Pulse shape simulation for segmented true-coaxial HPGe detectors

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Abstract A new package to simulate the formation of electrical pulses in segmented true-coaxial high purity germanium detectors is presented. The computation of the electric field and weighting potentials inside the detector as well as of the trajectories of the charge carriers is described. In addition, the treatment of bandwidth limitations and noise are discussed. Comparison of simulated to measured pulses, obtained from an 18-fold segmented detector operated inside a cryogenic test facility, are presented.

1 Introduction

High purity germanium detectors, HPGeDs, are used in a wide variety of applications in particle and nuclear physics [1, 2]. In particular, they are used for gamma ray tracking in arrays like AGATA [3] and GRETA [4], and in the search for neutrinoless double beta decay in experiments like GERDA [5, 6] and MAJORANA [7].

For neutrinoless double beta decay experiments, it is important to study event topologies in order to separate events with energy depositions in one or multiple locations, single-site or multi-site events. The signal is predominantly associated with single-site events while most background events are multi-site events. The separation can be done using segmentation, i.e. the detector volume is read out through multiple electrodes and thereby divided into individual volumes. The size of the volumes is chosen such, that the multi-site events have a high probability to create signals in more than one segment [8].

The separation of single- and multi-site events for a detector or for an individual segment can also be done by the analysis of pulse shapes, PSA [9–11]. Previous PSA studies were often limited by the availability of clean event samples to train neural networks or to evaluate PSA efficiencies.

Pulse shapes also reveal interesting intrinsic properties of HPGeDs. Simulated events, reflecting a detailed understanding of the underlying processes, are extremely valuable for such studies.

The interactions of radiation (α , β , γ , n , p , etc.) inside a semiconductor create electron-hole pairs. These charge carriers are separated by the electric field inside an HPGeD and drift towards the electrodes inducing time dependent charges. In most applications, charge sensitive amplifiers are used and the resulting pulses are sampled and digitized at a given frequency. The simulation of such pulses has to take into account the physics processes inside the detector and the influence of the electronic readout. The package MGS [12] does this for the detectors optimized for gamma ray tracking in AGATA. These detectors are cylindrical with a closed cap and segmented 36-fold.

A new pulse shape simulation package was developed for the 18-fold, ($6\phi, 3z$), segmented true-coaxial n-type HPGeDs [13] optimized for neutrinoless double beta decay experiments. Here, true-coaxial detectors were chosen because they have a more homogenous electric field. As the signal is created internally, no loss in efficiency like for a beam experiment is encountered. The inner mantle has a radius of 5 mm, the outer of 37.5 mm. The length is 70 mm. This allows the comparison to data obtained from such a detector which was developed in connection with the GERDA [5, 6] experiment. The segmentation scheme was optimized to reduce photon induced backgrounds in neutrinoless double beta decay experiments. However, the simulation package itself is general and the geometry can easily be modified to accommodate any kind of germanium detector. The crystal is, by default, assumed to be n-type, because n-type based segmented detectors are commercially available from Canberra France. Should reliable p-type segmented detectors become available, the package can easily be adjusted.

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2 Simulation procedure

The package [14, 15] is separated into two parts, the calculation of the static properties of the HPGeD followed by the event by event simulation of the pulse development. The tabulation of the static properties is done once at the beginning of the simulation. It includes the electric field and the weighting potentials inside the detector.

The event by event simulation comprises the event topology and the development of the pulses in time-steps:

1. Simulation of the interactions of particles with germanium. The output are individual positions with energy depositions, hits.
2. Clustering of hits. According to the requirements of the simulation, hits can be clustered.¹ The position of the cluster is the bary-center of the original hits. The energy of the cluster, E_{cl} , is the sum of the energies of the original hits.
3. Simulation of the drift of charge carriers in time-steps. For each cluster, only one point-like charge is considered. At each time-step the velocity of the charge is calculated using the electric field as tabulated.
4. Calculation of the charges induced in the electrodes after each step.
5. Simulation of experimental effects such as noise, bandwidth limitation, shaping times, etc.

