Dielectric strength of noble and quenched gases for high pressure time projection chambers

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Abstract Dielectric breakdown strength is one of the critical performance metrics for pure gases and gas mixtures used in large, high pressure gas time projection chambers. In this paper we experimentally study dielectric breakdown strengths of several important time projection chamber working gases and gas-phase insulators over the pressure range 100 mbar to 10 bar, and gap sizes ranging from 0.1 to 10 mm. Gases characterized include argon, xenon, CO₂, CF₄, and mixtures 90-10 argon-CH₄, 90-10 argon-CO₂ and 99-1 argon-CF₄. We develop a theoretical model for high voltage breakdown based on microphysical simulations that use PyBoltz electron swarm Monte Carlo results as input to Townsend- and Meek-like discharge criteria. This model is shown to be highly predictive at high pressure, out-performing traditional Paschen–Townsend and Meek–Raether models significantly. At lower pressure-times-distance, the Townsend-like model is an excellent description for noble gases whereas the Meek-like model provides a highly accurate prediction for insulating gases.

1 Introduction

Since their introduction in 1974 [1], time projection chamber (TPC) detectors have become pervasive in neutrino physics and rare event searches [2–8]). The working principle of a TPC [9] is that ionization electrons or ions created by a charged particle in a liquid or gaseous medium are drifted to a detection plane preserving the three dimensional event structure. At the detection plane, the charges can be detected by induction or collection, or amplified through avalanche gain or electroluminescence, depending on the application. In all

cases, to drift charges to the detection plane before the event image is rendered un-reconstructable by diffusion or electron attachment, a drift field in the range 100–1000 V/cm must be applied to the active medium. For meter to tens-of-meter scale devices, this implies a high voltage be delivered to the detector anode or cathode that is of order tens to hundreds of kilovolts. This implies high voltage engineering challenges to ensure stable and safe detector operation.

For many neutrino physics or rare event detection applications, maximizing target density is of central importance. Cryogenic liquid time projection chambers are thus often favored due to the increased density of cryogenic liquids over gas phases of the same materials. In some situations, the increased precision available from tracking in a lower density medium favors the use of gaseous working media, however. Examples include identification of the topological two-electron signature [10] and exquisite energy resolution [11] for neutrinoless double beta decay searches in xenon gas, as employed by the NEXT program; and precise studies of neutrino interactions in the high-rate environment of the LBNF neutrino beam that will be made by an argon-gas-based detector in the DUNE near detector complex [3, 12]. In both of these applications, the relevant gas operating pressures are around 10 bar.

The study of high voltage breakdown of materials, both theoretically and experimentally, is a mature subject. The theory of dielectric discharge in gases traces its origin to the seminal work of Townsend in 1897 [13]. Nevertheless, fully trustworthy predictions of the breakdown properties of time projection chamber working media remain largely unavailable. Several recent experimental works have addressed the high voltage breakdown of liquid argon [14–17] and xenon [18] for time projection chamber applications. Experimental study of xenon gas and other pure noble elements for time projection chambers at pressures of up to 10 bar have been presented [19, 20], and various technical solutions to avoid breakdown or damage to time projection chambers in the

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event of discharge have also been proposed [21, 22]. There is also a wealth of literature on experimental studies of gaseous insulators under pulsed discharge conditions (for example, for an incomplete list, Refs. [23–29]).

In this paper we study the dielectric breakdown voltages of high pressure gases and gas mixtures of immediate interest to neutrino detection at 10 bar. This work is partly motivated both by the practical needs of the ND-GAr DUNE near detector, which is exploring gas mixtures including Ar–CO₂, Ar–CF₄, and Ar–CH₄ for the active medium, as well as insulating gases CO₂ and CF₄ for a separate buffer region used as a dedicated gaseous insulator [12]. Other mixtures with much larger hydrocarbon fraction are also being considered for studies of neutrino-hydrogen interactions [30]. The work also has a more general motivation, to develop and validate a predictive model of breakdown of high pressure gases for time projection chambers from fundamental microphysical considerations, which would also be of relevance to high pressure gas detectors for neutrinoless double beta decay [4]. Beyond using pure xenon, which has already been characterized for its high voltage strength at 10 bar [19], such experiments are also exploring various dopants and additives that may impact high voltage strength [31–38]. Due to additional costs and complexity of handling and recapturing xenon-based gas mixtures, our primary experimental focus in this work falls upon argon-based mixtures, though a comparative study of pure xenon gas validates the developed theoretical treatment for use with xenon as the base gas also.

