About the Criteria for the Choice of Materials to Protect Against the Mechanical Dynamic Loading

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Received December 3, 2020; revised January 26, 2021; accepted February 5, 2021

Abstract—A criterion for the selection of materials to protect against the mechanical dynamic loading is proposed and substantiated. The mechanisms of the fracture of brittle ceramic materials that are widely used in structures that prevent penetration and are very common in practice are discussed. Unlike other estimates, the proposed formula is based on the physical principle of comparing the total energies of loading and obstacles, and is in good agreement with the experimental data.

Keywords: barrier, elastic properties, ceramics, penetration depth **DOI:** 10.1134/S1087659621040179

INTRODUCTION

The criterion is understood to mean the ability of the material to absorb, dissipate, and transform the loading energy. For example, for a projectile with a diameter (caliber) of 12.7 mm, this energy is \sim 17 kJ (at a loading rate of about 900 m/s and an indenter mass of 46 g).

M. Ashby published the classic work "Selection of materials for the design of technical applications" [1] in 1993 and introduced M (the material index M), which in a semiquantitative form allows us to evaluate materials for security applications, where *E* is Young's modulus, ρ is density, and C_1 is the longitudinal speed of sound in matter.

$$M = \frac{E^{\frac{1}{2}}}{\rho} = \frac{C_1}{\rho^{\frac{1}{2}}},$$

This index is valid (according to Ashby) under conditions of quasi-static loading. At high loading rates, the entire amount of loading energy is distributed over a short period of time throughout the entire volume of the material. To prevent the destruction of the material (structure) and exclude penetration, this energy must be absorbed due to elastic and inelastic deformations, the mechanism of destruction, phase transitions, chemical reactions, and other mechanisms.

ANALYTICAL PART

Let us consider the process of interaction between the projectile and the obstacle sequentially.

For most ceramics, the elastic wave resulting from a high-velocity impact consists of surface waves (Rayleigh waves), shear waves (S-waves), and compression waves (P-waves). The wave energy of loading is roughly divided in the following ratio: Rayleigh wave, 67%; S-wave, 26%; and compression wave (P-wave), 7% [2].

The overall picture of impact is very complex and involves several processes.

At average speeds ($v_{sp} \ll C_1$) the material of the striker undergoes deceleration due to destruction (dwell), the material of the barrier is destroyed due to the Hertz formation of radial and circular cracks, as well as the formation of Mescal zones and grinding of ceramics in them. In these zones, the plasticity of ceramics (or quasi-plasticity) plays an important role. The table from [2] presents estimates of the energy consumption of an impact on a ceramic barrier in combination with a substrate (two-layer)¹. All stages indicated in the table are related to the elastic properties of the barrier. The term *quasi-plasticity* was analyzed in [3] and the term *brittleness index*, which is defined as the magnitude of the shear stress for the

¹ This term was introduced by V.Ya. Shevchenko in 1981. In the English-language literature, this design is called "Tandem."

Dwell (destruction

Platinum thickness	energy absorption)	of the drummer)	(Mescal zones)	zones)	absorption energy)	
Thin	10	40	25	5	20	
Thick	10	30	35	20	5	
onset of brittle fracture with the formation of cracks. tors such as the projectile speed, substrate design, and						

destruction

 Table 1. Impact energy distribution [1]

Platinum thickness

onset of brittle fracture with the formation of cracks, was introduced (Table 1).

Impact (elastic

Quasi-plasticity can be defined as "all elastic deformations before the catastrophic failure of microcracks" [4] arising from various mechanisms—nano and micro—i.e., twinning, dislocations, grain boundaries, depreciation, microcracks, chips, phase transitions, micromelting, and dissociation.

The distribution of energy in a two-layer ceramic and aluminum by projectile of small diameter shows that the energy consumption of the projectile for the destruction of ceramics is insignificant (2-10%). The main mechanism of energy dissipation is the plastic deformation of the substrate (20-40%) and the impactor (10-15% dwell), as well as the fracture energy of ceramics due to the formation of spalling (40-70%) [5].

The term spalling refers to the grinding of a material from one particle size to a smaller particle size by breaking, crushing, cutting, vibratory grinding, and other processes. This phenomenon on impact is typical for fragile bodies.

