



# Erratum to: Chiral perturbation theory for nucleon generalized parton distributions

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## 1 Erratum

The result for  $E_n^{(2,\pi)}(t)$  in (50) contains mistakes in the terms that multiply the low-energy constants  $c_2$  and  $c_3$ . The corrected version of this equation reads

$$\begin{aligned}
 E_n^{(2,\pi)}(t) &= \frac{3m^2 g_A^2}{(4\pi F)^2} \log \frac{m^2}{\mu^2} \sum_{\substack{j=0 \\ \text{even}}}^{n-2} \tilde{a}_{n,n-j-2} \\
 &+ \frac{6}{(4\pi F)^2} \sum_{\substack{j=0 \\ \text{even}}}^{n-2} \tilde{a}_{n,n-j-2} \int_{-1}^1 d\eta \eta^j (1-\eta^2) \\
 &\times \left\{ \frac{g_A^2}{32} \left[ 2t \left( \log \frac{m^2(\eta)}{\mu^2} + 1 \right) - \frac{(t-2m^2)^2}{m^2(\eta)} \right] \right. \\
 &+ M \left[ \left( c_1 m^2 + \frac{1}{4} c_3 (t-2m^2) \right) \left( \log \frac{m^2(\eta)}{\mu^2} + 1 \right) \right. \\
 &\left. \left. - \frac{1}{4} c_2 m^2(\eta) \log \frac{m^2(\eta)}{\mu^2} \right] \right\} \\
 &= -\frac{3m^2 g_A^2}{2(4\pi F)^2} \log \frac{m^2}{\mu^2} \sum_{\substack{j=2 \\ \text{even}}}^n 2^{-j} j A_{n,n-j}^{\pi(0)} \\
 &- \frac{6}{(4\pi F)^2} \sum_{\substack{j=2 \\ \text{even}}}^n 2^{-j} A_{n,n-j}^{\pi(0)} \int_{-1}^1 d\eta (1-\eta^j)
 \end{aligned}$$

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$$\begin{aligned}
 &\times \left\{ \frac{g_A^2}{32} \left[ 2t \left( \log \frac{m^2(\eta)}{\mu^2} + 1 \right) - \frac{(t-2m^2)^2}{m^2(\eta)} \right] \right. \\
 &+ M \left[ \left( c_1 m^2 + \frac{1}{4} c_3 (t-2m^2) \right) \left( \log \frac{m^2(\eta)}{\mu^2} + 1 \right) \right. \\
 &\left. \left. - \frac{1}{4} c_2 m^2(\eta) \log \frac{m^2(\eta)}{\mu^2} \right] \right\},
 \end{aligned}$$

where the terms that have changed are marked in red. The corresponding corrections in equations (52) and (54) read

$$\begin{aligned}
 E_n^{(2,\pi)}(0) &= -\frac{3m^2 g_A^2}{2(4\pi F)^2} \log \frac{m^2}{\mu^2} \sum_{\substack{j=2 \\ \text{even}}}^n 2^{-j} j A_{n,n-j}^{\pi(0)} \\
 &+ \frac{12m^2}{(4\pi F)^2} \left\{ \frac{g_A^2}{8} - M \left[ \left( c_1 - \frac{1}{2} c_3 \right) \left( \log \frac{m^2}{\mu^2} + 1 \right) \right. \right. \\
 &\left. \left. - \frac{1}{4} c_2 \log \frac{m^2}{\mu^2} \right] \right\} \sum_{\substack{j=2 \\ \text{even}}}^n 2^{-j} \frac{j}{j+1} A_{n,n-j}^{\pi(0)}
 \end{aligned}$$

and

$$\begin{aligned}
 \partial_t E_n^{(2,\pi)}(0) &= -\frac{3g_A^2}{4(4\pi F)^2} \left[ \log \frac{m^2}{\mu^2} + 3 \right] \sum_{\substack{j=2 \\ \text{even}}}^n \frac{2^{-j} j}{j+1} A_{n,n-j}^{\pi(0)} \\
 &+ \frac{2}{(4\pi F)^2} \sum_{\substack{j=2 \\ \text{even}}}^n 2^{-j} \frac{j(j+4)}{(j+1)(j+3)} A_{n,n-j}^{\pi(0)} \left\{ \frac{g_A^2}{8} \right. \\
 &\left. + M \left[ c_1 - \frac{1}{2} c_3 - \left( \frac{1}{4} c_2 + \frac{3(j+3)}{2(j+4)} c_3 \right) \left( \log \frac{m^2}{\mu^2} + 1 \right) \right] \right\}
 \end{aligned}$$

respectively. With the parameter estimates  $c_1 \approx -0.9 \text{ GeV}^{-1}$ ,  $c_2 \approx 3.3 \text{ GeV}^{-1}$ ,  $c_3 \approx -4.7 \text{ GeV}^{-1}$  given below (52), one obtains corrected numerical values

$$E_2^{(1,\pi)}(0) + E_2^{(2,\pi)}(0) \approx (0.12 + 0.10) A_{2,0}^{\pi(0)},$$

$$\partial_t E_2^{(1,\pi)}(0) + \partial_t E_2^{(2,\pi)}(0) \approx -(2.5 + 3.4) \text{ GeV}^{-2} A_{2,0}^{\pi(0)}.$$

After the above corrections, we agree with the results obtained in [1]. We thank M. Polyakov for pointing us to the difference between the calculation in that paper and the published version of our work.

## Reference

1. H. Alharazin, D. Djukanovic, J. Gegelia, M. Polyakov., [arXiv:2006.05890](https://arxiv.org/abs/2006.05890) [hep-ph]