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Structural evolution and phase transition mechanism of MoSe₂ under high pressure

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MoSe₂ is a layered transition-metal dichalcogenide (TMD) with outstanding electronic and optical properties, which is widely used in field-effect transistor (FET). Here the structural evolution and phase transition of MoSe₂ under high pressure are systematically studied by CALYPSO structural search method and first-principles calculations. The structural evolutions of MoSe₂ show that the ground state structure under ambient pressure is the experimentally observed *P6₃/mmc* phase, which transfers to *R3m* phase at 1.9 GPa. The trigonal *R3m* phase of MoSe₂ is stable up to 72.1 GPa, then, it transforms into a new *P6₃/mmc* phase with different atomic coordinates of Se atoms. This phase is extremely robust under ultrahigh pressure and finally changes to another trigonal *R-3m* phase under 491.1 GPa. The elastic constants and phonon dispersion curves indicate that the ambient pressure phase and three new high-pressure phases are all stable. The electronic band structure and projected density of states analyses reveal a pressure induced semiconducting to metallic transition under 72.1 GPa. These results offer a detailed structural evolution and phase diagram of MoSe₂ under high pressure, which may also provide insights for exploration other TMDs under ultrahigh pressure.

Most transition-metal dichalcogenides (TMDs) are layered compounds, which contain insulators, semiconductors and metals, in which, some of them are superconductors. The molecular formulas of TMDs are MX₂, where M is the transition metals, such as W, Mo, Nb, Ta, Ti and others, X is the chalcogen, such as S, Se, Te and so on^{1–6}. Up to now, the ground state structures of TMDs under ambient conditions are extensively studied. According to the number of stacked layers, the possible structures of TMDs can be classified into 1T phase with trigonal antiprismatic, 2H phase with trigonal prismatic, 3R phase with trigonal prismatic, etc, which have many stacking patterns in common. Generally, the weak van der Waals force connect layers of TMDs and allow the atom/molecules to enter the interlayers and change their electronic properties^{7,8}. On the other hand, pressure can also cause the change of interlayer spacing and the interlayer slip, and lead to the varied structure and electronic properties of different TMDs^{9,10}.

MoSe₂ is a typical TMD with hexagonal phase stable structure at ambient conditions^{1,5}. It is an indirect bandgap semiconductor, with bandgap of about 1 eV. However, there is a very few structural evolutions of MoSe₂ under high pressure. In contrast, the structural phase transitions of MoS₂ under high pressure are extensively studied. Saha¹¹ et al. has carried out the first-principles calculations of MoS₂ under high pressure and confirmed the stable high-pressure phases in the pressure range of 100 GPa to 200 GPa, which are *P4/mmm* and *I4/mmm* structures. Kohulák et al.¹² has reported that MoS₂ transformed from semiconducting to metallic at 40 GPa. However, the interesting subject needs further attentions is that in the similar compound, whether MoSe₂ exists the similar pressure induced semiconductor to metal transition.

In the present paper, we focus on the structural transition and electronic properties of MoSe₂ under high pressure by using the structure search method and first-principles calculations. Our results show that MoSe₂ transfers from *P6₃/mmc* structure to *R3m* phase at 1.9 GPa, which is stable up to 72.1 GPa. Interestingly, as the pressure increase, MoSe₂ again transfers from *R3m* phase to *P6₃/mmc*, however, it is metallic, which is different from the semiconducting *P6₃/mmc* phase under ambient pressure. These results are different from the previous experiments showed that MoSe₂ is mostly stable as 2Hc phase below 100 GPa^{11,12}. This contradiction leads us

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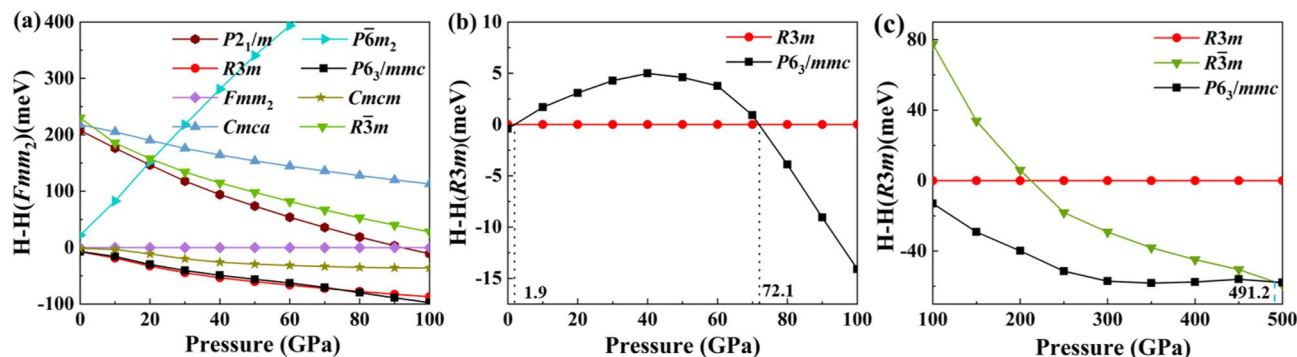