Upon impact, a destruction region forms in front of the striker and remains in the conoidal destruction zone. This zone is called the Mescall zone. Mescall was the first to describe this phenomenon under supersonic impact, but it is also observed for normal loading rates.

When a striker strikes a brittle body, the fracture's conoid, radial cracks, and circular cracks are formed [6]. Such a cone is called a Hertzian cone.

For corundum, it was determined that, on average, one radial crack corresponds to a fraction of ~ 150 MPa of the developing hoop stress. The number of large radial cracks is also dependent and reflects the bending points that appear in a brittle body. They form as some kind of concentric circles around the impact site and appear after the radial cracks, but they have a common nature. The geometry of the sample significantly affects the process of destruction of the target and, under appropriate conditions, can lead to the complete erosion of the projectile (Dwell).

According to [7], it was found that the cone angle increases with an increase in Poisson's ratio for large diameter strikers and thus has a higher ballistic efficiency. When Poisson's ratio changes from 0.1 to 0.3, the angle changes from 60° to 70° . However, other fac-

tors such as the projectile speed, substrate design, and stiffness also affect the taper angle of the failure.

obstacle (Mescal

Substrate stiffness

(substrate

Spalling Hertzian Spalling shredding

The base of the Hertz cone is approximately half the projectile diameter plus twice the plate thickness [8].

Two stages of fracture exist in a material subjected to dynamic loading at high loading rates ($v_{sp} \ge C_l$). At the second stage, when the values of the loading speed become of the order of the longitudinal speed of sound (different for different types of materials), the effects related to the distribution of shock waves prevail. A decrease in the loading rate leads to destruction due to inertial effects, and the adiabatic response of the obstacle leads to melting. At this stage, an increase in the loading energy often leads to melting or evaporation of part of the barrier. For ceramics at loading rates suitable for the corresponding barriers, the response to an elastic wave is the governing process. In the elastic mode, the pressure arising in the compression wave is linearly proportional to the velocity of the material particle, the constant of proportionality is known as the elastic impedance equal to the product of the density and the velocity of the shock wave, and the velocity of the particle is equal to the velocity of the contact surface. The ratio of the target thickness to the projectile thickness is the factor determining the superposition of the compression and rarefaction waves. The dependence of the compression of real bodies on the pressure during compression by impact is determined by the Hugoniot function and characterizes the material on the stress-strain curve as the Hugoniot elastic limit (HEL), at which the material begins to transform into irreversible shear.

In ceramics, the HEL is much higher than the crushing strength, which tends to zero as the pressure of the compression pulse approaches the HEL. In general, the HEL can be expressed as $\Delta_{\text{HEL}} = (1 - \upsilon)Y_c/(1-2\upsilon)$, where Y_c is the compressive strength under uniaxial compression and υ is Poisson's ratio. This is analogous to the static loading of ceramics, which have very high compressive strength and very weak tensile strength.

Thus, the factors influencing the energy dissipation in the target are the elastic impedance and HEL. Other factors are the density, modulus of elasticity, and static compressive strength or hardness.

However, all these quantities are related by simple relations with dynamic properties [9].

The quantities E, G, v, and K are related by the ratios

$$G = E/2 (1 + \upsilon),$$

$$K = E/3 (1 - 2\upsilon).$$

In turn,

$$\upsilon = \frac{1 - 2\left(\frac{C_t}{C_1}\right)^2}{2 - 2\left(\frac{C_t}{C_1}\right)^2}, \quad E = \frac{C_t^2 \rho [(1 + \upsilon)(1 - 2\upsilon)]}{(1 - \upsilon)}, \quad G = C_t^2 \rho.$$

where *E*, *G*, υ , and *K* are Young's modulus, the shear modulus, Poisson's ratio, and the bulk modulus, respectively, and *C*₁ is the longitudinal speed of sound, *C*_t is the transverse speed of sound, and usually in isotropic solids the formula $C_1 \approx \sqrt{2} C_t$. It also for a shear wave that

$$C_{1} = \sqrt{\frac{E(1-\nu)}{\rho(1+\nu)(1-2\nu)}} = \sqrt{(K+\frac{4}{3G})}/\rho,$$
$$C_{t} = \sqrt{\frac{E}{2\rho(1+\nu)}} = \sqrt{\frac{G}{\rho}}.$$

All elastic constants in a solid are determined mainly by the velocities of the longitudinal and transverse sound waves, and are interrelated. Compression shockwaves ultimately bounce off the back surface as extensional waves. This dampens the compression waves in the material. The interference of compression and extension waves enhances the stretching at the appropriate locations of the barrier and leads to a fracture (delamination). This phenomenon is called spalling.²

When a wave travels through a high impedance plate that is coupled to a low impedance plate, tensile waves are emitted from the interface. This leads to structural failure if the high impedance plate is brittle. In the opposite case, if the wave initially passes through a low impedance plate coupled to a high impedance plate, then the compression waves are obviously reflected from the interface. This can be useful if we want to suppress a fracture in a brittle material such as ceramics.

