

Electromagnetic properties of vibrational bands in ^{170}Er

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Abstract. Excited states of the nucleus ^{170}Er have been studied by Coulomb excitation using the GASP γ -ray detector system at the Laboratori Nazionali di Legnaro. The ground-state band along with a low-lying $K^\pi = 0^+$ band and γ -vibrational band were populated during the experiment. Based on the measured γ -ray yields, a set of interband and intraband matrix elements has been extracted using the Coulomb excitation code GOSIA. The resulting $E2$ matrix elements are compared to collective model predictions.

1 Introduction

In the nucleus ^{170}Er , a low-lying $K^\pi = 0^+$ band occurs at nearly the same energy as the γ -vibrational band. The interaction between these bands has been investigated previously in inelastic scattering experiments [1]. While the reduced quadrupole transition probability between the ground-state band and the 2^+ state of the $K^\pi = 0^+$ band corresponds to only $\sim 8\%$ of the transition probability to the 2^+ state in the γ -band [2], mixing between the two bands at spin 4^+ enhances the population of the low-lying $K^\pi = 0^+$ band. This mixing manifests itself as a deviation in the electromagnetic transition strengths from the leading-order relations described by Bohr and Mottelson [3]. Therefore a direct measure of these strengths provides information on not only the collective and single-particle properties but also on the magnitude of the mixing. For this reason we have carried out a Coulomb excitation measurement of the nucleus ^{170}Er . Prior to this experiment, experimental evidence regarding electromagnetic transition strengths was limited to the low-lying band heads and the intraband elements

of the ground-state band. A number of low-lying positive- and negative-parity bands have also been established [4, 5]. In addition, candidate states built on the two phonon γ -vibrational mode have been identified in the neighboring nuclei ^{166}Er [6, 7] and ^{168}Er [8–10]. Due to the low-lying nature of these bands, Coulomb excitation provides an excellent means for further exploring the electromagnetic properties and interactions of these structures.

2 Experimental methods

The Coulomb excitation measurement was performed using a ^{32}S beam at a safe energy of 117 MeV at the Laboratori Nazionali di Legnaro, Italy. The beam current throughout the experiment was ~ 1 pnA. The GASP [11] γ -ray detector system was used to detect the de-excitation γ -rays. GASP consists of 40 hyper-pure high-efficiency Compton-suppressed germanium detectors. The detector system was set up in configuration II, without the BGO multiplicity filter. In this configuration the array has a total efficiency of $\sim 5.8\%$ at 1.33 MeV. A square Double-Sided Silicon Strip Detector (DSSSD), placed

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at 90° with respect to the beam axis and perpendicular to the 1 mg/cm^2 ^{170}Er target, was used for particle identification. During the experiment, the strips of the 32×32 DSSSD array were connected in groups of two amounting to a total of 32 channels. The recording of an event was triggered by the detection of at least a single γ -ray in GASP and a charged particle in the DSSSD. The EUCLIDES [12] data acquisition system along with Mesytec [13] amplifiers were used for readout of the detectors. In addition a $12\ \mu\text{m}$ thick Al foil was placed cylindrically around the target position to stop delta electrons. A thin ^{181}Ta collimator was also placed upstream of the target. Energy calibration of the GASP array was performed using a standard ^{152}Eu γ -ray source.

The results presented in this paper were obtained through the following steps: 1) reducing the data to events which contained only a single front and back strip hit in the DSSSD; 2) applying a time cut between front and back strip hits; 3) imposing a kinematical cut on the measured particle energies and scattering angles; 4) applying a particle- γ -ray coincidence condition; and 5) event-by-event Doppler correction of the resulting γ -ray spectrum. This last condition is necessary since the γ -rays of interest were emitted in-flight. With this selection on the kinematics of the reaction, the target thickness, and the insertion of the Al foil, the ^{170}Er particles are stopped before reaching the DSSSD. The energies and angles of the recoiling nucleus were calculated based on the information provided by the ^{32}S scattered beam particles. The reconstructed angles and energies were subsequently used during the Doppler correction. A selection of the measured raw and Doppler-corrected spectra are shown in fig. 1. The data represent γ -rays detected in the full GASP array in coincidence with a particle in the region corresponding to $52.4^\circ < \theta < 66.0^\circ$ of the DSSSD. In total, $\sim 3.3 \times 10^6$ particle- γ -ray coincidences were used in the analysis. Emitted γ -rays resulting from excitations in the ^{181}Ta collimator and peaks from $^{166-168}\text{Er}$ contaminants can also be identified in the Doppler-corrected spectrum.

