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Road marking retroreflectivity study via a visual algorithm

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Abstract

The retroreflectivity (R_L) of road markings is important and should be inspected and maintained throughout their service life. The specifications are provided by European nations, the United States, and many other countries. Although acceptance tests ensure the good R_L quality of newly placed road markings, the R_L values of all in-service road markings are rather difficult to inspect by using currently available devices. This study, therefore, aims to determine the relationship between R_L and corresponding image brightness of yellow road markings to evaluate their visibility by analyzing recorded images captured at night. An integrated algorithm was developed to analyze recorded images continuously for identifying road marking brightness 30 m away from a vehicle. Field experiments on three types of road marking materials were performed and repeated at four separate locations. The findings provide a promising direction for using the image brightness of road markings to predict their field R_L . However, limitations of this study are discussed and suggestions for future direction are presented.

Keywords: Road marking; Retroreflectivity; Mask R-CNN; Image brightness

1. Introduction

Road markings play an important role in ensuring road safety. Therefore, the retroreflectivity (R_L) and completeness of road markings should be maintained to an acceptable level throughout their entire service life to fulfill their functions. Related specifications are provided for newly painted or in-service road markings in most countries or regions. Although several materials, such as thermoplastic, paint, and preformed materials, are commonly used for road markings, they generally do not differ in R_L quality requirements.

 $R_{\rm L}$ indicates the coefficient of retroreflected luminance, which is measured in compliance with an international standard. The minimum accepted road marking reflectivity index increases with roadway speed limit to provide drivers with sufficient safety. The United States Manual on Uniform Traffic Control Devices (MUTCD) specifies the lowest maintained levels of dry nighttime visibility $R_{\rm L}$ of 50 and 100 mcd/m²/lx for yellow road markings in roadways with speed limits of 35 to 50 and above 50 mph, respectively [1].

Other specifications or standards, such as the American Society of Testing Materials (ASTM) D7942, specifies that the RL requirement at 180 days after placement should be above 200 mcd/m²/lx, and the maintenance minimum R_L should be no less than 125 mcd/m²/lx [2]. The Central, East and West Nippon Expressway Company Limited and the Hong Kong Highways Department set the minimum R_L values of yellow road markings to be 80 mcd/m²/lx [3,4]. European nations also laid down specifications CEN 1436 for yellow road marking R_L, with the minimum levels of R1 (the lowest requirement) and R4 (the highest standard) set at 80 and 200 mcd/m²/lx, respectively [5]. Taiwan's specification, CNS 15834, of road marking follows the EN1436; thus, the specified R_L numbers of yellow marking R1 to R4 of both standards are exactly the same [6]. Although these mentioned specifications also indicate the required R_L for white road markings, only yellow road markings are considered in the current study due to research constraints.

Devices have been developed to measure road marking R_L , and the commonly used measuring devices include two general types: handheld and mobile retroreflectometers. The former is usually handled manually to measure road marking R_L from one location to another or mounted with moving wheels and pushed manually at a walking speed. The latter is mounted at one side of a vehicle, and the measurement is conducted while the vehicle runs up to 120 km/h. Fig. 1 illustrates the various types of road marking retroreflectometers. Although the efficiency of the mobile type is much higher than that of the handheld type in terms of measuring speed, the high cost of the mobile type limits its wide adoption.

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Fig. 1. Various types of retroreflectometers (a) handheld, (b) push type, and (c) vehicle mounted.

Beside the instrumental measurements, the MUTCD suggests that the trained inspectors can provide stable evaluation through visual inspection; however, the training procedures and inspection vehicles should be standardized [1]. Benz et al. also stated that manual visual inspection of road marking retroreflectivity is a highly efficient, low cost, no device needed, and low traffic impact method [7]. However, the variation among subjective judgements may induce the inaccurate results.

In 2006, Horberry et al. applied driving simulation analysis to study the possible safety benefits by enhancing road markings with large glass beads. It was found that the enhanced roadway markings tend to help drivers receive better marking's visibility and keep the vehicle within the traffic lane [8]. Autonomous vehicle technology has rapidly developed in recent years with corresponding progress in image processing and machine learning algorithms, which apply to automatic road marking recognition. Therefore, the visibility of road marking has become more and more important for the autonomous vehicle industry [9]. Considering the possible positive correlation between the concepts of road marking R_L and image characteristics, this study aims to study the feasibility of using road marking image brightness captured from video recording devices to analyze R_L and increase the efficiency of the R_L evaluating of in-service road markings.