This paper is structured as follows. In Sect. 2, we discuss the physics of high voltage breakdown in the 0.1–10 bar pressure range. We review some previous models that have been used to characterize high voltage breakdown thresholds, and introduce our microscopic extension of the Townsend and Meek discharge models based on the `PyBoltz` [39] swarm simulation package, used to interpret our experimental data. We present our experimental methods in Sect. 3, including a detailed explanation of the apparatus, data collection method, and systematic uncertainty analysis. Section 4 presents the experimental results and comparison to theoretical predictions. We conclude with a discussion of the implications of this work for future gas-phase neutrino detectors in Sect. 5.

2 Theoretical models of high voltage breakdown

For the purposes of this work, we define a high voltage breakdown as a condition when the applied potential between two electrodes is sufficient to cause a discharge that can be self sustaining. This causes a large current to flow leading to rapid drop in the potential difference [40]. The original Townsend breakdown is at its core a steady-state phenomenon. Under the original formulation, electron avalanche

multiplication in a gas generates positive ions that travel to the cathode where their impact with the cathode surface may liberate further electrons, leading to a self-sustained discharge. The Townsend breakdown criterion can also be applied to non-steady-state scenarios and photon-feedback driven avalanches. Combination of the Townsend model with an empirical parameterization of the Townsend attachment coefficient leads to a description of high voltage breakdown based on Paschen's law. We review this model in Sect. 2.1.

Townsend theory was called into question for breakdown of gases at higher pressures, where it is expected that the breakdown mechanism transitions from the Townsend breakdown to a streamer or leader breakdown [40, 41]. Under these breakdown mechanisms, space charge of ions at the tip of an advancing column of charge play a key role. We briefly describe this theory, originated by Meek and Raether, in Sect. 2.2. The transition from Townsend to streamer breakdown is imperfectly described but is generally understood to occur for air at some pressure-distance above 5 bar-cm [40]. At the pressure range of our experiments, and given the large variety of gases used, it is unclear a priori whether the Townsend or Meek description of the breakdown criterion would be more appropriate. However, since both models depend on empirical parameters that must be measured for each gas, it is often the case that in practice either can provide a reasonable fit to experimental data over a limited pressure range.

This dependence on arbitrary parameters rather compromises the predictivity of the two models above. One of our motivating goals in this work is to develop and test a fully predictive model of high voltage breakdown for TPC gases in the 1–10 bar pressure regime. In Sect. 2.3 we describe two such models, which augment the Townsend and Meek discharge models with microphysically calculated values of the Townsend first ionization and attachment coefficients. Both models are in excellent agreement at high pressure-times-distance pd and out-perform both the Paschen–Townsend and Meek–Raether models with their conventional parameters when compared to our data, providing a strong description of the breakdown strengths of all the tested gas mixtures over the pressure range 10^2 – 10^4 Torr-cm. At the lowest values of pd the `PyBoltz`-augmented Meek and Townsend predictions diverge and we find that breakdowns in noble gases are well predicted by the Townsend-like model and molecular gases by the Meek-like model, consistent with circumstantial evidence from previous studies.

2.1 Townsend breakdown and Paschen's law

In a Townsend discharge, electrons moving from the cathode to anode acquire sufficient energy between collisions with gas atoms or molecules to cause secondary ionization from electron impact on neutral gas atoms or molecules. The rate

of such ionization processes per centimeter of transport is described by Townsend's first ionization coefficient, $\alpha(E)$, which is typically a strongly growing function of electric field E under the field strengths relevant for breakdown. The total number of electrons generated by a single electron emanating from the cathode is then $N_e = e^{\alpha d}$ where d is the anode-to-cathode distance.

The production of secondary electrons also implies production of positive ions in equal numbers by charge conservation. These positive ions move toward the cathode, and when they arrive, may liberate additional electrons. The number of liberated electrons per arriving positive ion was originally encoded in Townsend's second ionization coefficient, or the secondary emission coefficient, γ_{se} . The secondary emission coefficient is dependant upon the work function and therefore the material of the cathode, as well as the ionization potential of the surrounding gas [42]. It was subsequently realized that other secondary electron generating processes may also contribute to γ_{se} [43] including photo-ionization or Penning ionization [44], the latter being relevant in multi-component gas mixtures where excitation transfer from a high energy noble excimer to a molecular gas may be efficient. The parameter γ_{se} is thus considered an effective parameter determining how many secondary electrons are produced by the sum of these processes for each positive ion produced.

