

Erratum to: Quantum Yang-Mills field theory

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After publication, the author has realized that a couple of indexes were not properly set in the equations for the 1-point function (eqs. (60) and (61)) whose correct version is as follows:

$$\begin{aligned}
 & \partial^2 G_{1\nu}^{(j)a}(x) + g f^{abc} (\partial^\mu G_{2\mu\nu}^{(j)bc}(x, x) + \partial^\mu G_{1\mu}^{(j)b}(x) G_{1\nu}^{(j)c}(x) - \partial_\nu G_{2\mu}^{(j)\mu bc}(x, x) - \partial_\nu G_{1\mu}^{(j)b}(x) G_1^{(j)\mu c}(x)) \\
 & + g f^{abc} \partial^\mu G_{2\mu\nu}^{(j)bc}(x, x) + g f^{abc} \partial^\mu (G_{1\mu}^{(j)b}(x) G_{1\nu}^{(j)c}(x)) \\
 & + g^2 f^{abc} f^{cde} (G_{3\mu\nu}^{(j)\mu bde}(x, x, x) + G_{2\mu\nu}^{(j)bd}(x, x) G_1^{(j)\mu e}(x)) \\
 & + G_{2\nu\rho}^{(j)eb}(x, x) G_1^{(j)\rho d}(x) + G_{2\mu\nu}^{(j)de}(x, x) G_1^{(j)\mu b}(x) \\
 & + G_1^{(j)\mu b}(x) G_{1\mu}^{(j)d}(x) G_{1\nu}^{(j)e}(x) = g f^{abc} (\partial_\nu P_2^{(\varepsilon)bc}(x, x) + \partial_\nu (\bar{P}_1^{(\varepsilon)b}(x) P_1^{(\varepsilon)c}(x))) + j_\nu^a
 \end{aligned} \tag{60}$$

and then, for $j = 0$,

$$\begin{aligned}
 & \partial^2 G_{1\nu}^a(x) + g f^{abc} (\partial^\mu G_{2\mu\nu}^{bc}(0) + \partial^\mu G_{1\mu}^b(x) G_{1\nu}^c(x) - \partial_\nu G_{2\mu}^{\nu bc}(0) - \partial_\nu G_{1\mu}^b(x) G_1^{\mu c}(x)) \\
 & + g f^{abc} \partial^\mu G_{2\mu\nu}^{bc}(0) + g f^{abc} \partial^\mu (G_{1\mu}^b(x) G_{1\nu}^c(x)) \\
 & + g^2 f^{abc} f^{cde} (G_{3\mu\nu}^{\mu bde}(0, 0) + G_{2\mu\nu}^{bd}(0) G_1^{\mu e}(x)) \\
 & + G_{2\nu\rho}^{eb}(0) G_1^{\rho d}(x) + G_{2\mu\nu}^{de}(0) G_1^{\mu b}(x) \\
 & + G_1^{\mu b}(x) G_{1\mu}^d(x) G_{1\nu}^e(x) = g f^{abc} (\partial_\nu P_2^b(0) + \partial_\nu (\bar{P}_1^b(x) P_1^c(x))).
 \end{aligned} \tag{61}$$

This indexes problem was also present in the equations for the 2-point function of the gluon (eqs. (62) and (63)), where a term was also omitted. These should read as follows:

$$\begin{aligned}
 & \partial^2 G_{2\nu\kappa}^{(j)am}(x - y) + g f^{abc} (\partial^\mu G_{3\mu\nu\kappa}^{(j)bcm}(x, x, y) + \partial^\mu G_{2\mu\kappa}^{(j)bm}(x - y) G_{1\nu}^{(j)c}(x) + \partial^\mu G_{1\mu}^{(j)b}(x) G_{2\nu\kappa}^{(j)cm}(x - y) \\
 & - \partial_\nu G_{3\mu\kappa}^{(j)\mu bcm}(x, x, y) - \partial_\nu G_{2\mu\kappa}^{(j)bm}(x - y) G_1^{(j)\mu c}(x) - \partial_\nu G_{1\mu}^{(j)b}(x) G_{2\kappa}^{(j)\mu cm}(x - y)) \\
 & + g f^{abc} \partial^\mu G_{3\mu\nu\kappa}^{(j)bcm}(x, x, y) + g f^{abc} \partial^\mu (G_{2\mu\kappa}^{(j)bm}(x - y) G_{1\nu}^{(j)c}(x)) + g f^{abc} \partial^\mu (G_{1\mu}^{(j)b}(x) G_{2\nu\kappa}^{(j)cm}(x - y)) \\
 & + g^2 f^{abc} f^{cde} (G_{4\mu\nu\kappa}^{(j)\mu bdem}(x, x, x, y) + G_{3\mu\nu\kappa}^{(j)bdm}(x, x, y) G_1^{(j)\mu e}(x) + G_{2\mu\nu}^{(j)bd}(x, x) G_{2\kappa}^{(j)\mu em}(x - y)) \\
 & + G_{3\nu\rho\kappa}^{(j)acm}(x, x, y) G_1^{(j)\rho b}(x) + G_{2\nu\rho}^{(j)eb}(x, x) G_{2\kappa}^{(j)\rho dm}(x - y) + G_{2\nu\rho}^{(j)de}(x, x) G_{2\kappa}^{(j)\rho bm}(x - y) + G_1^{(j)\mu b}(x) G_{3\mu\nu\kappa}^{(j)dem}(x, x, y) \\
 & + G_{2\kappa}^{(j)\mu bm}(x - y) G_{1\mu}^{(j)d}(x) G_{1\nu}^{(j)e}(x) + G_1^{(j)\mu b}(x) G_{2\mu\kappa}^{(j)dm}(x - y) G_{1\nu}^{(j)e}(x) + G_1^{(j)\mu b}(x) G_{1\mu}^{(j)d}(x) G_{2\nu\kappa}^{(j)em}(x - y)) \\
 & = g f^{abc} (\partial_\nu K_{3\kappa}^{(j\varepsilon)bcm}(x, x, y) + \partial_\nu (\bar{P}_1^{(\varepsilon)b}(x) K_{2\kappa}^{(j\varepsilon)cm}(x, y))) + \partial_\nu (\bar{K}_{2\kappa}^{(j\varepsilon)bm}(x, y) P_1^{(\varepsilon)c}(x)) + \delta_{am} g_{\nu\kappa} \delta^4(x - y)
 \end{aligned} \tag{62}$$

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and, for $j = 0$,

$$\begin{aligned}
& \partial^2 G_{2\nu\kappa}^{am}(x-y) + gf^{abc}(\partial^\mu G_{3\mu\nu\kappa}^{bcm}(0, x-y) + \partial^\mu G_{2\mu\kappa}^{bm}(x-y)G_{1\nu}^c(x) + \partial^\mu G_{1\mu}^b(x)G_{2\nu\kappa}^{cm}(x-y) \\
& - \partial_\nu G_{3\mu\kappa}^{\mu bcm}(0, x-y) - \partial_\nu G_{2\mu\kappa}^{bm}(x-y)G_1^{\mu c}(x) - \partial_\nu G_{1\mu}^b(x)G_{2\kappa}^{\mu cm}(x-y)) \\
& + gf^{abc}\partial^\mu G_{3\mu\nu\kappa}^{bcm}(0, x-y) + gf^{abc}\partial^\mu(G_{2\mu\kappa}^{bm}(x-y)G_{1\nu}^c(x)) + gf^{abc}\partial^\mu(G_{1\mu}^b(x)G_{2\nu\kappa}^{cm}(x-y)) \\
& + g^2 f^{abc} f^{cde}(G_{4\mu\nu\kappa}^{\mu bdem}(0, 0, x-y) + G_{3\mu\nu\kappa}^{bdm}(0, x-y)G_1^{\mu e}(x) + G_{2\mu\nu}^{bd}(0)G_{2\kappa}^{\mu em}(x-y) \\
& + G_{3\nu\rho\kappa}^{acm}(0, x-y)G_1^{\rho b}(x) + G_{2\nu\rho}^{eb}(0)G_{2\kappa}^{\rho dm}(x-y) + G_{2\nu\rho}^{de}(0)G_{2\kappa}^{\rho bm}(x-y) + G_1^{\mu b}(x)G_{3\mu\nu\kappa}^{dem}(0, x-y) \\
& + G_{2\kappa}^{\mu bm}(x-y)G_{1\mu}^d(x)G_{1\nu}^e(x) + G_1^{\mu b}(x)G_{2\mu\kappa}^{dm}(x-y)G_{1\nu}^e(x) + G_1^{\mu b}(x)G_{1\mu}^d(x)G_{2\nu\kappa}^{em}(x-y)) \\
& = gf^{abc}(\partial_\nu K_{3\kappa}^{bcm}(0, x-y) + \partial_\nu(\bar{P}_1^b(x)K_{2\kappa}^{cm}(x-y))) + \partial_\nu(\bar{K}_{2\kappa}^{bm}(x-y)P_1^c(x)) + \delta_{am}g_{\nu\kappa}\delta^4(x-y). \tag{63}
\end{aligned}$$

These corrections are completely irrelevant for the conclusions of the paper, as the omitted term in the equation for the 2-point function is just another term for the mass correction that adds to the two others already present.