The substrate material must withstand large plastic deformations before the fracture. The impact impedance Z of the material is defined as

$$Z=p_0U_{\rm s},$$

where p_0 is the density and U_s is the velocity of the shock wave and is quite similar to the elastic impedance

$$Z = pC_0,$$

where C_0 is the volumetric speed of sound in the material. For the case when elastic waves propagate with the longitudinal speed of sound, then C_1 is used. The elastic impedance will be equal to

$$Z = p_0 C_1$$
.

During the first stage of penetration, $0-9 \mu/s$, cracks are formed near the ceramic–substrate interface due to the shear stresses of the substrate and begin to expand in the direction of motion of the projectile. Between 9 and 15 μ/s , the impactor degrades, and the ceramic breaks down due to multitude of cracks that intersect and join. Approximately 40% of the projectile mass and energy is spent on destruction. After 15 μ/s , the erosion of the projectile stops, and the rest of the energy is absorbed by the substrate [10].

The third type of waves can exist near the surface. These waves were investigated by Rayleigh [11], who showed that their action rapidly decreases with depth and their propagation speed is less than that of bulk waves. Usually, under some assumptions, the speed of the Rayleigh wave is

$$C_R = 0.9194C_{\rm t}$$

where C_t is the speed of transverse waves. In a more general form, we can write

$$C_R/C_t = (0.87 - 1.12\upsilon)/(1 + \upsilon),$$

where υ is Poisson's ratio.

The distribution of the excitation energy of a sound wave at the axial normal load is shown in Fig. 1 (at v = 0.6) [12].

The issue of the maximum limiting fracture velocity has been discussed and investigated many times. All of these works can be divided into four groups, in general, reflecting four groups of solids.

Griffiths believed that crack growth begins with the speed of elastic waves.

Mott obtained the following expression for the maximum possible fracture rate of a crack with the initial length l_0 [13]:

$$V_{\max} = \sqrt{\frac{2\pi E}{k\rho}} \left(1 - \frac{l_0}{l}\right)^{1/2},$$

where *l* is the final crack length.

Coefficient
$$\sqrt{\frac{2\pi}{K}}$$
, is about 0.3 and at $l \ge l_{0}$,
 $v = 0.38 \frac{C_1}{\frac{1}{\rho^2}}$,

which is very similar to Ashby's parameter M.

The third group of works is based on the proposal, according to which the limiting velocity of a crack is limited by the velocity at which the branching process begins, which is approximately 0.6 times the velocity of the transverse

In the last group, the maximum crack velocity is identified with the propagation velocity of Rayleigh waves. A review of these works is presented in detail in [14]. It is known that when a pulsed load is applied,

² See above.

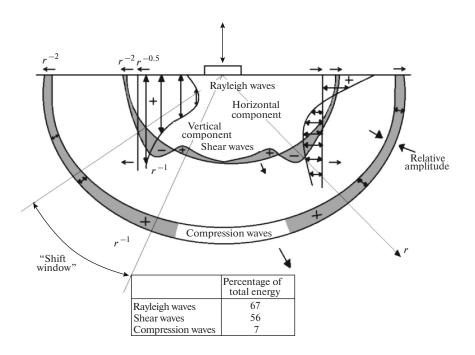


Fig. 1. Distribution of elastic waves in a solid from [10].

crack growth accelerates sharply. According to the estimates in [15],

$$r = \sqrt{\rho C_{\rm t}^{3/2}},$$

where *r* is the radius of destruction of an ideally brittle infinite body caused by an axial impulse

$$\rho = 2\pi r_0 q \Delta t,$$

where r_0 is the radius of the indenter diameter, q and Δt are the average value of the energy and time of interaction of the indenter and the obstacle, and it is assumed that the radius of destruction r is much larger than the radius of the initial hole r_0 .