A breakdown will occur in a scenario where each cathode-originated electron produces a sufficient number of positive ions to generate at least one more electron from the cathode. Under such a condition, the current flow can sustain indefinitely. This criterion is encoded mathematically in the Townsend criterion, Eq. 1:

$$\alpha(E)d = \ln \left(1 + \frac{1}{\gamma_{se}} \right). \quad (1)$$

The first Townsend coefficient depends in a complex way on the microphysical behaviour of electrons traversing the gas. To liberate a secondary electron, the electron must acquire sufficient energy between collisions to cause impact ionization. The energy spectrum of swarm electrons depends on the cross sections for elastic and inelastic processes, and the cross section for impact ionization often has a complex energy dependence, especially for molecular gases. Townsend introduced an empirical equation to describe the first ionization coefficient in several gases of experimental interest, Eq. 2 below [41].

$$\alpha(E) \sim Ape^{-\frac{Bp}{E}}. \quad (2)$$

Combination of Eq. 2 with Eq. 1, and making substitution $E = \frac{V_b}{d}$ leads to Paschen's law, which models the breakdown voltage as a function of pressure p , gap distance p , empirical

coefficients A , B and γ_{se} :

$$V_b = \frac{Bdp}{\ln(Apd) - \ln \left(\ln \left(1 + \frac{1}{\gamma_{se}} \right) \right)}. \quad (3)$$

The A and B coefficients must be measured independently for each gas or gas mixture and many experimental values for different gases can be found in the literature, e.g. Ref. [45]. For attaching gases, another process is also active: negative ion formation resulting from capture of electrons on neutral gas molecules. The Townsend criterion can be modified to include an additional coefficient, $\beta(E)$, which represents the number of electrons lost through negative ion production per unit distance [46]. The resulting modified Townsend criterion and Paschen Law are shown below as Eqs. 4 and 5 respectively [46].

$$(\alpha - \beta)d = \ln \left(1 + \frac{\xi}{\gamma_{se}} \right), \quad \xi = 1 - \frac{\beta}{\alpha}, \quad (4)$$

$$V_b = \frac{Bdp}{\ln(Apd\xi) - \ln \left(\ln \left(1 + \frac{\xi}{\gamma_{se}} \right) \right)}. \quad (5)$$

For pure noble gases which have no attachment, $\beta = 0$ gives $\xi = 1$ and then Eq. 5 reduces to Eq. 3. It is notable that in these breakdown conditions, the breakdown voltage depends only on the combination pd and not on p and d independently.

2.2 Streamer breakdown and the Meek–Raether criterion

A streamer breakdown is distinguished from a Townsend breakdown in that the electric field causing electron avalanche is dominated by the space charge associated with the avalanche itself, rather than the applied anode-to-cathode potential difference. The condition for formulation of a streamer is that the charge in an evolving avalanche must be sufficiently spatially concentrated that the E field it generates is sufficient to sustain the avalanche.

At each time during its evolution, the head of a streamer can be approximated as a sphere with radius $R(t)$. This sphere of space charge generates an electric field E' , which can be obtained from Gauss's law. Given a known number of electrons $N_e = e^{\alpha(E)x}$, the field caused by space charge at the surface of the avalanche tip is:

$$E' = \frac{eN_e}{R^2} = \frac{e \exp(\alpha x)}{R^2}. \quad (6)$$

The electric field from space charge in the streamer exceeds the electric field applied between the electrodes when:

$$E' > E \rightarrow \frac{e \exp(\alpha x)}{R^2} > E. \quad (7)$$

Raether [47] postulated that the value of R for streamers could be associated with the diffusion radius of the advancing charge column, and subsequently measured R in advancing

streamers in air to be $R \sim 0.013$ cm, consistent with this expectation. Meek, and then Meek and Loeb [48,49] used a similar principle to calculate that a self-sustained streamer breakdown would be expected when the value of αx satisfies Eq. 7 by the time $x = d$, which using the charge diffusion radius implies an order of magnitude prediction for the product $\alpha(E)d$ at the electric field strength where streamer formation begins:

$$[\alpha(E)d]_{crit} \sim 18-21. \quad (8)$$

This is conventionally called the Meek–Raether criterion. Although diffusion is central to Meek’s mechanism, the diffusion constant does not feature in the numerical result, since it is eliminated in later stages of the derivation via use of the Einstein relation. Bazelyan and Raizer subsequently re-obtained the Meek–Raether criterion without invoking diffusion [50], which shows that the Meek Raether criterion may be obtained from several different underlying mechanisms. Subsequent work [51] has discussed corrections to the criterion from detailed modelling of charge transport around the streamer front.