The first step is done using the GEANT4 [16, 17] based simulation package MAGE [18], jointly developed by the GERDA and Majorana collaborations. The good agreement between MaGe and data obtained for segmented detectors was demonstrated previously for photon and neutron induced events [8, 19] in the range of ≈ 20 keV to ≈ 10 MeV.

All calculations are performed in cylindrical coordinates, r , ϕ and z , with the origin at the center of the detector.

3 Electric field and weighting potentials

The electric field, $E(x)$, at a position $x = (r, \phi, z)$ inside an HPGeD depends on the geometry of the detector, the bias voltage, V_{bias} applied and the density of electrically active impurities, $\rho_{imp}(x)$. It is considered static, calculated only once and tabulated for a reasonably spaced grid.² The electric field at any position is calculated by interpolation.

For simple cases like a constant $\rho_{imp}(x)$, $E(x)$ can be calculated analytically solving Poisson's equation $\nabla \cdot E(x) =$

$\frac{\rho(x)}{\epsilon}$, where $\rho(x)$ is the space charge density ϵ is the dielectric constant. However, the electric field is always calculated numerically using the potential $\varphi(x)$ and the boundary conditions.

The boundary conditions for φ depend on V_{bias} . For the true-coaxial n -type HPGeDs considered here, the potential is fixed to V_{bias} on the inner mantle, zero on the outer mantle and it floats on the end surfaces. The lithium drifted zone around the inner mantle and the volumes taken up by the implantations on the outer mantle are implemented in the geometry and the boundary conditions are modified accordingly.

The density $\rho_{imp}(x)$ determines $\rho(x)$ and thereby affects the electric field inside an HPGeD. In the case of constant ρ_{imp} , the electric field only depends on r . For this case, the output of the numerical calculation based on successive over-relaxation was tested against the numerical solution [15]. The deviations for realistic values of $\rho_{imp}(x)$ were found to be less than 0.6% throughout the detector.

Figure 1 shows the calculated strength of the electric field as a function of r for $V_{bias} = 3$ kV and varying constant ρ_{imp} . This range of ρ_{imp} values is realistic for HPGeDs. For lower ρ_{imp} , the field is strong throughout the detector. For higher ρ_{imp} , the field is insufficient at small radii; a higher V_{bias} is needed.

As $\rho_{imp}(x)$ can vary up to a factor three between the two ends of a detector and might depend on r , it is possible to specify a three dimensional distribution for $\rho_{imp}(x)$.

The influence of any electrode on a given space-point inside the HPGeD is characterized by its weighting potential. This is defined according to Shockley-Ramo's theorem [20–22] as the solution of Poisson's equation for the boundary conditions that the potential on the electrode of interest equals unity and the potentials on all other electrodes equal zero. All weighting potentials are treated numerically like the electric field.

Fig. 1 Strength of the electric field as a function of the cylindrical coordinate r for constant impurity densities between 0.3 and $1.3 \times 10^{-10}/\text{cm}^3$

¹Hits closer to each other than the best hypothetical radial resolution of the detector, 1 mm, calculated as the speed of the charge carriers multiplied by the time resolution of the electronics, are clustered by default.

²The default is a grid with a 1 mm spacing in r and z and a two degree spacing in ϕ .

4 Drift of charge carriers

The drift of the charge carriers is calculated in time-steps, Δt , for each point representing a cluster of hits as defined in Sect. 2. At each step the velocity is calculated using the electric field as tabulated. Between grid points a simple linear extrapolation is used for the electric field. Two different numerical methods are implemented to calculate the trajectories, the Euler method and the 4th Runge-Kutta method. The former is less computer time intensive, but is also less precise. However, for step-sizes $\Delta t < 1$ ns, the resulting trajectories do not differ significantly [14].

