cannings theorem [86] strategies supporting a mixed equilibrium need to have the same fitness. Thus, at a mixed equilibrium supported by cooperators and defectors the fitness' of both strategies should be the same. Let us denote the level of cooperativeness in the population as  $x$ , then the fitness of a mutant playing strategy  $y$  can be written as follows for  $n = 3$ ,  $T = 2$  [see [71]]:

$$W(y, x) = rx^2 + y(2rx(1-x) - c) \quad (1)$$

Where  $c$  is the cost of cooperation and  $r$  is the benefit received by all of the individuals if the number of cooperators is equal or above  $T$ . If  $x$  is a Nash equilibrium then the  $W$  should be independent of  $y$  (since any strategy is either cooperator:  $y = 1$  or defector:  $y = 0$ , or any in between should get the same payoff). This condition holds only if the second part of Eq.1. equals zero [71], that is:

$$g(x) = 2rx(1-x) - c = 0 \quad (2)$$

Accordingly there are two solutions for  $x$  [71]:

$$x_1 = \frac{1}{2} + \frac{1}{2} \sqrt{1 - 2\frac{c}{r}}, \quad x_2 = \frac{1}{2} - \frac{1}{2} \sqrt{1 - 2\frac{c}{r}} \quad (3)$$

Evolutionary stability further requires that  $g'(x) < 0$  thus  $x_1$  is an ESS solution while  $x_2$  is an instable equilibrium. This gives the simple bifurcation diagram shown in Figure 1. in Bach *et al.* 2006 [71]. The fitness of a given strategy for any group size and for any threshold number can be written up and the equation equivalent to Eq.2. can be derived accordingly. The following general formulas can be obtained:

$$\begin{aligned} x^{n-1}(r-c) - c(1-x^{n-1}) = 0 \quad \text{if } T = n \\ (r-c) \sum_{i=n-1-j}^{n-1} \binom{n-1}{i} x^i (1-x)^{n-1-i} - c \sum_{i=0}^{n-2-j} \binom{n-1}{i} x^i (1-x)^{n-1-i} \\ - r \sum_{i=n-j}^{n-1} \binom{n-1}{i} x^i (1-x)^{n-1-i} = 0 \quad (4) \\ \text{if } T \neq n, T \neq 1, \text{ where } 1 < j < n-1 \\ r(1-x)^{n-1} - c = 0 \quad \text{if } T = 1 \end{aligned}$$

While analytical solution might not be possible to calculate at large group sizes, numerical solutions can be obtained. Of course, the numerical solutions of this kind will not tell us which points are the stable and which points are the instable [but see ref. [72]]. To check the stability of our fixed points we used an individual based simulation of the model (details see below). The numerical results and the results of the simulations are depicted on Figure 3.

We also substitute the strict deterministic step-wise benefit function with a sigmoid probabilistic function.

$$P = \frac{1}{1 + e^{(-s)^*(cn-T)}} \quad (5)$$

Where  $P$  is the probability that the public goal is reached, which depends on the steepness of the function ( $s$ ), the number of cooperators in the group ( $cn$ ) and the threshold value ( $T$ ).

### Individual based simulation of the model

We model the evolutionary dynamics in a finite size population consisting of  $N_{all}$  individuals (10,000 and 12,500 individuals). We set up two different scenarios in which the population structure is modelled by the two extremes. On the one part individuals have no fixed partners in a well-mixed model. In every time step both the composition of cooperating groups and competition neighbourhoods change ( $n$ , we increase the number of cooperators up to 50 on Figure 3.b), where partners randomly chosen from the entire population, so the interaction environment of the individual is well-mixed. In the case of spatially explicit model individuals occupy the grid points of a regular lattice ( $N \times N = N_{all}$ ), with toroidal boundary conditions, and the focal individual has a constant interaction environment, its immediate neighbourhood. The neighbourhood in both cases defines both the cooperating and the competing group for the focal individual ( $n$ ), which is 4 (von Neumann neighbourhood) group members in the spatially explicit model. The simulations were run for a given number of update steps with asynchronous updating. An update step consists of a game played by the group, individual competition, group competition if occurred (see Figure 1), and mutation.