A partial level scheme resulting from the experiment is shown in fig. 2. The low-lying $K^\pi = 0^+$ band and γ -vibrational band were excited up to the 6^+ states and the ground band up to the 10^+ state. In addition several previously known higher-lying states were excited. These include two 3^- states at 1340 keV and 1579 keV, one 5^- state at 1483 keV, one 7^- state at 1705 keV, and a 2^+ state at 1416 keV [2]. The placement of these states were confirmed by the coincidence data. In addition, a 686 keV γ -ray was found in coincidence with the 843 keV γ -ray depopulating the $4^+_{K=0^+}$ state, corresponding to a level at an energy of 1789 keV. The coincidence data showed no indication of a significant population of the $K^\pi = 3^+$ band observed in ref. [1]. The width of the 1049 keV peak was, however, measured to be $\sim 10\%$ larger than the peak at 1024 keV, which could possibly indicate the presence of a doublet arising from the $4^+_{K=3^+} \rightarrow 4^+_g$ transition.

From the Doppler-corrected γ -ray singles spectrum, relative intensities were extracted using the RADWARE [14, 15] package. They are listed in table 1. Due to

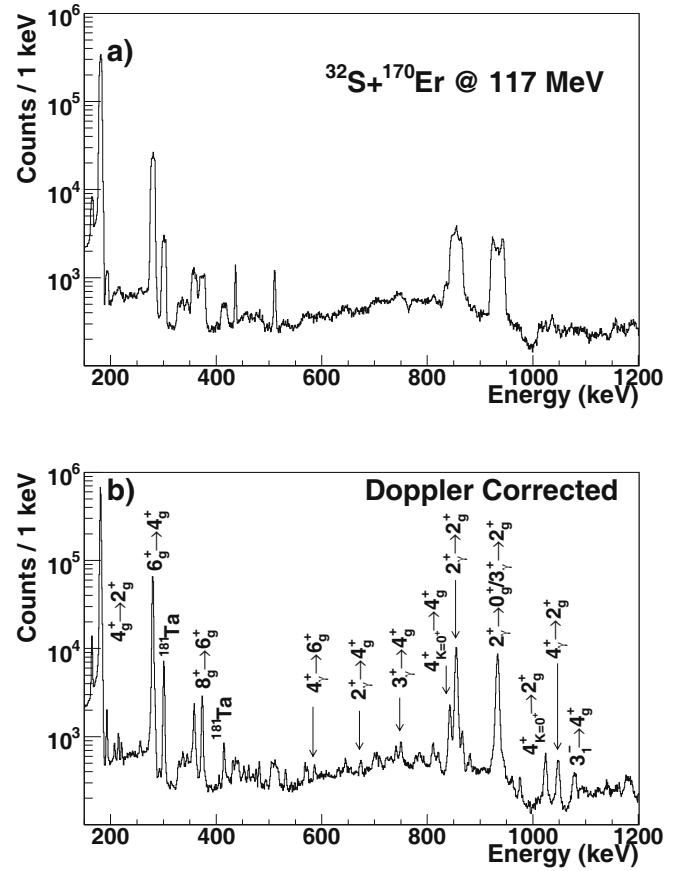


Fig. 1. Raw (a) and Doppler-corrected (b) γ -ray spectra for the entire experiment detected with the full GASP array. The spectra were generated with the coincidence condition that a scattered ^{32}S nucleus was detected within the range $52.4^\circ < \theta < 66.0^\circ$. Several of the relevant transitions are highlighted. The ^{181}Ta lines arise from the collimator placed in front of the target position.

uncertainties in the efficiency calibration at low energies, the intensities for the $4^+_g \rightarrow 2^+_g$ and $2^+_g \rightarrow 0^+_g$ transitions were not determined with high precision and were therefore not used directly in the analysis described below. The transitions corresponding to $2^+_g \rightarrow 0^+_g$ and $3^+_g \rightarrow 2^+_g$, as well as $0^+_{K=0^+} \rightarrow 2^+_g$ and $6^+_{K=0^+} \rightarrow 6^+_g$ are given as unresolved doublets. The $4^+_{K=0^+} \rightarrow 6^+_g$ transition may or may not be present in the spectrum and is given as an upper limit. The two transitions at 476 keV and 481 keV possibly overlap with corresponding transitions in ^{181}Ta and should be considered upper limits [16].