All derivations of this criterion involve a degree of ambiguity, encoded in the numerical value chosen for the critical value of αd . However, the rapidly varying value of $\alpha(E)$ with electric field in the vicinity of a discharge over-voltage and the exponential dependence of the criterion on this number often means that the breakdown voltage prediction is not particularly sensitive to the critical value chosen, as we will soon verify.

2.3 PyBoltz-augmented Townsend and Meek models

Our goal is to develop predictive models of high voltage breakdown in 1–10 bar pressures of gases of interest to time projection chamber detectors without arbitrary parameters for each gas. To this end, we have constructed modified Townsend and Meek models, which replace the empirical Townsend form for the $\alpha(E)$ Eq. 2 with one calculated from microscopic electron swarm simulations performed in the PyBoltz [39] software package. PyBoltz performs Monte Carlo modelling of electron trajectories in gases and gas mixtures accounting for effects of elastic and inelastic scattering, ionization, attachment, predicting diffusion constants, drift velocities, and Townsend avalanche and attachment coefficients. Figure 1, left shows as an example of the predicted functional dependence of $\alpha(E)$ from PyBoltz in comparison to the Townsend approximation with measured values of A and B from Ref. [45] in pure argon. In this illustrative example we see clear differences between both the functional form and absolute value of the Townsend function between the conventional approximation and direct calculation.

The functional form of $\alpha(E)$ so obtained is then inserted into Eq. 1, and inverted to find the breakdown voltage. The resulting breakdown criterion is a modified Paschen-like law, with one free parameter γ_{se} , is:

$$V_b = d\alpha^{-1} \left[\frac{1}{d} \ln \left(1 + \frac{1}{\gamma_{se}} \right) \right]. \quad (9)$$

Since γ_{se} appears only inside a logarithm and $\alpha(E)$ varies rapidly with electric field in the vicinity of breakdown, even rather large variations γ_{se} have a small impact on the predicted breakdown voltage. A central value of $\gamma_{se} = 0.01$ is assumed based on values that can be found in the literature, though a full order or magnitude around this number is considered when making our predictions, $0.0033 < \gamma_{se} < 0.033$. This has a small impact on the predicted breakdown voltages, only manifest at the lowest pressures. One can also obtain an augmented Meek-like criterion by replacing $1 + 1/\gamma_{se}$ with a constant $\exp([\alpha d]_{crit})$.

For gases with attachment, both $\alpha(E)$ and $\beta(E)$ are predicted, and Eq. 4 is solved numerically. Because in this case α and β appear both inside and outside the logarithm, there is not a simple expression like Eq. 9 involving an inversion of α or β , though numerical solution for the value of E that satisfies Eq. 4 is straightforward.

The mean energy of electron swarms in gases is predicted to depend on the ratio E/P and not on E or P independently. This implies an expected scaling of various transport parameters with pressure. In particular, α and β are both expected to scale as α/P and β/P at fixed E/P . This allows for calculation of these two coefficients at one pressure in PyBoltz followed by scaling to other operating pressures. The quality of the predicted scaling was checked with PyBoltz for all the gases used in this study, with excellent agreement in all cases. Included in Fig. 1, right is a comparison of α/P and β/P simulated at 1 and 10 bar demonstrating the accuracy of the predicted scaling behavior between pressures. All transport parameters used in this work are evaluated at 1 bar and scaled to the relevant working pressures.

It is notable that when $\alpha(E)$ scales with pressure in the expected way then $\alpha_p(E) = \alpha_0(E p_0/p) p/p_0$ and the breakdown voltage will be a universal function of $\chi = \frac{pd}{p_0}$, even without applying the Townsend approximation:

$$V_b = \chi \alpha_0^{-1} \left[\frac{1}{\chi} \ln \left(1 + \frac{1}{\gamma_{se}} \right) \right]. \quad (10)$$

For attaching mixtures, in terms of the reduced Townsend and attachment coefficients the breakdown condition reads:

$$[\tilde{\alpha}_0 - \tilde{\beta}_0] = \chi^{-1} \ln \left(1 + \frac{1 - \tilde{\beta}_0/\tilde{\alpha}_0}{\gamma_{se}} \right). \quad (11)$$

Fig. 1 Left: Comparison of the conventional Townsend approximation for α against the PyBoltz microphysical prediction. The blue line shows the interpolated function which is inverted to use in solution of Eq. 9. Right: PyBoltz calculations of reduced attachment and

Townsend coefficients in CO₂ evaluated at 1 and 10 bar showing the expected pressure-dependent scaling. Also shown are the two interpolated functions used in numerical solution of Eq. 4

Where the functions $\tilde{\alpha}_0$ and $\tilde{\beta}_0$ are the Townsend and attachment functions evaluated at $(V_b \chi^{-1})$:

$$\tilde{\alpha}_0 = \alpha_0 [V_b \chi^{-1}], \quad \tilde{\beta}_0 = \beta_0 [V_b \chi^{-1}]. \quad (12)$$

Solving Eq. 11 for V_b numerically provides a value for the expected breakdown voltage, which will again scale as a universal function of pd .