A brittle cleavage always contains numerous steps and tongues, which are a consequence of cleavage on the cleavage plane, twin plane, and the intersection of a crack with screw dislocations. In addition, such steps can appear when a crack crosses the boundaries of subgrains and weakly misoriented crystallites. The following definition can be put forward: a fracture is brittle if the elastic energy of the destroyed body is sufficient for its flow and completion.

It is difficult to imagine the initiation of microcracks in crystalline materials bypassing the stage of plastic deformation. If plasticity is required for crack initiation, then its role is not significant during crack propagation. It is always possible to imagine the opening of a fast crack due to the elastic rupture of bonds at the mouth of the crack. The loads there are close to the theoretical strength.

A fracture can remain brittle if there is a supercritical stage of avalanche quasi-elastic crack growth, when its high propagation velocity excludes the possibility of using the impact energy and the only source of elastic energy for feeding the crack is the long-term decay of the stress field of the target itself after impact [14].

Inelastic deformation leads to the following stages of destruction, depending on the magnitude of the applied stress:

 An axial fracture of the target due to macroscopic cracks expanding in the direction of axial compression in the absence of any lateral loading;

- Formation of defects or macroscopic shear failure;

Viscous flow under conditions of sufficiently large axial compression.

The transition from a brittle to ductile fracture occurs when a microscopic deformation of the target becomes more uniformly distributed in the volume [14].

Let us define *viscosity* as

$$\Delta = K_c / \tau_v \left(\pi c \right)^{1/2},$$

where K_c is approximately equal to the Griffiths coefficient and τ_y is the shear stress. The value of Δ at room temperature for viscous materials, such as steels or aluminum, is quite large (3–4 for steels and somewhat higher for aluminum in the presence of microcracks of the order of the grain size). For crystalline bodies with microcracks, the value of Δ is quite small, on the order of a few hundredths. These materials are thus "brittle," although their brittleness or toughness will also depend on the values of the loading ratio Z_1 to the load at the mouth of crack Z_2 , where l_0 is the crack's length at the beginning of the growth, L is the crack's length, and the characteristic coefficient l/l_0 is less than one.

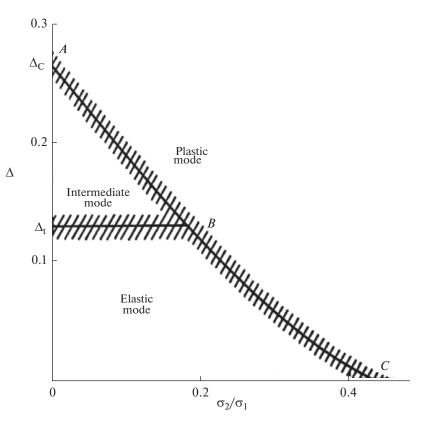


Fig. 2. The brittle-ductile transition diagram from [14].

Figure 2 shows the diagram of the brittle-ductile transition from [16].

An accurate model must describe the various inelastic processes in order to use the appropriate laws and equations. For example, a uniaxial model of splitting and defect formation under various constraints was considered in [17] and founded the development of microcracks in the deformation—stress plane. However, when moving into three-dimensional space, such an analysis is very difficult.

RESULTS OF THE STUDY AND THEIR DISCUSSION

In [14], a micromechanical model for highly deformed ceramics based on the formation of noninteracting microcracks uniformly distributed in the volume is presented.

In general, these four basic concepts can be presented as a theoretical basis for describing the inelastic fracture of ceramics.

In the first representation, the material is presented as elastic and the stresses are calculated based on Hooke's law.

In the second one, stresses are estimated that tend to zero when the variable in the equation of state reaches the critical value. The behavior of ceramics under load can be either elastic or elastic-plastic. The third view considers ceramics as an elasticplastic medium, and uses the same conditions and equations of state as for metals.

The fourth is based on the statistical description of the number of cracks per unit volume as a function of position, crack size, and orientation with respect to the direction of the deformation.

A detailed review of these works is presented in [17].

Together with [16], these concepts, despite their obvious limitations (model), unequivocally indicate that the plastic (i.e., nonlinear relationship between the stress and strain) behavior of ceramics is a consequence of brittle grinding and is determined by the breaking of the interatomic bonds between the particles. This problem was posed and solved in [18].