3 Coulomb excitation analysis

The yields corresponding to the relative intensities shown in table 1 can be used as input for the coupled-channels code GOSIA [17] to extract electromagnetic properties of the low-lying structures shown in fig. 2. The principle behind the code is to find a set of electromagnetic matrix elements, within the Coulomb excitation framework, which

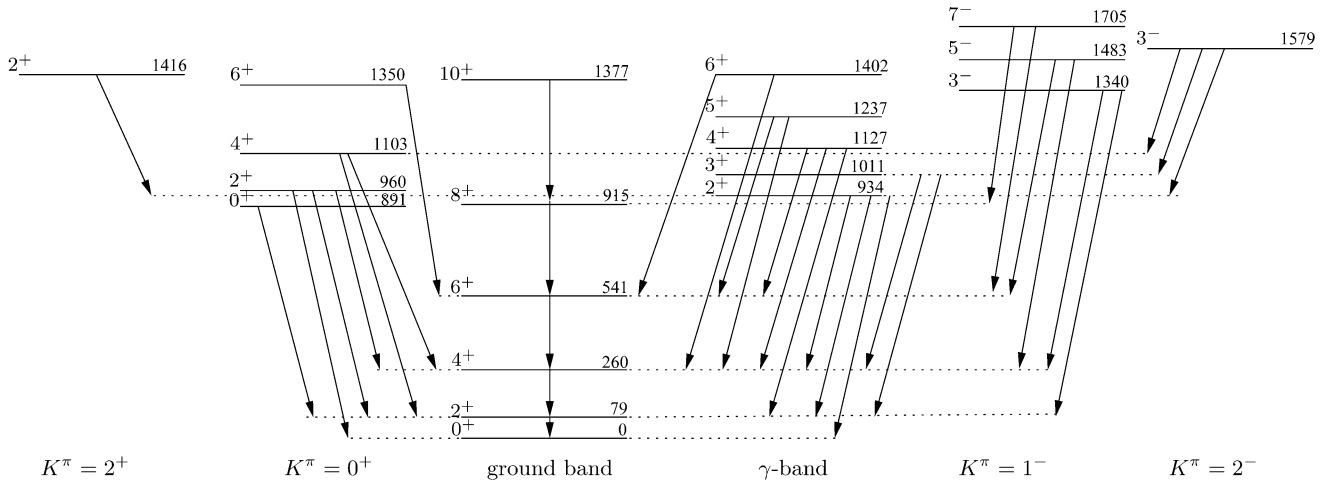


Fig. 2. Partial level scheme showing the levels observed during this study. The $K^\pi = 0^+$ ground-state band (central) and low-lying $K^\pi = 0^+$ (to the left), the $K^\pi = 2^+$ γ -band (to the right), a $K^\pi = 2^+$ state (far left), and negative-parity states (far right) are indicated. The transitions observed in the experiment are indicated by arrows. The level energies are given in keV.

Table 1. Relative intensities extracted from the Doppler-corrected spectrum.

Transition	Energy (keV)	Relative γ -ray intensity
$6_g^+ \rightarrow 4_g^+$	280	100(6)
$8_g^+ \rightarrow 6_g^+$	374	4.88(30)
$10_g^+ \rightarrow 8_g^+$	462	0.37(4)
$2_\gamma^+ \rightarrow 0_g^+ / 3_\gamma^+ \rightarrow 2_g^+$	934/932	42(3)
$2_\gamma^+ \rightarrow 2_g^+$	855	43(3)
$2_\gamma^+ \rightarrow 4_g^+$	674	0.55(6)
$3_\gamma^+ \rightarrow 4_g^+$	750	1.45(11)
$4_\gamma^+ \rightarrow 2_g^+$	1049	2.37(18)
$4_\gamma^+ \rightarrow 4_g^+$	867	3.26(22)
$4_\gamma^+ \rightarrow 6_g^+$	587	0.44(5)
$5_\gamma^+ \rightarrow 4_g^+$	976	0.72(7)
$5_\gamma^+ \rightarrow 6_g^+$	696	0.17(11)
$6_\gamma^+ \rightarrow 4_g^+$	1142	< 0.62
$6_\gamma^+ \rightarrow 6_g^+$	861	< 2.50
$0_{K=0^+}^+ \rightarrow 2_g^+ / 6_{K=0^+}^+ \rightarrow 6_g^+$	812/810	1.67(16)
$2_{K=0^+}^+ \rightarrow 0_g^+$	960	0.35(7)
$2_{K=0^+}^+ \rightarrow 2_g^+$	881	0.92(10)
$2_{K=0^+}^+ \rightarrow 4_g^+$	700	0.73(13)
$4_{K=0^+}^+ \rightarrow 2_g^+$	1024	2.37(17)
$4_{K=0^+}^+ \rightarrow 4_g^+$	843	7.96(49)
$4_{K=0^+}^+ \rightarrow 6_g^+$	563	< 0.11
$3_1^- \rightarrow 4_g^+$	1080	1.36(11)
$3_1^- \rightarrow 2_g^+$	1262	< 0.40
$3_2^- \rightarrow 2_\gamma^+$	645	0.56(6)
$3_2^- \rightarrow 3_\gamma^+$	569	0.50(6)
$3_2^- \rightarrow 4_{K=0^+}^+$	476	0.26(4) ^a
$2_{K=2^+}^+ \rightarrow 2_\gamma^+$	481	0.48(5) ^a