3 Experimental apparatus and method

To perform the breakdown measurements we designed and assembled a test stand with accurately positionable spherical electrodes operable at pressures between 0.1 and 10 bar. Figure 2, left, shows the device, consisting of two 50 mm diameter spherical 316 stainless steel electrodes that are attached to two large stainless steel disks. The disks fit snugly into a pressure vessel and locate the electrodes at its center, maintaining at least 4 cm each side between the spheres and the 6 inch diameter inner wall. Electrode distances between 0.1 and 10 mm were used. The upper gap limit was chosen to ensure the gap size was always small compared to the sphere radii and sphere-to-wall or rod distances, which at larger scales could introduce unacceptable field distortions.

The cathode sphere connects to a custom-manufactured high voltage feed-through that sits on a center flange and connects through a metal contact running through the HDPE insulator seen at the bottom of Fig. 2, left. The feed-through was made by cryo-fit of polyethylene into steel tube and performs to our specification of holding at least 55 kV high volt-

age, 10 bar operating pressure and evacuability to better than 10⁻⁶ Torr. The high voltage cathode disk is stationary while the ground disk slides along the guide rods to set the gap spacing. The position is set by placing precision thickness gauges within the gap between the spheres and then locking the shaft collars on each side of the disk preventing movement. The disks are not fixed to the pressure vessel and can slide over it, so the breakdown gap distance is not affected by any elastic deformations when the system is pressurized.

The high voltage power supply used was a Glassman KT-100 series power supply capable of delivering a maximum voltage of 100 kV and a maximum current of 20 milliamps. The power supply has a precision of ± 50 V from the read-out panel, however an improved precision of ± 5 V can be obtained via multimeter on the monitoring port. We set a maximum operating voltage of 55 kV for this study, in order to protect the feed-through. The experiment was performed over two distinct ranges of pressure, 1–10 bar and 0.1–1 bar, and to measure pressure we used two separate Bourdon pressure gauges, one for each range. The lower range gauge had a range of 0.1–1 bar of absolute pressure and a precision of ± 0.005 bar. The upper range gauge had a range of 0–20 bar of gauge pressure and a precision of ± 0.25 bar.

Before each run the vessel was evacuated overnight, and the experiments were started only when residual gas pressures of order 10⁻⁶ mbar were obtained, as read from an ion gauge on the vacuum line. The vessel was isolated from vacuum using a Carten valve and filled with test gas to the specified pressure. Every gas was of a minimum 99.999% purity, including the individual gases used in the gas mix-

Fig. 2 Left: A photograph of the apparatus used in this study. Breakdowns are initiated between two polished spheres with an adjustable gap width, at voltages of up to 50 kV. Right: Block diagram of the experiment showing key system components

tures which had an uncertainty of $\pm 0.01\%$ on the mix ratio. Gases and mixtures that were compatible were filled through a SAES cold getter for initial purification. We made a comparison run in pure argon from the gas bottle without purification and found equivalent breakdown voltages, so even in the case of molecular gas mixtures which could not be purified, the raw gas purity is expected to be sufficiently high not to compromise the dielectric strength measurements.

Once the vessel was filled to the desired pressure, the voltage was steadily increased until a sharp increase in current occurred, tripping the over current protection on the power supply, which was taken as evidence of a high voltage breakdown across the gap. This was repeated for at least three breakdown measurements at each pressure increment and a range of pressures for each gas and electrode separation distance. To test for possible hysteresis, comparative measurements were made with increasing and then decreasing pressure increments for argon gas, with very similar results in both cases. The difference of average magnitude 6% is added in quadrature as a small uncertainty contribution in the final error bars.

Since our device does not incorporate continual circulation and re-purification, to test for time dependence of the breakdown strength due to out-gassing of water during the run a time dependent study was undertaken. A set of breakdown measurements were taken at one bar pressure immediately after filling the vessel and again at time intervals up to 24 h. The results of this study can be seen in Fig. 3 with

data taken at every 30 min interval and the last data point taken at 24 h. An $\mathcal{O}(5\%)$ deviation is observed, taking place over around 5 h. Since one run typically takes 1–2 h starting from clean gas in an evacuated vessel, this degree of variation is small. While this effect is somewhat degenerate with the previously described hysteresis uncertainty, it is conservatively included in the final error bars as an uncorrelated contribution.