2. Data acquisition systems

In this study, two types of data were collected for algorithm development. The following sections describe the data features and corresponding devices adopted for data acquisition.

2.1. Road marking retroreflectivity, R_L

The first type of data included R_L , which were collected by devices manufactured in compliance with international specifications/standards, such as CEN 1436 (R_L) [5], ASTM E1710 (R_L) [10], and ASTM E2177 (R_L wet) [11]. Fig. 2 illustrates the standard geometry of R_L measurement. The simulation assumes that a driver's eye height and vehicle headlight height are 1.2 m and 0.65 m above the ground, respectively. The regulated

visibility of surface road marking at 30 m in front of a vehicle should be considered. Therefore, the geometric locations among the driver, headlights, and road marking create a driver's observation angle of 2.29° and an illumination angle of 1.24°. The coefficient of retroreflected luminance is calculated on the basis of the given circumstances with vehicle headlight only. Various brands of R_L -measuring devices have been designed, manufactured, and sold commercially. In the current study, a portable handheld device that meets the specifications of CEN 1436 (R_L) [5], ASTM E1710 (R_L) [10], and ASTM E2177 (R_L wet) [11] was adopted for R_L data collection. Table 1 provides the general technical specifications of the device.

2.2. Road marking images

The second type of data included road marking images, which were collected using video cameras. Imaging techniques were applied for road marking recognition, brightness detection, and distance measurement.

2.2.1. Image processing algorithm

Methodologies for image recognition and identification have been developed for more than three decades, and the algorithms are continuously improved over the years. In general, two major types of image processing algorithms are used, namely, traditional and machine learning methods. The three typical traditional image processing algorithms are threshold segmentation, edge detection, and regional growth method. Studies in various fields have applied one or more of these algorithms to solve research problems successfully. The traditional methods are typically used to identify and recognize a single object in a given region. Targeting objects under certain circumstances, such as those with sizes and/or angles that vary significantly, and the simultaneous targeting of multiple types of objects are both considered relatively difficult. However, these problems have been overcome in recent years, given the rapid improvements in machine learning techniques.

Convolutional neural networks (CNNs) have become the standard for image classification. Several CNNs, such as regional CNN (R-CNN) [12], fast R-CNN [13], faster R-CNN [14], and



Fig. 2. Standard 30-Meter Geometry of R_L.

Table 1	
General specifications of	portable handheld retroreflectometers.

Standards	EN 1436 (RL), ASTM E1710(RL),
	ASTM E2177 (R _L wet)
Observation angle	2.29°
Illumination angle R _L	1.24°
Equivalent observation	30 m
distance	
Measuring area ($W \times L$)	52 mm × 218 mm (2.05" × 8.58")
Measuring range (R _L)	$0 - 4,000 \text{ mcd/m}^2/\text{lx}$
Measuring time (R _L)	$\approx 2 \text{ s}$
Operating temperature	$-10 ^{\circ}\text{C} \pm 50 ^{\circ}\text{C} (14 ^{\circ}\text{F} - 122 ^{\circ}\text{F})$

mask R-CNN [15], have been developed. Mask R-CNN, an updated CNN developed by He et al. in 2017, has an algorithm that is based on faster R-CNN, but it creates an additional CNN to form a mask for identifying individual targeted objects. During the training process, the mask of the least systemic losses is selected to obtain the best results [15]. In this study, mask R-CNN was adopted for processing road marking images.

2.2.2. Distance measurement algorithm

Video images have been used for decades for distance detection. In a past study, the images from a single camera were used to analyze 3-dimensional information; however, the data obtained did not satisfy the accuracy of computing distance [16]. Pollefeys et al. highlighted that a single camera image yields a relative scale factor of distance rather than the actual distance [17]. Olaverri-Monreal et al. used two nearby cameras to capture an image of the same object and compute the distance through triangulation [18].