^a These lines may be contaminated with corresponding lines in ^{181}Ta and should be considered as upper limits.

best reproduces the experimentally measured yields. A least-squares approach is employed and the quality of the fit is determined by the normalized χ^2 criterion. The χ^2 parameter is calculated in the standard way, but is however normalized to the number of data points rather than the number of degrees of freedom. The input to GOSIA, in addition to the measured yields, are the energies of the observed excited states, along with some unobserved states to account for virtual excitation effects, the geometry of the particle and γ -ray detector setup, and other previously known experimental data. These include branching ratios, lifetimes, mixing ratios, and matrix elements.

The leading-order intensity relation, described by Bohr and Mottelson [3], relates the interband and intraband matrix elements between the states shown in fig. 2 to one free parameter respectively, the intrinsic matrix element. This relation can be represented by eq. (4-92) in ref. [3],

$$\langle K_2 I_2 \| \mathcal{M}(\lambda) \| K_1 I_1 \rangle = (2I_1 + 1)^{1/2} \langle I_1 K_1 \lambda, \Delta K | I_2 K_2 \rangle \langle K_2 | \mathcal{M}(\lambda, \mu) | K_1 \rangle \xi, \quad (1)$$

where $\langle K_2 | \mathcal{M}(\lambda, \mu) | K_1 \rangle$ is the intrinsic matrix element, $\langle K_2 I_2 \| \mathcal{M}(\lambda) \| K_1 I_1 \rangle$ is the reduced matrix element, and $\langle I_1 K_1 \lambda \Delta K | I_2 K_2 \rangle$ is the Clebsch-Gordan coefficient. For transitions between the three low-lying bands, $K_1 = 0$ and the constant $\xi = \sqrt{2}$ if $K_2 = 2$ and is equal to 1 when $K_2 = 0$. For the intraband transitions, the constant ξ is also equal to 1. Three intrinsic matrix elements, one for each of the bands, coupling the states up to spin 12^+ in the ground band, 10^+ in the $K^\pi = 0^+$ band, and 8^+ in the γ -band, were defined in the fitting procedure. Additionally, two intrinsic matrix elements for the interband transitions between the γ - and ground bands and the $K^\pi = 0^+$ and ground bands were also defined. The coupling between the γ - and $K^\pi = 0^+$ bands was assumed to be zero.

A similar coupling approach has also been introduced for the $M1$ matrix elements. In principle these components could be determined from previously known mixing ratios and could potentially be entered into GOSIA. However

Table 2. Previously known branching ratios and lifetimes defined as data points during the GOSIA fitting procedure. These branching ratios and lifetimes were reproduced in the fit within the given 1σ limit.

$I_i \rightarrow I_f / I_i \rightarrow I_f$	Ref. [2]
$2^+_{\gamma} \rightarrow 4^+_g / 2^+_{\gamma} \rightarrow 2^+_g$	0.014(3)
$2^+_{\gamma} \rightarrow 0^+_g / 2^+_{\gamma} \rightarrow 2^+_g$	0.897(24)
$3^+_{\gamma} \rightarrow 4^+_g / 3^+_{\gamma} \rightarrow 2^+_g$	0.146(11)
$4^+_{\gamma} \rightarrow 2^+_g / 4^+_{\gamma} \rightarrow 4^+_g$	0.86(11)
$2^+_{K=0^+} \rightarrow 4^+_g / 2^+_{K=0^+} \rightarrow 2^+_g$	0.65(4)
$2^+_{K=0^+} \rightarrow 0^+_g / 2^+_{K=0^+} \rightarrow 2^+_g$	0.63(7)
$4^+_{K=0^+} \rightarrow 2^+_g / 4^+_{K=0^+} \rightarrow 4^+_g$	0.273(22)
$6^+_{K=0^+} \rightarrow 4^+_{K=0^+} / 6^+_{K=0^+} \rightarrow 6^+_g$	0.076(25)
Level	Lifetime (ps) ref. [2]
2^+_{γ}	2.61(9)
$2^+_{K=0^+}$	17.46(216)