A systematic uncertainty is applied to account for the non-planar nature of the electrodes leading to breakdown occurring in a region of slowly varying electric field rather than a uniform field configuration, as in the idealized Townsend discharge. We performed a calculation to determine the ratio of field strength of spherical electrodes to planar electrodes (which we call the ‘enhancement factor’) following the methods of Ref. [52]. The determined enhancement factor is shown in Fig. 3, right. The largest value of the enhancement factor in the gap is taken as a systematic uncertainty on the applied voltage leading to breakdown for each geometry. In practice it is expected that the breakdown is initiated in the highest field region and so we expect the true values to be near the upper part of this allowed range, which has a span of around $\pm 6\%$.

Each data point in our presented results represents the mean of at least three breakdown measurements at each pressure point, with the standard deviation added in quadrature to the systematic uncertainties described above to form the

Fig. 3 Left: Breakdown voltage as a function of the time elapsed after pressurizing to 1 bar of Ar-CH₄; Right: calculation of enhancement factors of electric field relative to parallel plate geometry as a function

of position in the gap between the two spheres z for fixed values of radius R and gap size S used in this study

error bar. In all cases the statistical spread is dominant over all of the systematic uncertainties.

4 Results and discussion

Data was taken at varying gap distances to span the full range of pd values of interest for several gas mixtures of interest to future neutrino detectors: pure argon, pure xenon, pure CO₂, pure CF₄, Ar-CO₂ (90%/10%), Ar-CH₄ (90%/10%) and Ar-CF₄ (99%/1%). The largest dataset was accumulated with pure argon gas, with gap spacings 0.1 to 10 mm in order to make detailed comparisons between available high voltage breakdown models. The resulting dataset can be seen in Fig. 4 alongside various theoretical curves. We show the traditional Paschen curve with the Townsend approximation for $\alpha(E)$ with A and B taken from Ref. [42], which fits the data well at lower pressures but diverges rapidly at higher ones, as well as the Meek criterion with conventional values for A and B which does not fit the data well anywhere.

We also show two intermediate Paschen-Townsend curves, which have the traditional form but re-fitted parameters. The first has A and B in the Townsend approximation for $\alpha(E)$, Eq. 2, fitted to PyBoltz predictions over the pd range of interest. This prediction represents, in a sense, the best theoretically informed version of the traditional Paschen curve. This theoretical description shows similar deficiencies to the original Paschen-Townsend curve, agreeing well at low pressure and poorly at high pressure. It thus appears that the primary deficiency of the Paschen-Townsend model lies in the

form of the empirical parameterization Eq. 2 and not only its parameters, since even after making our best theoretical prediction of the free parameters it does not match experiment well over all pd values. We also show a Paschen-Townsend curve with A and B fitted to our experimental data directly. Naturally, this model fits more closely to the data used to constrain it, though the values of A and B that emerge from the fit are far from the values typically measured at low pd , and their interpretation in this context is questionable. In this fit γ_{se} was fixed to 0.01 with A and B free. Allowing γ_{se} as a further free parameter and fitting a three-parameter Townsend-Paschen model to our data yields $\gamma_{se} = 0.02$ and an almost indistinguishable Paschen-Townsend curve (so much so that we omit it from Fig. 4 to avoid over-cluttering). Values of the fitted A and B for each of these models are tabulated in Table 1.

Also shown on Fig. 4 are the two models that dispense with A and B and represent central theoretical products of this work: the PyBoltz-augmented Townsend and Meek models for breakdown voltage, calculated per the methods of Sect. 2.3. The shaded region around the Townsend-like model covers an order of magnitude of realistic values of γ_{se} as described in Sect. 2.3. The shaded region around the Meek-like model covers the range of viable $[\alpha d]_{crit}$ values 18–21. At the lowest pd , the region of smaller gap sizes and lower pressures where the Paschen curve is most frequently studied, this prediction is in good agreement with the conventional Paschen-Townsend description. The model diverges from the other descriptions at higher pressures but maintains a good match to data, out-performing all of the

Table 1 A , B and γ coefficients from various descriptions of the breakdown voltage in terms of the Paschen–Townsend parameterization. Numbers in (brackets) are fixed constants, whereas those without are fit results. The first row shows the conventional values from Ref. [42]. The second row shows the result of fitting the Townsend approximation Eq. 2 to PyBoltz predictions of $\alpha(E)$ for argon. The third and fourth rows show the result of fitting the Paschen curve to data directly, either with or without γ_{se} as a free parameter; in practice these two models are nearly indistinguishable. None of these models fits the data well over all pd values as well as the PyBoltz–Townsend model, which predicts $\alpha(E)$ directly rather than relying on A and B coefficients