The drift velocity of the charge carriers, $v_e(x)$ for electrons and $v_h(x)$ for holes, is calculated for each step using the electric field, $E(x)$, as tabulated:

$$v_{e/h}(x) = \mu_{e/h}(x)E(x), \quad (1)$$

where $\mu_{e/h}(x)$ is the mobility [1] of electrons and holes, respectively.

Whether $\mu_{e/h}(x)$ depend on the relative position of x to the crystal axes is determined by the temperatures of the germanium crystal, T_{crystal} , and of the charge carriers, T_{cc} . If $T_{\text{crystal}} \approx T_{\text{cc}}$, $\mu_{e/h}(x)$ become numbers, $\mu_{e/h}^0$ and the drift velocities are directly proportional to the electric field. However, HPGeDs are normally operated at temperatures around 100 K and $T_{\text{crystal}} \ll T_{\text{cc}}$. In this case, the mobility becomes a complex tensor. Therefore, the simulation has to take the crystal structure into account and the calculation of $v_{e/h}(x)$ becomes quite involved. The drift of the charge carriers is not any longer parallel to the electric field [23] for all x .

The axes of the face-centered cubic structure of germanium crystals are characterized by Miller indices [24]. Cylindrical germanium detectors are produced with their z axis aligned to the crystal axis $\langle 001 \rangle$ [25]. This is implemented in the simulation. The axes $\langle 100 \rangle$ and $\langle 110 \rangle$ are in the $r\phi$ -plane. Their relative position to the segment boundaries can be chosen freely, i.e. adjusted to the detector to be simulated.

The tensors $\mu_{e/h}(x)$ are unfortunately not known. Special measurements along the crystallographic axes are used and parameterized. The results are combined to get results for any point in the crystal.

If the electric field is parallel to any of the principal crystallographic axes, the charge carriers will drift along this axis, because of the symmetric structure of the germanium crystal [23, 26]. The measured drift velocities [27–29], $v_{e/h}$, along the axes $\langle 100 \rangle$ and $\langle 111 \rangle$ with $E(x) \parallel \langle 100 \rangle$ for x on $\langle 100 \rangle$ and $E(x) \parallel \langle 111 \rangle$ for x on $\langle 111 \rangle$, respectively, are parametrized well [1, 28] for $E = |E(x)| < 300$ V/mm by

$$v_{e/h} = \frac{\mu_{e/h}^0 E(x)}{[1 + (\frac{E(x)}{E_0})^\beta]^{1/\beta}}, \quad (2)$$

Table 1 Parameters for the experimental drift velocities in the $\langle 111 \rangle$ and $\langle 100 \rangle$ directions used in the simulation

Carrier	Axis	μ_0 [$\frac{\text{cm}^2}{\text{V}\cdot\text{s}}$]	E_0 [$\frac{\text{V}}{\text{mm}}$]	β
e	$\langle 111 \rangle$	38536	53.8	0.641
	$\langle 100 \rangle$	38609	51.1	0.805
h	$\langle 111 \rangle$	61215	18.2	0.662
	$\langle 100 \rangle$	61824	18.5	0.942

where $\mu_{e/h}^0$, E_0 and β are parameters determined by fitting. The parameters $\mu_{e/h}^0$ represent the linear relation between v and E at large T_{crystal} and low E . The parameters E_0 and β are used to model the deviation from this linear relation at low lattice temperature and high electric fields.

The set of parameters given in [27] and validated for the drift of electrons [30] was used in the simulation presented here. The values are listed in Table 1.

The drift velocities in any direction can be derived from the velocities along the $\langle 111 \rangle$ and $\langle 100 \rangle$ axes. The model used for the electron drift [28] is based on the idea that the conduction band in a germanium crystal reaches its minimal potential in regions around the four equivalent $\langle 111 \rangle$ axes. Free electrons effectively only populate these regions. The probability density of free electrons in other regions can be ignored. The resulting drift velocities along the $\langle 110 \rangle$ axis are shown together with the velocities for the $\langle 111 \rangle$ and $\langle 100 \rangle$ axes in Fig. 2(a).