there exists a large discrepancy in both sign and magnitude for many of the mixing ratios listed in ref. [2] and they were therefore not included. The $M1$ matrix elements were instead coupled to intrinsic matrix elements which were each varied as a single parameter during the fit. The $M1$ intraband matrix elements for the γ -band were included by eq. (1). The K -forbidden $M1$ transitions to the ground band were coupled using eq. (4-95) in ref. [3]. The $M1$ components between the $K^{\pi} = 0^+$ and ground bands were included by eq. (4-254) in ref. [3].

This simplified coupling scheme is however not sufficient to reproduce the observed decay patterns. It is possible that the two near-degenerate 4^+ states in the $K^{\pi} = 0^+$ and γ -bands lead to a breaking of the coupling scheme described above. During the fitting procedure, the interband $E2$ matrix elements, originating from the 0^+ , 2^+ and 4^+ states in the $K^{\pi} = 0^+$ and γ -bands, were instead varied individually. The remaining interband $E2$ matrix elements were coupled to the respective $2^+_{K=0^+, \gamma} \rightarrow 0^+_g$ element by eq. (1) and each varied as a single parameter. This approach is similar to the procedures outlined in refs. [18, 19]. The $M1$ and in-band $E2$ matrix elements were coupled as described above. The signs of the start values were selected to correspond to the signs of the Clebsch-Gordan coefficients but were allowed to vary. It should be noted that during the final error analysis, the above constraints were removed and the error calculation was performed individually for each matrix element.

The matrix elements coupling the 2^+ level at 1416 keV and the four negative-parity states showed little sensitivity to the data set. Further, no reliable information regarding the level at 1416 keV could be extracted from the Doppler-corrected spectrum. Evidence for possible band mixing effects on the $K^{\pi} = 1^-$ band were discussed in ref. [5]. The K -selection rules, which would normally hinder transitions from the $K^{\pi} = 2^-$ band to the $K^{\pi} = 0^+$

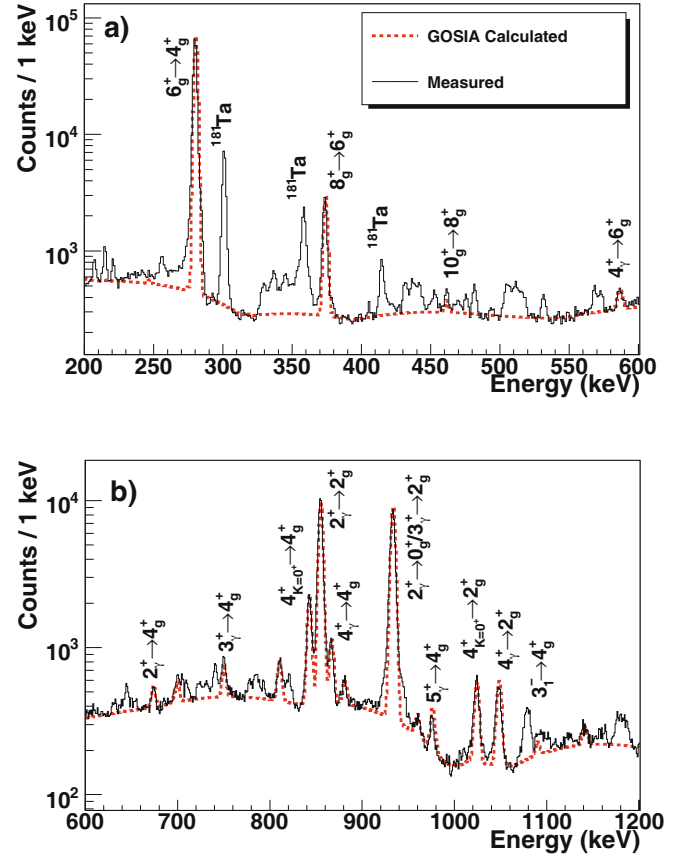


Fig. 3. Calculated spectrum based on the best set of matrix elements as determined from the GOSIA fitting procedure compared with the experimentally measured spectrum. Details related to the generation of the calculated spectrum are given in the text.