Source	A	B	γ_{se}
Conventional value [42]	(12)	(180)	(0.01)
Fit to PyBoltz $\alpha(E)$	15	173	(0.01)
Fit to data $V_B(pd)$: AB(γ_{se})	3.6	52	(0.01)
Fit to data $V_B(pd)$: AB γ_{se}	3.0	52	0.02

previous models in terms of its ability to describe the data over the full range of pd values of this study. The weak (logarithmic) dependence of the breakdown voltage upon the only unknown parameter γ_{se} implies a high degree of predictivity, without sensitive dependence of breakdown voltage on a-priori unknown empirical parameters. The PyBoltz-augmented Meek model is not a good fit at lower pd values but tends toward the PyBoltz-augmented Townsend prediction at higher pressures.

Figure 5 shows similar comparison for argon plus five other gases and gas mixtures studied in this work, compared to the theoretical PyBoltz-augmented Townsend and Meek predictions. The PyBoltz calculations are rather predictive in all cases, especially at higher pressures with small offsets between the curves and data for every gas except Argon. In xenon gas, once again the PyBoltz-augmented Townsend model appears very accurate at all values of pd . The pure molecular gases CF_4 and CO_2 (shown separately in Fig. 6) appear to fit significantly better to PyBoltz-augmented Meek predictions rather than PyBoltz augmented Townsend ones, however. The noble-molecular gas mixtures appear to be intermediate, relatively well described by either model, though with some tendency towards the Meek–Raether model, as may be expected in quenched gas mixtures.

Since the PyBoltz-augmented Townsend model clearly under-predicts the breakdown strength at the lowest pd values for photon-quenched gases despite having being validated very well over all pd values in nobles, we may postulate that the dielectric breakdowns in the noble gases are more Townsend-like in nature whereas the dielectric breakdowns in the molecular gases are more streamer-like in this pressure range. Before discussing this hypothesis further, we consider two other possibilities. First, we note that the largest deviations from Townsend-like behaviour are observed in CO_2 and

CF_4 , which both have relatively strong attachment, unlike argon and xenon. We should consider whether the method of incorporating attachment into the Townsend formalism is sufficient, since it is based on steady-state discharge arguments, and the sparks in this system are clearly transient events. Comparison of the with- and without-attachment models for CO_2 shown in Fig. 6 demonstrates that the effects of attachment in the breakdown criterion primarily emerge only at higher pd values, and thus are not likely to explain the Townsend model deficiencies at lower pd . A further consideration is that the molecular gases are clearly more complex to model in swarm simulations, in particular their scattering and ionization cross sections may be less well characterized than for pure argon or xenon. On the other hand, both CO_2 and CF_4 are relatively widely used gases in particle detectors [53], and both sets of cross sections used in this work have a five-star demarcation in the MagBoltz [54] package, the highest quality rating. It thus appears unlikely that they are so deficient as to cause the observed effects.

We thus consider the plausible yet speculative explanation, that the Townsend-to-streamer transition occurs at lower pressure-distance values for CO_2 and CF_4 and Ar-based mixtures than for pure Ar and Xe gases, and indeed the discharges in noble gases should be considered as Townsend-like whereas those in insulating or quenched gases should be considered as Meek-like. In dry air, the transition between Townsend and streamer-like discharge has been reported to occur at a pd value above around 5000 Torr cm [55,56], the upper end of the values explored in this work. It is therefore very reasonable to consider transitions between these two descriptions would occur in this regime for the various gases tested. That the quenched gases may develop streamers at lower pressures than the noble and predominantly noble gases also appears consistent with previous results. For example, Ref. [57] studies time evolution of discharges at pressures of up to 1 bar in various gases. There, argon gas showed Townsend-like behaviour of the time profile for all tested values of pd , whereas a transition from Townsend-like to streamer-like behaviour was observed in the molecular gases SF_6 and CCl_2F_2 at pressures below 1 bar. This appears to be in good circumstantial agreement with our observations of a Meek-like breakdown criterion in photon quenched and insulating gases and a more Townsend-like one in noble gases.