Figure 1. The enthalpy curves of MoSe₂ under high pressure. (a,b) MoSe₂ under high pressure with pressure in range of 0 GPa to 100 GPa. (c) MoSe₂ under ultrahigh pressure with pressure in range of 100 GPa to 500 GPa.

to further explore the new phases and structural transition sequence of MoSe₂ under high pressure, especially at ultrahigh pressure.

Theoretical methods

We have conducted a systematical structure search for MoSe₂ under high pressure based on Crystal structure ANALYSIS by Particle Swarm Optimization (CALYPSO) approach and first-principles calculations^{13–20}. The advantages of these techniques are to predict the stable and metastable structures at the given chemical compositions within certain condition^{21,22}. The total energies and electronic properties are calculated within the density functional theory (DFT) framework, as it has implemented by Vienna ab initio simulation package (VASP) code²³. The projector augmented wave (PAW) method has employed in the DFT calculations to describe electron–ion interactions in MoSe₂. The 4d⁵, 5s¹ and 4s², 4p⁴ are treated as the valence electrons for Mo and Se atoms, respectively²⁴. We set the cutoff energy of 600 eV for the wave-function to expand plane waves and select dense Monkhorst–Pack *k*²⁵ meshes to ensure all enthalpy calculations are converged in 1 meV/atom. The phonopy code has used to calculate the phonon dispersion curves using 2 × 2 × 1 supercells for *P6₃/mmc*, *R3m*, and *R-3m* phases of MoSe₂²⁶. Based on the ground state structures of MoSe₂ under different pressure, the energy band structure, density of states, and elastic properties are also calculated²⁷ and discussed in detail.

Results and discussion

We have predicated about 1000 potential structures for MoSe₂ at each selected pressure. The top 100 candidate structures of MoSe₂ under 0 GPa, 50 GPa, 100 GPa, 200 GPa, and 500 GPa are reoptimized by high accuracy calculations. We have successfully identified the experiment observed *P6₃/mmc* (2H) phase under ambient pressure, which verifies that the CALYPSO method is perfectly suitable for MoSe₂ and the searched results are reliable. It can be seen from Fig. 1a that the enthalpies of *R3m* and *P6₃/mmc* phases are almost the same when the pressure increase from 0 to 100 GPa. Interestingly, some potential low energy phases at low-pressure range are all layered structures. Thus, we have considered the van der Waals (VDW) interactions in the DFT calculations under low-pressure between 0 to 10 GPa. From Fig. 1b, we can clearly find that the energy of *P6₃/mmc* phase is lower than that of *R3m* phase at 0 GPa to 1.9 GPa²⁸, and the energy of *R3m* phase is lower than that of *P6₃/mmc* phase with pressure ranged of 1.9 GPa to 72.1 GPa. In fact, the transform pressure of MoSe₂ from *R3m* phase to *P6₃/mmc* phase is almost unchanged with/without considering the VDW effects. The transform pressure of MoSe₂ from *R3m* phase to *P6₃/mmc* phase is about 2.5 GPa by without considering the VDW interactions, which maybe due to that the Mo and Se atoms are relatively heavy and the influences of VDW interactions on the energy calculations of MoSe₂ are negligible. When the pressure is higher than 72.1 GPa, a new *P6₃/mmc* phase is uncovered, which is different from the initial *P6₃/mmc* phase. The main differences are the crystal lattice parameters and atomic coordinates of Se atoms. It is extremely robust under ultrahigh pressure and final changes to the trigonal *R-3m* phase under 491.1 GPa. The structural phase transition of MoSe₂ under ultrahigh pressure is shown in Fig. 1c. The corresponding crystal structures of MoSe₂ under high pressure up to 500 GPa are shown in Fig. 2. To further prove the structural stability of MoSe₂, we have calculated the formation energies of possible phases and considered the potential energy decomposition to bulk Se and Mo crystals and relevant Mo–Se compounds. The calculations once again indicate that MoSe₂ is stable. The detailed results are shown in Fig. S1 in the Supplementary Information.