band, are broken due to the mixing of the two 4^+ states discussed above [5]. This conclusion is further supported by the observation of the 3^-_{γ} transitions shown in table 1. These challenges make it difficult to draw firm conclusions on the properties of these structures. Therefore, the matrix elements coupling the three lowest bands were fit first and the influence of the higher-lying states was estimated as discussed below.

The coupling scheme described above reduced the number of matrix elements to 19 and a total of 31 experimental data points were defined in the fitting procedure. This includes our 21 extracted γ -ray yields between the three lowest-lying bands, eight previously reported branching ratios listed in ref. [2], and the lifetimes for the 2^+_{γ} and $2^+_{K=0^+}$ states. Lifetimes for the ground-state band were not included as constraints in the fitting procedure and instead these corresponding matrix elements are compared to the fitted results in the next section. The previously known branching ratios and lifetimes are presented in table 2 and were reproduced during the GOSIA fitting procedure to within the 1σ limit. The best fit of the experimental data resulted in a GOSIA calculated χ^2 value of ~ 1.8 and the calculated γ -ray energy spectrum is shown in fig. 3. The calculated spectrum was obtained

Table 3. Reduced matrix elements, given in eb and μ_N , from the GOSIA analysis determined using the coupling scheme described in the text. The error bars for each matrix element are those given by GOSIA. The IBA-1 calculations, described in the text, are given for comparison. The matrix elements marked with footnotes are compared with values from previous measurements.

Transition	GOSIA	IBA-1
Inband $E2$ transition matrix elements		
$2_g^+ \rightarrow 0_g^+$	$2.59_{-0.09}^{+0.05a}$	2.59^h
$4_g^+ \rightarrow 2_g^+$	$4.15_{-0.27}^{+0.08b}$	4.12
$6_g^+ \rightarrow 4_g^+$	$5.23_{-0.15}^{+0.16c}$	5.14
$8_g^+ \rightarrow 6_g^+$	$6.12_{-0.32}^{+0.93d}$	5.92
$4_\gamma^+ \rightarrow 2_\gamma^+$	$2.70_{-0.08}^{+0.37}$	2.45
$6_\gamma^+ \rightarrow 4_\gamma^+$	$4.56_{-2.52}^{+0.22}$	4.09
$2_{K=0^+}^+ \rightarrow 0_{K=0^+}^+$	$1.91_{-0.18}^{+0.16}$	2.28
$4_{K=0^+}^+ \rightarrow 2_{K=0^+}^+$	$3.07_{-0.57}^{+0.40}$	3.62
Interband $E2$ transition matrix elements		
$2_\gamma^+ \rightarrow 0_g^+$	$0.32_{-0.01}^{+0.01e}$	0.32^h
$3_\gamma^+ \rightarrow 2_g^+$	$-0.51_{-0.03}^{+0.11}$	-0.50
$3_\gamma^+ \rightarrow 4_g^+$	$-0.32_{-0.07}^{+0.02}$	-0.36
$6_\gamma^+ \rightarrow 4_g^+$	$0.36_{-0.27}^{+0.03}$	0.31
$6_\gamma^+ \rightarrow 6_g^+$	$0.70_{-0.54}^{+0.53}$	0.70
$2_{K=0^+}^+ \rightarrow 0_g^+$	$0.09_{-0.01}^{+0.01f}$	0.12
Interband $M1$ transition matrix elements		
$2_{K=0^+}^+ \rightarrow 2_g^+$	$ 0.10 _{-0.01}^{+0.01g}$	

^a Previously measured using Coulomb excitation to 2.33(3), 2.48(9), 2.41(2) see refs. [20–22], respectively.

^b Previously measured to 3.74(5) [23].

^c Previously measured to 5.00(11) [23].

^d Previously measured to 5.66(21) [23] and to $\pm 5.93(24)$ ref. [2].

^e Reported value $\pm 0.321(5)$ in ref. [2].

^f Reported value $\pm 0.088(5)$ in ref. [2].

^g Reported value $\pm 0.099(8)$ in ref. [2].