The model used to calculate the hole drift velocities [27] in any direction is based on the idea that only the “heavy hole valence band” [31] is responsible for the anisotropy of the mobility. All other effects are neglected. A parameterization [27] is used to calculate the three components of the hole drift velocity v at any position. The results for the $\langle 110 \rangle$ axis together with the values for the $\langle 111 \rangle$ and $\langle 100 \rangle$ axes are shown in Fig. 2(b).

5 Trajectories

The results presented here were obtained with the Runge-Kutta method.

Figure 3 shows the trajectories of electrons and holes created at the outer and inner mantle, respectively. The step size was set to 1 ns and the total time simulated was 400 ns, $V_{\text{bias}} = 3000$ V and $\rho_{\text{imp}} = 0.62 \cdot 10^{10}/\text{cm}^3$ was constant through the volume. The trajectories are bent due to the crystal structure; this is called transverse anisotropy. The charge carriers are slower in the $\langle 110 \rangle$ than in the $\langle 100 \rangle$ direction; this is called longitudinal anisotropy. As holes are slower than electrons, the longitudinal anisotropy can be seen very clearly along $\langle 110 \rangle$ where the holes do not reach the outer mantle within 400 ns.

Fig. 2 Drift velocities of (a) electrons and (b) holes along the principal crystal axes as functions of the electric field. Velocities along the axes $\langle 111 \rangle$ and $\langle 100 \rangle$ are calculated according to (2). For the calculation along $\langle 111 \rangle$, see text

The transverse anisotropy is also demonstrated for electrons in Fig. 4. It shows the displacement $\Delta\phi$ at the end of the drift and the total time needed for the drift as functions of the azimuthal angle ϕ at the start. Along the crystal axes $\langle 110 \rangle$ and $\langle 100 \rangle$, $\Delta\phi = 0$. The drift time is minimal at $\langle 100 \rangle$ and maximal at $\langle 110 \rangle$.

6 Charges induced on electrodes

The electric signals are induced in the electrodes of a detector by the cumulative influence of moving electrons and

Fig. 3 Trajectories of (a) electrons and (b) holes in the $(x, y) = (r, \phi)$ plane for constant ρ_{imp} . Electrons drift inwards and holes outwards

holes. Shockley-Ramo's Theorem [20–22] is used to calculate the time development of the induced charge $Q(t)$ or current $I(t)$ in each electrode:

$$Q(t) = -Q_0 \cdot [\varphi_w(x_h(t)) - \varphi_w(x_e(t))], \quad (3)$$

$$I(t) = Q_0 \cdot [\mathbf{E}_w(x_h(t)) \cdot \mathbf{v}_h(t) - \mathbf{E}_w(x_e(t)) \cdot \mathbf{v}_e(t)], \quad (4)$$

where Q_0 is the electric charge carried by electrons or holes, $x_{e/h}(t)$ and $\mathbf{v}_{e/h}(t)$ are the position and velocity vectors of electrons/holes as a function of time, and φ_w and $\mathbf{E}_w$ are the weighting potentials and weighting fields.

Fig. 4 (a) Displacement $\Delta\phi$ between starting point on the outer mantle and the end point on the inner mantle of the detector as a function of the azimuthal angle ϕ at the start. (b) Total drift-time as a function of ϕ

Fig. 5 Weighting potential of segment B together with an indication of a γ interaction

Figure 5 shows the weighting potential of a segment, B, with the indication of a photon interaction. The drift trajectories of holes and electrons are also indicated. Figures 6(a) and (b) show the charges and currents induced on the elec-

trodes of the segment with the interaction and its neighbors. The pulses induced in the neighboring segments are called mirror pulses. The amplitude of the mirror pulse induced in segment A is larger than the one in segment C since the trajectory is closer to segment A than C.

The charge pulses in segment B and the core show clear kinks at the time when the inwards drifting electrons reach the core electrode, i.e. the inner mantle. At that time the current pulses show maxima. The charge mirror-pulses do not show clear features at this time; the current mirror-pulses show more distinct features.