During competition step, we use a pair-wise comparison update rule [6], which is the finite population analogue of the replicator dynamics (called the *imitate the better*, for further details see Additional file 1), in which an individual adopts the strategy of a randomly chosen neighbour with a probability proportional to the fitness difference, only if this difference is greater than zero.

$$p = \frac{W_{rival} - W_{focal}}{W_{max} - W_{min}}$$

We analyze multiple competition update scenarios (see Additional file 1 for details).

We also model territorial group behavior, in which case groups compete with each other for territories (sites). Groups composed of  $n$  individuals living in the same site. The rivals could be neighbouring groups in the spatial population (Moore neighbourhood, that is 8 closest sites) or groups randomly chosen from the population in the well-mixed case. Groups are compared according to the average group payoffs, and the successful group entirely replaces all members of the loser one. We calculate the average payoff of the group ( $\bar{W}$ ) as the arithmetic average of the payoffs of all group members, that is the participation in the group competition is compulsory.

$$\bar{W} = \frac{\sum_{j=1}^n W_j}{n}$$

The chance for each group to occupy the focal site is given as described above in the competition rules, but using average group payoffs.

Next we introduce voluntary participation in both of the two group actions, and individuals have two continuous, evolving traits. Besides,  $x$  that defines the propensity to cooperate in the PGG, we introduce  $a$ , which describes the individual's propensity to participate in the territorial group defense action. The marginal values are also 0-1. If  $a$  is high, the individual will participate in the group competition with high probability, whereas if it is low or 0, it will never. As the group defense is considered as an act of cooperation here, it involves a cost  $C(a)$  for those who participated. The average group payoff is now calculated as the average of the payoffs of those group members, who participate in the group competition. Groups then compared by their average group payoffs according to the above described competition rules.

To ensure evolution, after the competition steps, mutation can occur in the traits of the focal individuals with the chance 0.01. The mutant's trait is drawn from a normal distribution, with the original trait value as a mean and with a given variance (0.01). The trait can only be between 0 and 1. After individual competition, only the focal individual's traits can mutate, after group competition in all members of the focal group has a chance for mutation to occur with the same probability.

The points on figures were calculated as the average of the last 1 M ( $10^6$ ) update steps of multiple iterated simulation results (for Figure 4 15 and for Figure 5 3 repetitions, with insignificant variation between the repetitions). The length of the simulation was determined by preliminary simulations, that is 1,000 M, 625 M and 312.5 M update steps for Figure 3, 4 and 5 accordingly. Graphs on Figure 5.a-d were obtained by plotting the trait distribution of the population in every 100th update step for 25,000 steps.

## Additional material

**Additional file 1: Supplementary Information.** The file contains additional simulation results and their interpretation. Additional simulations were made with different update rules, different population structure models. Here we also show and analyze some representative time series simulation results. Text and graph files are included.

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## Authors' contributions

GB and SzSz contributed equally to the research and the preparation of the article. GB and SzSz participated in the design of the study and in the analysis and interpretation of the results. SzSz analyzed the analytical model. GB constructed and carried out the analysis of the IBM model. All authors read and approved the final manuscript.

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## References

1. Hamilton WD: **The genetical evolution of social behaviour.** *J Theor Biol* 1964, **7**:1-16.
2. Trivers R: **The evolution of reciprocal altruism.** *Q Rev Biol* 1971, **46**:35-57.
3. Axelrod R, Hamilton WD: **The evolution of cooperation.** *Science* 1981, **211**:1390-1396.
4. Axelrod R: **The Evolution of Cooperation.** New York, NY: Basic Books; 1984.
5. Maynard Smith J, Szathmáry E: **The Major Transitions in Evolution.** Oxford: Freeman & Co; 1995.
6. Doebeli M, Hauert C: **Models of cooperation based on the Prisoner's Dilemma and the Snowdrift game.** *Ecol Lett* 2005, **8**:748-766.
7. Sachs JL, Mueller UG, Wilcox TP, Bull JJ: **The evolution of cooperation.** *Q Rev Biol* 2004, **79**:135-160.
8. Nowak MA: **Five rules for the evolution of cooperation.** *Science* 2006, **314**:1560-1563.
9. Dugatkin LA: **Cooperation among animals: An evolutionary perspective.** New York, NY: Oxford University Press; 1997.