^h This matrix element was used to normalize the results of the IBA-1 model calculation.

by fitting the background of the Doppler-corrected spectrum shown in fig. 1 and adding the GOSIA calculated yields. The yields were Gaussian broadened to meet the experimentally measured FWHM as a function of energy. The $4_{K=0^+}^+ \rightarrow 2_g^+$ transition was used to normalize the two spectra to each other.

4 Results and discussion

A reduced set of matrix elements with correlated errors was determined as described above. They are shown in tables 3 and 4. The matrix elements indicated with foot-

Table 4. Individually fitted reduced matrix elements, given in eb, from the GOSIA analysis. The errors are those given from GOSIA. The predictions of eq. (1) along with the IBA-1 calculations, discussed in detail in the text, are given for comparison. The predictions of eq. (1) were calculated using the $2^+ \rightarrow 0_g^+$ matrix elements for the two bands given in table 3. The matrix elements marked with footnotes are compared with previous measurements.

Transition	GOSIA	eq. (1)	IBA-1
Interband $E2$ transition matrix elements			
$2_\gamma^+ \rightarrow 2_g^+$	$0.41_{-0.01}^{+0.01a}$	0.38	0.40
$2_\gamma^+ \rightarrow 4_g^+$	$0.09_{-0.01}^{+0.01b}$	0.09	0.10
$4_\gamma^+ \rightarrow 2_g^+$	$0.14_{-0.01}^{+0.01}$	0.33	0.31
$4_\gamma^+ \rightarrow 4_g^+$	$-0.05_{-0.07}^{+0.07}$	0.57	0.59
$4_\gamma^+ \rightarrow 6_g^+$	$0.25_{-0.02}^{+0.02}$	0.17	0.21
$0_{K=0^+}^+ \rightarrow 2_g^+$	$0.04_{-0.01}^{+0.01}$	0.09	0.13
$2_{K=0^+}^+ \rightarrow 2_g^+$	$-0.05_{-0.03}^{+0.03c}$	-0.11	-0.15
$2_{K=0^+}^+ \rightarrow 4_g^+$	$0.22_{-0.02}^{+0.01d}$	0.14	0.22
$4_{K=0^+}^+ \rightarrow 2_g^+$	$0.33_{-0.01}^{+0.01}$	0.14	0.17
$4_{K=0^+}^+ \rightarrow 4_g^+$	$-0.96_{-0.05}^{+0.04}$	-0.14	-0.19

^a Reported value > 0.413 in ref. [2].

^b Reported value $\pm 0.09(1)$ in ref. [2].

^c Reported value $|0.04|_{-0.02}^{+0.03}$ in ref. [2].

^d Reported value $\pm 0.199(14)$ in ref. [2].

notes are compared to previous measurements in order to evaluate the fit. The value of the $2_g^+ \rightarrow 0_g^+$ matrix element is compared with three other Coulomb excitation measurements [20–22]. The deviation between the two measurements, reported with the highest accuracy, of $\langle 2_g^+ \| E2 \| 0_g^+ \rangle = 2.33(3)$ and $\langle 2_g^+ \| E2 \| 0_g^+ \rangle = 2.41(2)$ is $\sim 3-4\sigma$. Our measurement deviates from the largest previously reported value of $\langle 2_g^+ \| E2 \| 0_g^+ \rangle = 2.48(9)$, by $\sim 1\sigma$. The interband matrix elements are in good agreement with previously reported values.

In table 4 the predictions of eq. (1) are also shown for comparison. The largest deviations for the individually varied matrix elements from the predictions of eq. (1) are for the 4^+ state transitions of the $K^\pi = 0^+$ band and γ -band. The $4_{K=0^+}^+ \rightarrow 4_g^+$ transition is enhanced significantly and exhibits a matrix element corresponding to a transition probability of $B(E2, 4_{K=0^+}^+ \rightarrow 4_g^+) = 18_{-2}^{+2}$ W.u. This is possibly due to the mixing discussed below. The $E2/M1$ mixing ratio for this transition, extrapolated from the $M1$ matrix element in table 3 and eq. (4-254) in ref. [3] is $|2.67|_{-0.26}^{+0.19}$. This value is similar to the previously reported value of $+2.81(10)$ [24]. The current analysis was not sensitive to the sign of the $M1$ matrix element.