While certainly of fundamental interest, it is notable that this distinction at low pd is of limited pragmatic interest for time projection chambers applications. The proposed uses, especially of pure CO_2 and pure CF_4 as gas-phase insulators, involve standing off high voltages at large gap distances and high pressures, for which the largest pd values probed in this work are most relevant. In this regime the Townsend and Meek predictions for breakdown voltage become equivalent, and our model is predictive independently of the critical value $[\alpha d]_{crit}$ or γ_{se} .

Fig. 4 Argon breakdown voltage vs. pressure-length data plotted alongside the theoretical curves

5 Conclusions

We have studied a suite of gases being actively considered as working media for near-future high pressure gas time projection chamber detectors in neutrino physics. Due to its low breakdown voltage and lack of photon quenching, pure argon gas is not a common working medium for large gas-phase time projection chambers, though was studied as a benchmark for comparison against historical data and models. Doped argon gas mixtures are of great interest, and in particular all of 90-10 argon-CH₄, 90-10 argon-CO₂ and 99-1 argon-CF₄ are being actively considered as working media for a high pressure gas near detector for the DUNE experiment. Surrounding this active volume may be a volume of insulating gas and in each case the minority component of the drift gas would be a favorable choice, to minimize the impact of possible (though undesirable) diffusive leaks between inner volumes. To this end we have also studied pure CO₂ and CF₄. Pure CH₄ is not an appealing insulating gas due to its flammability, and has not been studied. Finally we also studied pure xenon, the active medium of high pressure gas time projection chambers searching for neutrinoless double beta decay in ¹³⁶Xe.

In all cases, we observe deviations from Paschen-like pressure scaling at high pressures, which can be attributed to imperfection of the empirical Townsend approximation for describing the dependence of the Townsend coefficient $\alpha(E)$ upon electric field. A new model, which uses the PyBoltz electron swarm simulation code to predict the Townsend α and β coefficients was used to derive an augmented Townsend or Meek discharge model that is found to be highly predictive for the majority of the gases considered in this study. Both PyBoltz-augmented Townsend-like and

Meek-like models are strongly predictive for all gases at large pd values, unlike any of the conventional models.

For noble gases, the PyBoltz-augmented Townsend model is predictive for all pd values investigated, whereas for the pure molecular gases CF₄ and CO₂ the PyBoltz-augmented Townsend model under-predicts the breakdown voltage data by factors of up to two. A PyBoltz-augmented Meek criterion provides a good description of the data for these gases. We consider this as circumstantial evidence that a transition from Townsend-like to Meek-like discharges is present at lower pressures than in the noble gases, and this explanation also appears consistent with other reported studies. While plausible, we do not overlook that since micro-physics of CO₂ and CF₄ are rather more complex than the pure noble gases, the observed differences may also be associated with imperfect collision or impact ionization cross sections in the PyBoltz code. At the higher pressures and larger gap distances which are of the most pragmatic interest for this work, either the Townsend-like or Meek-like models become sufficiently accurate for projecting breakdown voltages in all cases, including for molecular gases CO₂ and CF₄ and gas mixtures.

Due to limitations imposed by our high voltage feed-through, we were not able to induce breakdown in all gases at 10 bar pressure and 1 cm distance below the maximum safe operating voltage of 55 kV. In all such cases (all gases except argon) we conclude a breakdown field of at least 55 kV over 1 cm is sustainable at 10 bar. Since the data and models agree very well at the higher pressures and gap sizes, we can also extrapolate the breakdown voltages observed at the highest pressures and gap distances to the benchmark point of 1 cm and 10 bar. Table 2 presents these projections for both models. Argon-based gas mixtures are projected to support

Fig. 5 Breakdown data for various gases and gas mixtures plotted alongside the PyBoltz Predictions for each gas. *5 mm Xe data presented from a functionally equivalent device in Ref. [19]

Table 2 Projected breakdown voltage of several gases at a benchmark point of 10 bar pressure, 1 cm gap distance. Based on the observed trends the bold values are the recommended projections for the pure gases

Projected breakdown voltage at 10 bar, 1 cm (kV)							
	Ar	Xe	Ar-CF ₄	Ar-CH ₄	Ar-CO ₂	CO ₂	CF ₄
Townsend	52.6	75.4	61.7	63.9	68.6	129.5	179.7
Meek	69.9	98.9	72.1	80.3	87.3	171.2	212.2

Fig. 6 CO₂ breakdown voltage vs. pressure-length data plotted alongside the theoretical curves

electric fields of ~ 90 kV/cm over 1 cm-scale gaps; the insulating gases CO₂ and CF₄ are projected to support ~ 170 and ~ 210 kV/cm respectively. These dielectric strengths are very promising for the proposed applications as active gases and insulating gases in large, high pressure gas time projection chambers.

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