10. Fehr E, Fischbacher U: **Social norms and human cooperation.** *Trends Cog Sci* 2004, **8**:185-190.
11. Marlowe FW: **What explains Hadza food sharing?** In *Socioeconomic Aspects of Human Behavioral Ecology*. Edited by: Alvard M. Greenwich, Conn: JAI Press; 2004:69-88, [Research in Economic Anthropology, vol 23].
12. Gächter S, Herrmann B: **Reciprocity, culture and human cooperation: previous insights and a new cross-cultural experiment.** *Phil Trans Roy Soc B* 2009, **364**:791-806.
13. Scheel D, Packer C: **Group hunting behaviour of lions: a search for cooperation.** *Anim Behav* 1991, **41**:697-709.
14. Heinsohn R, Packer C: **Complex cooperative strategies in group-territorial African lions.** *Science* 1995, **269**:1260-1262.
15. Gurven M: **To give and to give not: The behavioral ecology of human food transfers.** *Behav Brain Sci* 2004, **27**:543-583.
16. Doebeli M, Hauert C, Killingback T: **The evolutionary origin of cooperators and defectors.** *Science* 2004, **306**:859-862.
17. Gore J, Youk H, van Oudenaarden A: **Snowdrift game dynamics and facultative cheating in yeast.** *Nature* 2009, **459**:253-256.
18. Sigmund K, De Silva H, Traulsen A, Hauert C: **Social learning promotes institutions for governing the commons.** *Nature* 2010, **466**:861-863.
19. Nowak MA, May RM: **Evolutionary games and spatial chaos.** *Nature* 1992, **359**:826-829.
20. Nowak MA, Sigmund K: **Evolution of indirect reciprocity.** *Nature* 2005, **437**:1291-1298.
21. Hauert C, Michor F, Nowak MA, Doebeli M: **Synergy and discounting of cooperation in social dilemmas.** *J Theor Biol* 2006, **239**:195-202.
22. Hardin G: **Tragedy of the commons.** *Science* 1968, **162**:1243-1248.
23. Boyd R, Richerson PJ: **The evolution of reciprocity in sizeable groups.** *J Theor Biol* 1988, **132**:337-356.
24. Dugatkin LA: **N-person games and the evolution of co-operation: A model based on predator inspection in fish.** *J Theor Biol* 1990, **142**:123-135.
25. Dugatkin LA, Perlin M, Atlas R: **The evolution of group-beneficial traits in the absence of between-group selection.** *J Theor Biol* 2003, **220**:67-74.
26. Marwell G, Oliver P: **The critical mass in collective action: A micro-social theory.** New York, NY: Cambridge University Press; 1993.
27. Anderson C, Franks NR: **Teams in animal societies.** *Behav Ecol* 2001, **12**:534-540.
28. Nunn CL, Lewis RJ: **Cooperation and collective action in animal behavior.** In *Economics in nature*. Edited by: Noë R, Hammerstein P, van Hooff JARAM. Cambridge: Cambridge University Press; 2001:42-66.
29. Sumpter DJT: **The principles of collective animal behaviour.** *Phil Trans R Soc B* 2006, **361**:5-22.
30. Clutton-Brock T: **Cooperation between non-kin in animal societies.** *Nature* 2009, **462**:51-57.
31. Bergmüller R, Johnstone RA, Russell AF, Bshary R: **Integrating cooperative breeding into theoretical concepts of cooperation.** *Behav Process* 2007, **76**:61-72.
32. Olson M: **The Logic of Collective Action: Public Goods and the Theory of Groups.** Cambridge, MA: Harvard University Press; 1971.
33. Dionisio F, Gordo I: **The tragedy of the commons, the public goods dilemma, and the meaning of rivalry and excludability in evolutionary biology.** *Evol Ecol Res* 2006, **8**:321-332.
34. Nunn CL: **Collective benefits, free riders, and male extragroup conflict.** In *Primate males*. Edited by: Kappeler PM. Cambridge: Cambridge University Press; 2000:192-204.
35. Kitchen DM, Beehner JC: **Factors affecting individual participation in group-level aggression among non-human primates.** *Behaviour* 2007, **144**:1551-1581.
36. Stander PE: **Cooperative hunting in lions: the role of the individual.** *Behav Ecol Sociobiol* 1992, **29**:445-454.
37. Stander PE: **Foraging dynamics of lions in a semi arid environment.** *Can J Zool* 1992, **70**:8-21.
38. Fanshawe JH, Fitzgibbon CD: **Factors influencing the hunting success of an African wild dog pack.** *Anim Behav* 1993, **45**:479-490.
39. Creel S, Creel NM: **Communal hunting and pack size in African wild dogs, *Lycodon pictus*.** *Anim Behav* 1995, **50**:1325-1339.
40. Courchamp F, MacDonald DW: **Crucial importance of pack size in the African wild dog *Lycodon pictus*.** *Anim Cons* 2001, **4**:169-174.
41. Watts DP, Mitani JC: **Hunting behaviour of chimpanzees Ngogo, Kibale National Park, Uganda.** *Intern J Primat* 2002, **23**:1-28.