With a stereo camera, two two-dimensional (2D) photos can be reconstructed into a three-dimensional (3D) photo. The distance calculated between two cameras and an object is much more accurate than that obtained from a single camera. In this study, a dual-camera Raspberry Pi module was adopted and installed on a vehicle's rearview mirror to capture road marking images. The distance measurement theory by dual-camera images proposed by Olaverri-Monreal [18] is applied to calculate the distance between the cameras and the target road marking. Only the area where the images of both cameras overlap can be calculated. The distance between a vehicle and any specific road marking point within an overlapping area was computed by triangulation analysis using Eq. (1) [18]. Fig. 3 displays a close-up picture of the dual-camera Raspberry Pi module, and Table 2 provides basic information on this module.

$$D_{object} = \frac{D_{cameras} \times Px_h}{2 \tan(\frac{\Phi_0}{2}) \times (Px_L - Px_R)}$$
(1)

where, D_{object} : distance between the cameras and the object; $D_{cameras}$: distance between dual cameras; Px_h : horizontal pixel resolution (pixel number); Px_L : pixel number at the left picture; Px_R : pixel number at the right picture; ϕ_0 : horizontal field of view angle.

In our system, the distance between cameras ($D_{cameras}$) is 6 cm, the horizontal field of view (ϕ_0) is 60°, the horizontal pixel resolution (Px_h) is 1280, and the horizontal pixel difference to the same object in both pictures in pixels is Px_L-Px_R .

2.3. Integrated algorithm for the road marking image analysis

Fig. 4 displays a flowchart of an integrated algorithm for road marking image processing. A preprocessing step was conducted prior to the mark R-CNN analysis. The pixel intensity of raw images was preprocessed via gamma correction, as shown in Eq. (2). This step aimed to compensate for human sensitivity to visual



Fig. 3. Actual photo of the dual-lens module.

l able 2				
Detailed	parameters	of the	dual-lens	module

Model no.	HBV-1780-2 S2.0	
Model size	80 mm×22 mm×25 m	ım
	(distance between car	neras is 6 cm)
Sensor	OV9732	
Interface	MINI USB 2.0	
Display field of	60°	
view (DFOV)		
Video format	MJPG	
Output format	2560×720 (default)	1280×720
-	30 fps	30 fps
	1280×480 30 fps	640×480 30 fps
	640×240 30 fps	320×240 30 fps
Focus	Fixed focus	-



Fig. 4. Flowchart of the integrated algorithm.

brightness and grey level, which is typically nonlinear and close to gamma distribution.

$$V_{out} = A V_{in}^{\gamma} \tag{2}$$

where, V_{out} : output image pixel intensity after gamma correction; V_{in} : input image pixel intensity before gamma correction; A: constant coefficient; γ selected value.

In this study, thousands of road marking images were captured in a totally dark environment with only vehicle headlights. This experiment was conducted at the National Taiwan University Palm Boulevard, a four-lane undivided straight road of approximately 450 m. The center yellow road markings were reconstructed with three types of materials. Data collection was executed after midnight, and all streetlights were turned off.

Fig. 5(a) and 5(c) show the typical raw image collected in this study and its corresponding pixel intensity histogram distributions and cumulative frequencies. As can be seen, the pixel intensity histogram concentrates on a bandwidth between 0.0 and 0.2. This result commonly occurs in all of the raw images acquired in this study. This bandwidth is too narrow to sufficiently identify road marking images from the dark background. Therefore, Eq. (2) was applied to the raw images, and the γ value was tested from 0.1 to 1.0 at an increment interval of 0.1 to investigate the optimum pixel intensity distribution for further study.



Fig. 5. Pixel intensity histogram distributions and cumulative frequencies (a) original camera image, (b) gamma-corrected camera image, (c) original image intensity histogram, and (d) gamma-corrected image intensity histogram.

The results indicate that $\gamma = 0.5$ provides the best enhancement of pixel intensity. As shown in Fig. 5(b) and 5(d), the distinguishable pixel intensity distribution increases the efficiency of the following analysis steps.

2.3.1. Mask R-CNN.

After gamma correction was applied on each raw image, mask R-CNN was performed for image processing. Mask R-CNN is the latest development of CNN. It uses R-CNN as the base and adds object masks to image processing to increase the efficiency and accuracy of target image recognition and identification. Images with or without road markings are processed and classified into two groups. In this study, a total of 6415 images captured during the experiment, and Table 3 shows the numbers of images used in the training and testing. A confusion matrix [19,20] was adopted to evaluate the precision of analyzed results. Precision is defined in Eq. (3), and the terms of TP and FP are defined below. As indicated by the results, the images with and without road markings are successfully identified with precision rates of 83% and 92%, respectively. The overall precision rate is 87%. In general, the mask R-CNN method provides good results for identifying road marking images, which are retained for further analysis.

$$precision = \frac{TP}{TP + FP}$$
(3)

In the equation above, TP is true positive, and FP is false positive.