The position in r of an energy deposit is clearly reflected in the resulting pulses in the segment and core electrodes. This is demonstrated in Figs. 7 and 8.

7 Influence of electronics

The most widely used amplification scheme is based on charge sensitive devices. The bandwidth is limited by the amplifiers and by the transmission cables. In order to account for the limited bandwidth and the decay time of the amplifier, the simulated pulses can be convoluted with a

Fig. 6 (a) Simulated charge and (b) current pulses induced in segments A, B and C and the core for the gamma interaction depicted in Fig. 5

Fig. 7 Simulated charge pulses in the segment electrode for charges deposited at different radius, r

Fig. 8 Simulated charge pulses in the core electrode for charges deposited at different radius, r

Fig. 9 Pulses at different stages of the simulation: (a) Raw pulse, (b) after folding in the decay time of the signal, (c) after convolution with the bandwidth and (d) after adding noise

transfer function representing the readout electronics. In addition, Gaussian noise can be added to represent the noise of the system.

Figure 9 demonstrates the modification of a simulated pulse after folding in a decay time of 5 μ s and a cut-off in bandwidth of 10 MHz. The value of the cut-off was chosen to clearly demonstrate the effect. The noise level was set to 0.5% of the pulse amplitude. This noise level was generally achieved for pulses with an energy of about 1 MeV.

The decay-time of the preamplifier was chosen significantly larger than the length of the pulse. Therefore, mainly the plateau is affected. The cut-off in bandwidth smooths the features of the pulse. The kink clearly visible at $t = 150$ ns in Fig. 9(b) is washed out significantly. The noise applied for Fig. 9(d) makes the kink almost invisible.

8 Uncertainties of the simulation

The output of the simulation depends critically on the input parameters used. A fundamental problem is the input concerning the mobilities. Figure 10 demonstrates how the pulses of events starting at the outer mantle and observed in the core are stretched if a different set [28] of input parameters for the electron mobility is chosen. At $V_{\text{bias}} = 3000$ V and $\rho_{\text{imp}} = 0.66 \cdot 10^{10}/\text{cm}^3$, the pulse is 14% longer than with the default input parameters [27]. However, a simple time scaling makes the pulses indistinguishable.

The length of a pulse is also strongly influenced by ρ_{imp} . This is demonstrated in Fig. 11. At $V_{\text{bias}} = 3000$ V a change in ρ_{imp} from $0.66 \cdot 10^{10}$ to $0.83 \cdot 10^{10}/\text{cm}^3$ has an effect on the core pulse of similar size than changing the mobility. In this case, the shape of the pulse is also modified; a simple time scaling does not make the pulses indistinguishable. However, the effect is quite subtle and will be difficult to observe in real data. Unfortunately, the value of ρ_{imp} is generally not known to very high precision. In addition, it often varies up to a factor of three along z . Therefore, it is unavoidable that pulses simulated for a particular detector or even detector section have to be scaled in time before more detailed comparisons to data can be made. Assuming a certain mobility, the length of the measured pulses can be used to derive the impurity density locally.

9 Comparison to data

The focus of the comparisons presented here is the drift of electrons. Therefore pulses as seen in the core electrode were used. Simulated pulses were compared to measured pulses produced by a well understood true-coaxial n -type detector [13] irradiated with a collimated Europium source. The 122 keV line was used to study energy deposits close to the detector outer mantle. In this case, the holes are quickly absorbed by the electrodes on this outer mantle and mainly the drift of the electrons is relevant for the shape of the resulting pulses. Further studies with other sources aiming at other aspects of pulse shape development are under way. These studies will include comparisons between predicted and measured mirror charges.

Two methods were used. Simulated pulses were either fitted to individual measured pulses or to averages of sets of pulses obtained in a given configuration. The latter was done to reduce the effects of noise.