42. Bednarz JC: **Cooperative hunting Harris' Hawks (*Parabuteo unicinctus*).** *Science* 1988, **239**:1525-1527.
43. Kollock P: **Social dilemmas: the anatomy of cooperation.** *Annu Rev Sociol* 1998, **24**:183-214.
44. Alvard MS, Nolin DA: **Rousseau's whale hunt? Coordination among big-game hunters.** *Curr Antropol* 2002, **43**:533-559.
45. Sinclair ARE, Mduma S, Brashares JS: **Patterns of predation in a diverse predator-prey system.** *Nature* 2003, **425**:288-290.
46. Packer C, Pusey AE: **Divide we fall: Cooperation among lions.** *Sci Am* 1997, **276**:32-39.
47. Packer C, Scheel D, Pusey AE: **Why lions form groups: Food is not enough.** *Am Nat* 1990, **136**:1-19.
48. Funston PJ, Mills MGL, Biggs HC: **Factors affecting the hunting success of male and female lions in the Kruger National Park.** *J Zool* 2001, **253**:419-431.
49. Schaller GB: **The Serengeti lion.** Chicago, IL: University of Chicago Press; 1972.
50. Cooper SM: **Optimal hunting group size: the need for lions to defend their kills against loss to spotted hyenas.** *Afr J Ecol* 1991, **29**:130-136.
51. Boesch C: **Cooperative hunting in wild chimpanzees.** *Anim Behav* 1994, **48**:653-667.
52. Yosef R, Yosef N: **Cooperative hunting in Brown-Necked Raven (*Corvus ruficollis*) on Egyptian mastigure (*Uromastix aegyptius*).** *J Ethol* 2010, **28**:385-388.
53. Fertl D, Würsig B: **Coordinated feeding by Atlantic spotted dolphins (*Stenella frontalis*) in the Gulf of Mexico.** *Aquat Mammal* 1995, **21**:3-5.
54. Connor RC: **Group living in whales and dolphins.** In *Cetacean societies: field studies of whales and dolphins*. Edited by: Mann J, Connor R, Tyack P, Whitehead H. Chicago, IL: University of Chicago Press; 2000:199-218.
55. Nøttestad L, Simila T: **Killer whales attacking schooling fish: why force herring from deep water to the surface?** *Mar Mamma Sci* 2001, **17**:343-352.
56. Gazda SK, Connor RC, Edgar RK: **A division of labour with role specialization in group-hunting bottlenose dolphins (*Tursiops truncatus*) off Cedar Key, Florida.** *Proc Roy Soc Lond B* 2005, **272**:135-140.
57. Leighton TG, Richards SD, White PR: **Trapped within a 'wall of sound'.** *Acoustics Bulletin* 2004, **29**:24-29.
58. Frison GC: **Prehistoric, plains-mountain, large-mammal, communal hunting strategies.** In *The evolution of human hunting*. Edited by: Nitecki MH, Nitecki DV. New York, NY: Plenum Press; 1987:309-421.
59. Frison GC: **Paleoindian large mammal hunters on the plains of North America.** *Proc Natl Acad Sci* 1998, **95**:14576-14583.
60. van de Kragt AJC, Orbell JM, Dawes RM: **The minimal contributing set as a solution to public goods problems.** *Am Pol Sci Rev* 1983, **77**:112-122.
61. Granovetter M: **Threshold models of collective behaviour.** *Am J Sociol* 1978, **83**:1420-1443.
62. Macy MW: **Chains of cooperation: threshold effects in collective action.** *Am Sociol Rev* 1991, **56**:730-747.
63. Woodroffe R, Ginsberg JR, Macdonald DW, IUCN/SSC Canid Specialist Group: **The African wild dog: status survey and conservation action plan.** IUCN, Gland, Switzerland; 1997.
64. Courchamp F, Grenfell B, Clutton-Brock T: **Population dynamics of obligate co-operators.** *Proc R Soc Lond B* 1999, **266**:557-563.
65. Crespi BJ: **The evolution of social behavior in microorganisms.** *Trends Ecol Evol* 2001, **16**:178-183.
66. Czárán T, Hoekstra RF: **Microbial communication, cooperation and cheating: quorum sensing drives the evolution of cooperation in bacteria.** *PLoS One* 2009, **4**:e6655.
67. Szathmáry E: **Coevolution of metabolic networks and membranes: the scenario of progressive sequestration.** *Phil Trans R Soc B* 2007, **362**:1781-1787.
68. Oliver P, Marwell G, Teixeira R: **The theory of the critical mass I. Interdependence, group heterogeneity and the production of collective action.** *Am J Sociol* 1985, **91**:522-556.
69. Ostrom E: **Social dilemmas and human behavior.** In *Economics in nature*. Edited by: Noë R, Hammerstein P, van Hooff JARAM. Cambridge: Cambridge University Press; 2001:23-41.
70. Heckathorn DD: **The dynamics and dilemmas of collective action.** *Am Sociol Rev* 1996, **61**:250-277.
71. Bach LA, Helvik T, Christiansen FB: **The evolution of n-player cooperation-threshold games and ESS bifurcations.** *J Theor Biol* 2006, **238**:426-434.