A long, thin undeformed rod (projectile) (density ρ_c , length *l*, and area *S*), which moves along its axis at speed v_c and meets a semi-infinite solid body (density ρ_n) was considered. The interaction occurs along the normal to the surface, and all the mechanical energy of the rod is spent on the dissociation (atomization) of the substance (*D*).

In [18] it was obtained that

$$l_{\rho} = 0.25 V_l \rho \sqrt{2D/M},$$
$$\varepsilon_{\rho} = l_n \times 2/V_l \sqrt{2D/M},$$

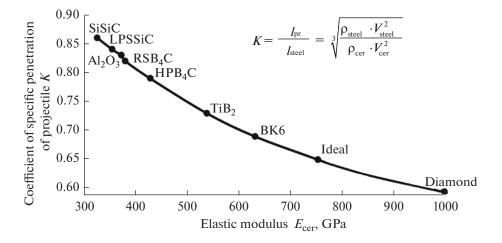


Fig. 3. Dependence of the coefficient of relative penetration of the steel striker into the ceramic.

$$W = \frac{1}{2\rho_c l S V_c^2} = D S l_n / V$$

where W is the mechanical energy of the rod, l_n is the depth of the cavity formed in the substance, V is the volume of one mole of the substance, M is the g/mol of the substance, and V_1 is the longitudinal speed of sound.

Taking into account that the relative deformation $\varepsilon_p = l_n/l$, we obtain the final formula of the equation

$$l_n = a l_c \sqrt[3]{\rho_c V_c^2 / \rho_n V_l^2}$$

where $a = (\ln 2)^{2/3}$, and ρ_c and ρ_n are the density of the rod and the ceramic, respectively.

An analysis of the obtained expression shows that under mechanical dynamic loading, the dissociation energy and the speed of sound are factors that determine the dissociation energy of loading during highspeed deformation. Moreover, using these fundamental constants, it is possible to construct a number of materials according to the degree of their resistance to dynamic loading. Figure 3 shows the curve of the dependence of the ratio of the relative penetration of steel and a number of known ceramic materials used in practice (shown in Table 2).

It is interesting that the review of works in the former Soviet Union on fracture mechanics, which appeared in 1992, gave this formula and discussed it. We have included two quotes below [19]: "Soviet studies of the mechanics of penetration in ceramics reflect more advanced thinking than Western studies due to the difference in their conceptual approaches. The

Material	Density ρ_{cer} , kg/m ³	Sound speed V_{cer} , m/s	Elastic modulus E_{cer} , GPa	$K = l_{\rm cer}/l_{\rm steel}$
Al ₂ O ₃	3750	9800	375	0.83
SiSiC	3100	10300	329	0.86
LPSSiC	3250	10500	358	0.84
RSB ₄ C	2550	13000	383	0.82
HPB ₄ C	2750	11800	431	0.79
BK6	15000	6500	633	0.69
TiB ₂	4500	11000	540	0.73
Ideal	3350	15000	754	0.65
Diamond	3510	17000	1000	0.59
Steel	7810	5173	209	1.00

 Table 2.
 Properties of ceramic materials

 Al_2O_3 , sintered corundum; SiSiC, reaction sintered silicon carbide; LPSSiC, liquid phase sintered silicon carbide; RSB₄C, reaction sintered boron carbide; HPB₄C, hot pressed boron carbide; BK6 alloy WC + 6% Co; TiB₂sintered titanium diboride; Ideal, material of diamond-silicon carbide; Diamond, single-crystal diamond.



Fig. 4. Destruction of "Ideal" ceramics.

development of the concept of characteristic waves of failure refers (probably) to tensile failure and precedes crater formation ... The Soviet experimental data confirm this hypothesis." We have also included another important quote [19]: "Soviet publications of analytical and experimental work were more advanced than those in the West by several years."

In conclusion, we present a photograph of the fracture's cavity of the "Ideal" ceramics (Fig. 4) under the action of an indenter 12.7 mm in diameter at a speed of 840 m/s. The circular and radial cracks are clearly visible. It is curious that the cavity's volume of the obstacle is about 20% of the total volume of the object, which is in good agreement with [2].

CONFLICT OF INTEREST

The authors declare that they have no conflict of interest.

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