The width of the final χ^2 minimum was investigated by randomly selecting the initial values of the $M1$ intrinsic matrix elements along with the uncoupled $E2$ interband

matrix elements and repeating the minimization several times. The sign conventions were first kept as described above but were later allowed to vary during the minimization. The procedure revealed the existence of other local minima but each with a higher χ^2 value than the best set presented here. The phases of the individually fitted matrix elements were evaluated by flipping the signs and restarting the minimization. In the majority of the cases, flipping the sign of a single-matrix element in the final set resulted in a larger χ^2 value or no significant change in the χ^2 value at the resulting minimum. The only exception being the sign of the $2_{\gamma}^+ \rightarrow 2_g^+$ matrix element which resulted in a slightly lower χ^2 value but no significant change in the measured matrix elements. The positive sign is however preferred as this choice agrees with both eq. (1) and the IBA-1 calculations described below.

The influence of the three higher-lying bands on the $K^{\pi} = 0^+$, γ - and ground-state band matrix elements was investigated by fixing the values coupling these transitions to the lower bands and observing changes in the final set of matrix elements. All states indicated in fig. 2 were included in the procedure along with an additional 5^- state in the $K^{\pi} = 2^-$ band. Estimates have been used to set the values of these matrix elements using data from nearby nuclei when possible. Little effect on the best set of matrix elements was observed.

Calculations using the IBA-1 model have been carried out using the program packages PHINT and FBEM [25]. Previously, comparisons with measured reduced matrix elements for the 2^+ states in ^{170}Er and the IBA-1 model were carried out in ref. [26]. It is now possible to extend the comparison to higher-lying states in both bands. The parameters used in the calculations are the following; PAIR = 1.06 keV, ELL = 17.08 keV, QQ = -21.23 keV as given in ref. [26]. The parameters E2SD and E2DD were calculated using the experimental $B(E2)$ values for the transitions $2_g^+ \rightarrow 0_g^+$ and $2_{\gamma}^+ \rightarrow 0_g^+$. Their values were: E2SD = 0.1565 eb, and E2DD = -0.162 eb. The calculated energy levels are in excellent agreement with the energy levels for the γ - and $K^{\pi} = 0^+$ bands shown in fig. 2, with the largest deviation between the $6_{K=0^+}^+$ energies of ~ 60 keV. The resulting IBA-1 matrix elements are listed in tables 3 and 4. The majority of the interband matrix elements are well accounted for by the IBA-1 calculations. There however remains a discrepancy for the 4^+ states of the $K = 0^+$ and γ -bands.

One unique feature of the IBA-1 model, compared to the geometric collective model, is the prediction of collective transition probabilities between the lowest-lying $K^{\pi} = 0^+$ band and the γ -band. The influence of including matrix elements between these two bands has been explored further. The minimization was restarted using the final set of matrix elements and fixing an intrinsic matrix element between the $K^{\pi} = 0^+$ and γ -bands of $\langle K_2 = 2 | E2 | K_1 = 0 \rangle = |0.16|$. This matrix element was calculated from the $2_{\gamma}^+ \rightarrow 0_{K=0^+}^+$ predictions of the IBA-1 model. The individual interband matrix elements were assumed to follow the relation provided by eq. (1). The most significant effect on the final set of matrix elements

was observed for the $0_{K=0^+}^+ \rightarrow 2_g^+$ matrix element, which changed by a maximum of 0.03 eb depending on the sign choice for the intrinsic matrix element connecting the two bands. No significant influence on the remaining matrix elements was observed.

The behavior of the interband matrix elements shown in table 4 can be discussed in terms of the band mixing between the three lowest-lying bands. The $E2$ matrix elements between the γ - and ground-state bands are well correlated by eq. (1). The only large deviations being for the 4_{γ}^+ transitions. These deviations could be the result of the near degeneracy of the two $4_{K=0^+, \gamma}^+$ states as was discussed in ref. [1]. The fact that the interband $E2$ matrix elements of the γ -band are well accounted for by eq. (1) indicates that the mixing between the γ - and ground-state bands is rather weak. A similar qualitative analysis for the $K^{\pi} = 0^+$ band transitions is more difficult due to the limited number of experimentally determined matrix elements.

5 Summary

Coulomb excitation has been used to investigate electromagnetic properties of the nucleus ^{170}Er . The $K^{\pi} = 0^+$ band and $K^{\pi} = 2^+$, γ -vibrational band were strongly populated during the experiment. In addition several low-lying octupole vibrations and a $K^{\pi} = 2^+$ state were populated. A set of matrix elements coupling the three lowest-lying bands was deduced using the Coulomb excitation code GOSIA.

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