From Fig. 2, we can find that the unit cell of *P6₃/mmc* is stacked repeatedly with a period of two MoSe₆ layers, while cells of *R3m* and *R-3m* are stacked repeatedly with a period of three MoSe₆ layers. The optimized lattice parameters and atomic coordinates of the four phases are listed in Table 1.

We now test the chemical, dynamical, and mechanical stabilities of MoSe₂. The cohesive energy of MoSe₂ can be calculated by the formula as following^{29–33},

$$E_{coh} = \frac{x E_{Mo} + y E_{Se} - E_{Mo_x Se_y}}{x + y}, \quad (1)$$

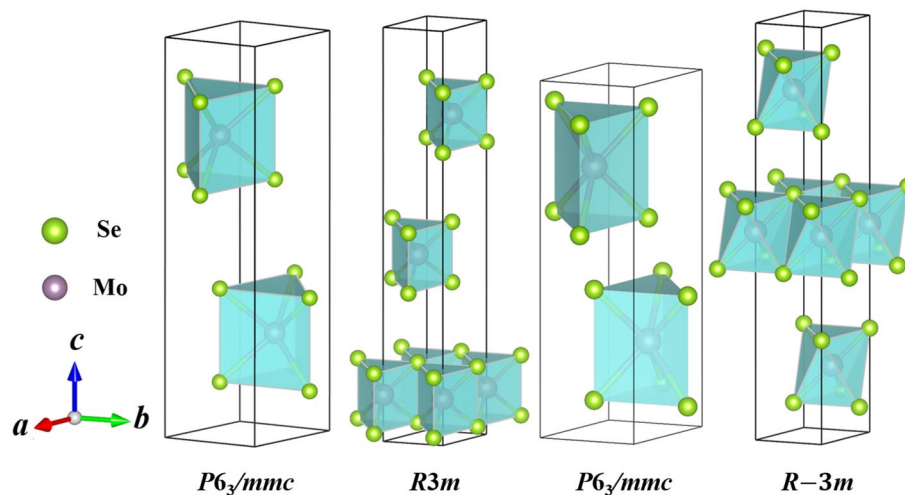


Figure 2. The crystal structures of MoSe₂ under high pressure up to 500 GPa. (a) *P6₃/mmc*, (b) *R3m*, (c) *P6₃/mmc*, and (d) *R-3m* phases.

Pressure (GPa)	Structure	Parameter (Å, °)	Atom	<i>x</i>	<i>y</i>	<i>z</i>
0	<i>P6₃/mmc</i>	$a = b = 3.3226, c = 14.3363$	Mo1	0.3333	0.6667	0.2500
		$\alpha = \beta = 90^\circ, \gamma = 120^\circ$	Se1	0.6667	0.3333	0.6338
20	<i>R3m</i>	$a = b = 3.1676, c = 17.4749$	Mo1	-0.0000	-0.0000	0.1128
		$\alpha = \beta = 90^\circ, \gamma = 120^\circ$	Se1	0.6667	0.3333	0.0166
			Se2	0.6667	0.3333	0.2085
80	<i>P6₃/mmc</i>	$a = b = 2.8898, c = 11.0080$	Mo1	0.3333	0.6667	0.2500
		$\alpha = \beta = 90^\circ, \gamma = 120^\circ$	Se1	0.3333	0.6667	0.5949
500	<i>R-3m</i>	$a = b = 2.3687, c = 15.3738$	Mo1	0.3333	0.6667	0.1667
		$\alpha = \beta = 90^\circ, \gamma = 120^\circ$	Se1	-0.0000	0.0000	0.2770

Table 1. Calculated lattice constants and atomic coordinates of MoSe₂ under selected pressures.

where E_{Mo} , E_{Se} , and $E_{Mo_xSe_y}$ are the energies of Mo atom, Se atom, and a unit cell of MoSe₂, respectively^{27,34}. The cohesive energies of the four candidate of MoSe₂ (0 GPa *P6₃/mmc*, 20 GPa *R3m*, 80 GPa *P6₃/mmc* and 500 GPa *R-3m*) are -13.49, -13.29, -1.83 and -5.29 eV per atom, respectively. These results indicate that the bulk MoSe₂ is strongly bonded with good chemical stability. Subsequently, we have calculated the phonon dispersion curves of four structures of MoSe₂ within different pressures. The results are displayed in Fig. 3. There is no presence of imaginary frequency in the Brillouin zone, which indicates that these four phases of MoSe₂ are dynamically stable.