Fig. 10 Simulated core pulses for two different sets of input parameters for the electron mobility. The result of a time scaling of the longer pulse is also shown

Fig. 11 Simulated core pulses for different impurities, ρ_{imp}

9.1 Test environment

Figure 12 depicts the measurement setup. Three segments, numbered 13 to 15, of the middle layer of the detector were scanned in ϕ at $z = 0$. A collimated 75 kBq ^{152}Eu source inside a copper collimator was used. The collimator pointed to the center of the detector and the spot had a 1σ diameter of about 5 mm on the outer mantle of the detector. Details of the setup can be found elsewhere [13]. The operational voltage was 3 kV. The step size of the scan was 5° in segment 14 and 10° in segments 13 and 15. The uncertainty in ϕ was approximately $\Delta\phi = 2.5^\circ$. In total, 25 steps were made to cover 180° in azimuth. The pulses of the core and all segments were recorded. Events from the 122 keV γ -line were selected with a cut on the core energy of 2σ of the energy resolution, i.e. about ± 4 keV.

Simulations were done with the energy deposits located exactly on the outer mantle or distributed according to the

Fig. 12 Schematic of the setup used to scan three segments of an $(6\phi, 3z)$ segmented detector at $z = 0$

interactions of the 122 keV photons from the ^{152}Eu source. A constant $\rho_{\text{imp}} = 1.05 \cdot 10^{10}/\text{cm}^3$ was implemented. This is the average of the values given by the manufacturer for the top and the bottom of the detector which differ by a factor of two. The electric field was calculated for a bias voltage of $V_{\text{bias}} = 3$ kV. The measured orientation of the crystal axes was used in the simulation; the $\langle 110 \rangle$ axis was set to 290° , almost aligned with one boundary of segment 15.

An amplifier decay-time of 50 μs and a cut-off in bandwidth of 37.5 MHz were implemented according to the specifications of the electronics system. Electronic noise was not added to the simulated pulses to simplify direct comparisons with individual measured pulses.

9.2 Fits to individual pulses

Simulated core pulses, $C_{\text{sim}}(t)$, were fitted to measured pulses, C_{meas} , using three parameters only: the amplitude, A , the time offset, T_0 , and the time scaling-factor T_{scale} :

$$C_{\text{meas}}(t) = A \times C_{\text{sim}}(t/T_{\text{scale}} + T_0). \quad (5)$$

Figure 13 shows a randomly selected core pulse at $\phi = 200^\circ$ and the fit of the pulse generated for this angle. This position falls between the $\langle 110 \rangle$ and the $\langle 100 \rangle$ axes. The actual values of the parameters A and T_0 have no relevance; they are not simulated in real units. The important parameter is T_{scale} which has a value of 0.90 ± 0.01 . The $\chi^2/\text{dof} = 184/146 = 1.3$ for this fit is quite good.

Figure 14 shows the distribution of χ^2/dof values of all fits of pulses at $\phi = 200^\circ$. The average $\chi^2/\text{dof} = 174/146 = 1.2$. In general, the quality of the fits is very good. This indicates that the simulation describes the general shape of the pulses very well. To determine an overall T_{scale} , a clean subset of measured pulses was selected by:

- requiring $\chi^2 < 220$, i.e. $\chi^2/\text{dof} < 1.5$, to eliminate background events which have probably more than one interaction in the segment;

Fig. 13 Fit of a simulated to a measured pulse at $\phi = 200^\circ$. The dots represent the data with vertical bars indicating the noise level which is about 5% of the amplitude

Fig. 14 χ^2 distribution from the fits of the simulated to measured pulses taken at $\phi = 200^\circ$. Only events with $\chi^2/\text{dof} < 1.5$ are analysed further. The cut is indicated by a vertical line

- rejecting events in which an intermittent DAQ problem might have affected the recording of the pulse.