72. Pacheco JM, Santos FC, Souza MO, Skyrms B: **Evolutionary dynamics of collective action in N-person stag-hunt dilemmas.** *Proc Roy Soc Lond B* 2009, **276**:315-321.
73. Grinnel J: **Modes of cooperation during territorial defense by African lions.** *Human Nature* 2002, **13**:85-104.
74. Mosser A, Packer C: **Group territoriality and the benefits of sociality in the African lion, *Panthera leo*.** *Anim Behav* 2009, **78**:359-370.
75. Wilson ML, Britton NF, Franks NR: **Chimpanzees and the mathematics of battle.** *Proc R Soc Lond B* 2002, **269**:1107-1112.
76. Mitani JC, Watts DP: **Correlates of territorial boundary patrol behaviour in wild chimpanzees.** *Anim Behav* 2005, **70**:1079-1086.
77. Choi J, Bowles S: **The coevolution of parochial altruism and war.** *Science* 2007, **318**:636-640.
78. Bowles S: **Did warfare among ancestral hunter-gatherers affect the evolution of human social behaviours?** *Science* 2009, **324**:1293-1298.
79. Számadó Sz, Szalay F, Scheuring I: **The effect of dispersal and neighbourhood in games of cooperation.** *J Theor Biol* 2008, **253**:221-227.
80. Arnold KE, Owens IPF, Goldizen AW: **Division of labour within cooperatively breeding groups.** *Behaviour* 2005, **142**:1577-1590.
81. Nunn CL, Deane RO: **Patterns of participation and free riding in territorial conflicts among ringtailed lemurs (*Lemur catta*).** *Behav Ecol Sociobiol* 2004, **57**:50-61.
82. McDermott R, Tingley D, Cowden J, Frazzetto G, Johnson DDP: **Monoamine oxidase A gene (MAOA) predicts behavioral aggression following provocation.** *Proc Natl Acad Sci USA* 2009, **106**:2118-2123.
83. Packer C, Heinsohn R: **Lioness Leadership (Reply).** *Science* 1996, **271**:1215-1216.
84. McBrearty S, Brooks AS: **The revolution that wasn't: a new interpretation of the origin of modern human behavior.** *J Hum Evol* 2000, **39**:453-563.
85. Stiner MC: **Carnivory, coevolution, and the geographic spread of the genus.** *Homo J Arch Res* 2002, **10**:1-63.
86. Bishop DT, Cannings C: **A generalized war of attrition.** *J Theor Biol* 1978, **70**:85-124.

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