Meanwhile, we have calculated the elastic constants of the four phases of MoSe₂ under different pressures, which are *P6₃/mmc* phase at 0 GPa, *R3m* phase at 20 GPa, *P6₃/mmc* phase at 80 GPa, and *R-3m* phase at 500 GPa. The elastic constants are listed in Table 2. The stability criteria of hexagonal and trigonal crystal structure are $C_{11} > |C_{12}|$, $(C_{11} + C_{12}) > 2C_{13}^2$, $(C_{11} - C_{12})C_{44} > 2C_{14}^2$ for trigonal crystal and $C_{11} > 0$, $C_{44} > 0$, $C_{11} > |C_{12}|$, $(C_{11} + C_{12}) > 2C_{13}^2$ for hexagonal crystal³⁵. According to the above criteria, we note that the calculated elastic constants match well with the stability criteria in corresponding space group symmetries^{36–39}. Thus, we can conclude that these four phases of MoSe₂ are mechanical stability.

To deeply understand of the effect of pressure on the electronic properties, the evolution of electronic band structure and density of states of the four phases of MoSe₂ are shown in Fig. 4. At 0 GPa, the ground state structure is *P6₃/mmc* phase. It can be seen from Fig. 4a, the *P6₃/mmc* phase is a direct bandgap semiconductor with bandgap of 1.22 eV. With pressure increasing, the bandgap is slowly decreasing. At 1.9 GPa, the structure *P6₃/mmc* transforms to *R3m* phase²⁸, which is an indirect bandgap semiconductor. The bandgap is 0.154 eV under 20 GPa (see Fig. 4b). From 20 to 500 GPa, MoSe₂ becomes to a metal as shown in Fig. 4c,d.

The detailed total and partial density of states are calculated (see Supplementary Information, Fig. S3). The states above -5.5 eV in *P6₃/mmc* phase at 0 GPa, -7.5 eV in *R3m* phase at 20 GPa, and -10 eV in *P6₃/mmc* at 80 GPa are mostly originated from Mo-*d* and Se-*p* orbitals. The Mo-*d* and Se-*p* orbitals show strong *p-d* hybridization and indicate obviously covalent bonding characteristics of Mo-Se chemical bond. In *P6₃/mmc* phase, the orbitals have more overlapping at 80 GPa than 20 GPa, which proves that covalent properties of Mo-Se bond is strengthened by increasing the pressure. In Fig. S3d, we can see a noticeable peak at -12 eV in the density of states of *R-3m* phase at 500 GPa, which are mainly contributed by the *p* orbitals of Mo atoms. Furthermore,

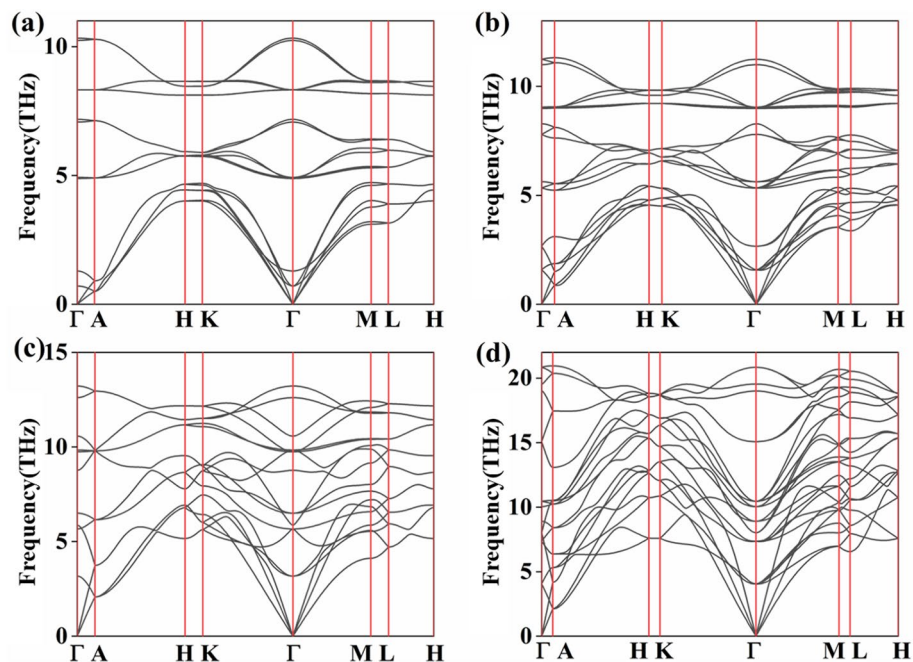


Figure 3. The phonon dispersion curves of MoSe₂. (a) *P6₃/mmc* under 0 GPa, (b) *R3m* under 20 GPa, (c) *P6₃/mmc* under 80 GPa, and (d) *R-3m* under 500 GPa, respectively.