For each pulse, a value of T_{scale} was determined. Figure 15 shows the distribution of the time scaling-factors of the pulses at $\phi = 200^\circ$. The mean time scaling-factor of 0.91 ± 0.01 was extracted using a Gaussian fit. This was done for all positions in ϕ . Figure 16 shows the ϕ dependence of the mean time scaling-factors. The dotted vertical lines indicate the segment boundaries. A value of $T_{\text{scale}} = 1$, independent of ϕ would be expected for a perfect simulation. However, considering the uncertainties in the input parameters, the level of agreement is quite astonishing. The time scaling-factors are systematically about 10% low. This means that the simulated pulses are too short. The effect

Fig. 15 Distribution of time scaling-factors from the fits of the simulated to measured pulses taken at $\phi = 200^\circ$. The result of a Gaussian fit is shown as a *solid line*

Fig. 16 Mean time scaling-factors, points, as extracted for each ϕ . The uncertainties were taken from the Gaussian fits. The result of a straight line fit to the points is given as a *solid line*

is too large to be caused by an overestimate of the thickness of the lithium drift layer. It indicates that the velocities of the electrons are overestimated. As discussed in Sect. 8, this could be due to too high mobilities assumed or due to a slightly underestimated ρ_{imp} . It is impossible to distinguish the two possibilities at this point.

The ϕ dependence was fitted with a straight line. The absence of an oscillation pattern with a period of 90° shows that the longitudinal anisotropies introduced in the model describe reality in a satisfactory manner. The obvious dependence of T_{scale} on ϕ is difficult to explain. In germanium crystals, ρ_{imp} often depends on r . If the central z -axis of the original crystal is not identical with the z -axis of the detector, a ϕ dependence of the observed average ρ_{imp} can result. A further investigation whether this effect can explain the about 5% effect is under way.

Fig. 17 Fit of the averaged simulated to the averaged measured pulse at $\phi = 200^\circ$. The statistical uncertainties in the averaged measured pulse are too small to be seen

9.3 Fits to averaged pulses

It would be interesting to carefully study the detailed shapes of individual pulses to distinguish between different sources of deviation between simulation and data. However, Fig. 13 shows that the noise level in this measurement does not allow this. In order to remove the effects of noise, the selected pulses at each scan position were averaged, even though the interaction points were spatially distributed according to the beam spot and the penetration depth of 122 keV photons.

The simulation was adjusted accordingly and the simulated pulses were also averaged. Averaged simulated pulses were fitted to averaged measured pulses. The result for $\phi = 200^\circ$ is shown in Fig. 17. The fit yields $T_{\text{scale}} = 0.90 \pm 0.01$. This is compatible with the mean $T_{\text{scale}} = 0.91 \pm 0.01$ observed before.

The χ^2/dof of the fit is ≈ 8 . This is quite large. In Fig. 17, the deviations are also clearly visible. The simulated pulse has sharper edges most likely due to the overly optimistic cut of 37.5 MHz in the bandwidth; Fig. 9 demonstrates how pulses get smoothed out by a cut in bandwidth of 10 MHz. At the very end of the pulse, the simulation shows an extra flattening. This would indicate that ρ_{imp} is slightly smaller than assumed. Nevertheless, the overall shape of the pulse is reproduced rather well and it will be tested soon, how well simulated pulses work as training sets for neural network based pulse shape analyses.

10 Summary and outlook

A fully functional pulse shape simulation package for HPGe detectors was developed. It can easily be adapted to any common HPGe detector geometry. The results of the simulation are critically dependent on the input parameters. While

some parameters are generic to germanium, the detailed properties of a detector like impurity concentration and axes orientation are also extremely important. They have to be given as input for each detector.

The longitudinal anisotropy of the electron drift is correctly described by the simulation. Therefore the comparison of simulated to measured pulses can yield information about intrinsic detector properties like local variations of the impurity concentration.

The comparisons with data presented in this paper mainly concern the electron drift. Further studies are under way, focusing on hole drift and mirror charges. The goal of these studies is to better understand the properties of segmented true-coaxial detectors. The simulated pulses will also be used as input to pulse shape analyses aiming at distinguishing events induced by external photons or electrons from internal beta decays.

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