Pressure (GPa)	Structure	C ₁₁ (GPa)	C ₁₂ (GPa)	C ₁₃ (GPa)	C ₁₄ (GPa)
0	<i>P6₃/mmc</i>	173	57	118	58
20	<i>R3m</i>	267	70	194	100
80	<i>P6₃/mmc</i>	501	145	678	180
500	<i>R-3m</i>	1659	826	2171	417

Table 2. The calculated the elastic constants of MoSe₂.

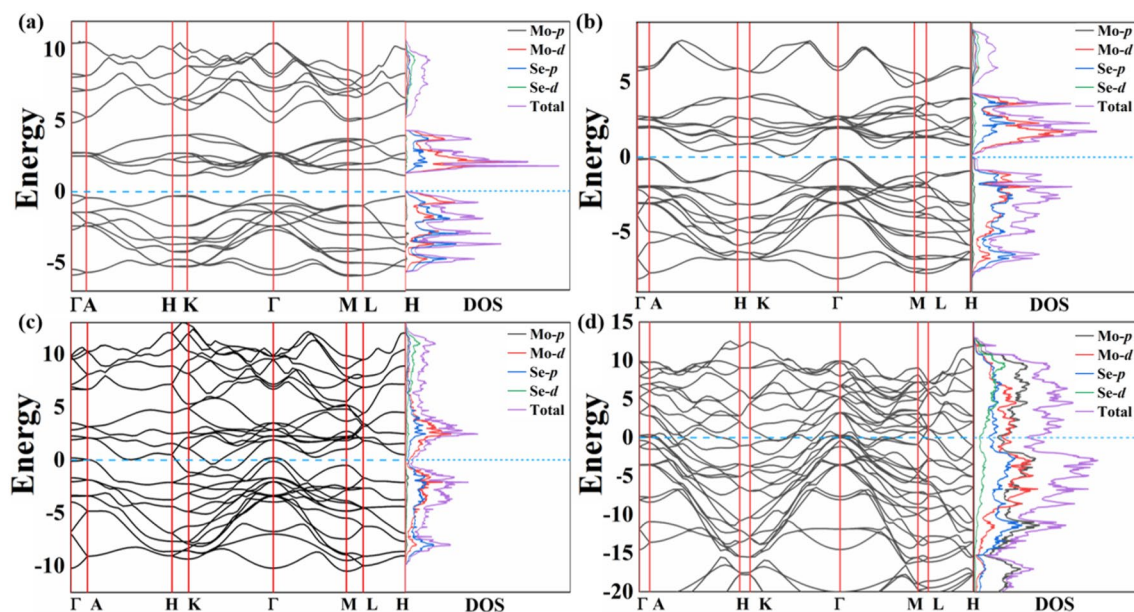


Figure 4. Band structure and projected density of states of MoSe₂. (a) *P6₃/mmc* phase at 0 GPa, (b) *R3m* phase at 20 GPa, (c) *P6₃/mmc* phase at 80 GPa, and (d) *R-3m* phase at 500 GPa, respectively.

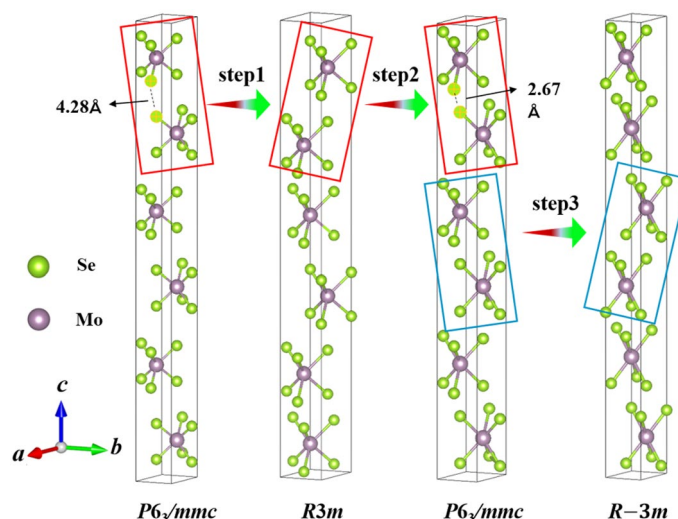


Figure 5. The schematic diagram of four phases of MoSe₂ under different pressures in the pressure range of 0 GPa to 500 GPa. **(a)** $1 \times 1 \times 3$ supercell for $P6_3/mmc$ phase at 0 GPa, **(b)** $1 \times 1 \times 2$ supercell for $R3m$ phase at 20 GPa, **(c)** $1 \times 1 \times 3$ supercell for $P6_3/mmc$ at 80 GPa, and **(d)** $1 \times 1 \times 2$ supercell for $R-3m$ phase at 500 GPa, respectively.

except for Mo-*d* and Se-*p* orbitals, the contributions from Mo-*p* orbitals are visibly increased compared with low pressure conditions. This may due to the firmer MoSe₆ octahedra in $R3m$ phase of MoSe₂.

We return again to search the potential structural phase transition mechanisms of MoSe₂ under high pressure. To clearly compare the four phases of MoSe₂ under different pressure, we have displayed the crystal structure with the same atomic number of Mo and Se atoms by using the supercell of $1 \times 1 \times 3$ for $P6_3/mmc$ phase at 0 GPa, $1 \times 1 \times 2$ for $R3m$ phase at 20 GPa, $1 \times 1 \times 3$ for $P6_3/mmc$ phase at 80 GPa, and $1 \times 1 \times 2$ for $R-3m$ phase at 500 GPa, respectively. The schematic diagrams are shown in Fig. 5.

From Fig. 5, we find that the structural phase transitions of MoSe₂ under high pressure are attributed to the chiral structure transitions of the top two MoSe₆ layers marked in red rectangles and the middle two MoSe₆ layers displayed in blue rectangles. The evolution of phase transitions is constituted by three steps. In the first step, three-unit cells of $P6_3/mmc$ phase translate into two $R3m$ unit cell at 1.9 GPa. The main changes occur at the top two MoSe₆ layers in $P6_3/mmc$ and $R3m$ phases, which is a chiral transform of the two MoSe₆ layers with mirror symmetry. In the second step, the two-unit cells of $R3m$ phase return to three $P6_3/mmc$ unit cells, and the central symmetric transformation occurs again on the top two MoSe₆ layers. However, the interlayer spacing of the top two MoSe₆ layers decreases from 4.28 to 2.67 Å as pressure increasing from 0 to 80 GPa, as shown in the red square of Fig. 5. In the third step, the structure evolution of MoSe₂ under ultrahigh pressure is different from the previous two steps. The structural transformation happens at the middle layers of the MoSe₆, as shown in the blue rectangles of Fig. 5. The three-unit cells of $P6_3/mmc$ phase return to two $R-3m$ unit cells, with a chiral structure transition of the middle two MoSe₆ layers. Furthermore, it is easy to find that the pressure induced semiconducting to metallic transition of MoSe₂ under high pressure, which is mainly attributed to the different stacking modes of the MoSe₆ layers in different phases of MoSe₂. These results offer important insights for exploration the evolutions of structures and electronic properties of other TMDs at extreme conditions.

Conclusion

In summary, we have performed comprehensively structure predictions of MoSe₂ under high pressure up to 500 GPa by CALYPSO method and first-principles calculations. Three new high pressure phases of MoSe₂ are uncovered, and the phase transition sequence follows the order of $P6_3/mmc \rightarrow R3m \rightarrow P6_3/mmc \rightarrow R-3m$. The energy band structure calculations indicate MoSe₂ are evolution from direct bandgap semiconductor to indirect bandgap semiconductor, eventually, to a metal with pressure increase. These attractively electronic properties are due to the chiral structure changes of the top two MoSe₆ layers in MoSe₂. The present findings establish the structural phase diagram of MoSe₂ under high pressure and describe the evolutions of structures and electronic properties of MoSe₂, which offer important insights for exploration other TMDs at extreme conditions.

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Author contributions

Y.X.: wrote and edited the manuscript, made the figures. Y.X. and S.H.: carried the main responsibility for the data analysis. M.L., W.S., Z.W. W.D and C.L.: carried out to review and supervision of the manuscript.

Competing interests

The authors declare no competing interests.

Additional information

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