2.3.2. Brightness and distance detection

For the image identification, the brightness levels of the suspected road marking pixels were investigated. Fig. 6 displays the brightness histogram of a typical road marking image. Only the pixels of road marking area are retained after applying the mask R-CNN on the raw image; thus, more than 70% of the pixel brightness intensity is concentrated between 200 and 225. The

average brightness of the retained pixels was computed to represent the specific road marking brightness. The distance between the vehicle and the farthest point within the mask was then calculated using the distance measurement algorithm and Eq. (1). Therefore, the distance and brightness of each road marking image were paired for further analysis. It should be mentioned that the calculated brightness is based on the experimental device used in this study. A variety of factors, such as brand and model of the dual-lens module or exposure time setting, may affect the capture image brightness. Further study should focus on how these factors will affect the results. However, all parameters are fixed in the following analyses.



Train and test dataset used in mask R-CNN.

Туре	With markings (frames)	No markings (frames)	Total
train	4907	1271	6178
test	206	31	237



Fig. 6. Brightness histogram intensity of a typical road marking image.

3. Field experiments and data analysis

The field experiments were conducted along the 450 m-long National Taiwan University Palm Boulevard. All the experiments were executed after midnight with the streetlights off and a specific traffic control condition to study the relationship between the road markings' R_L and their corresponding image brightness levels. Thus, test vehicle headlights were the only light source for illuminating road markings as the video images were captured.

Three types of road marking materials were selected and placed for the field experiments. Two of which, A and B, were thermoplastic materials with different types of beads and anti-skid additives, and C was a preformed pavement marking tape. The major difference between the beads used in types A and B was the reflective index (RI). Type A includes mixed conventional beads (RI = 1.5) and high-RI beads (RI = 1.64) internally and high-RI external drop-off beads. Type B is a widely used commercial product that uses conventional beads internally and externally. Fig. 7 shows the construction of thermoplastic type and preformed tape. Table 4 provides the specifications of the three materials. Every type of road marking was placed at four separate locations along the test road, and the R_L tests were conducted using the handheld retroreflectometer for 46 test points.

During the field experiment, videos were recorded by a dual-lens camera in totally dark environments with only vehicle headlights. The researchers videotaped the setup while a vehicle was moving from 150 m away toward each type of road marking at an average running speed of 40 km/h (25 mi/h, 11.1 m/s). The camera taping frequency was 30 fps. Thus, each frame covering range had approximately 37 cm variation. For every test run, all placed road markings were covered with black tapes, except for the targeted one.

Given that the testing runs always started far away from the target, the first few hundreds of picture frames did not include any road marking image. When the vehicle gradually approached the target, the frames then started to include the road marking images



Fig. 7. Field construction of (a) thermoplastic road markings and (b) preformed pavement marking tapes.

from far to near. Fig. 8 shows the typical analyzed results of the relationship between paired distance and brightness of one driving test. As indicated by the results, the average brightness of the road marking pixels tends to increase as the vehicle gets closer to the analyzed target.

Three types of road markings were tested separately, and each type was tested in four placed locations, resulting in 12 test runs. Similar to the data in Fig. 8, the relationship between paired distance and brightness resulting from the 12 test runs clearly show that the brightness of the road markings increases as the vehicle gets closer to the analyzed target. This finding is consistent regardless of the road marking type.

Meanwhile, Type C has the highest brightness at any giving distance, indicating that it can be seen more easily at night than the two other types. The sequence of brightness of the three road marking types is C > A > B. Type B which uses conventional beads internally and externally has the lowest performance, in terms of image brightness and measured R_L , given that the conventional beads have low RI. It should be mentioned that the R_L requirement is not yet regulated in existing road marking acceptance specifications in Taiwan, so type B occupies the most market share for its low cost. In order to analyze the correlation between image brightness and road marking R_L , the brightness values at a distance of 30 m of each test, the same distance applied to determine the R_L simulated by the retroreflectometer, are marked for further analysis.

The R_L measurements were conducted simultaneously with image tests. Table 5 provides the paired measured R_L and image brightness values of the three types of test road markings placed at four locations. The values of brightness represent the images collected by the dual-lens camera and analyzed by the developed algorithm 30 m ahead of the test vehicle. Once again, Type C provides the highest R_L and image brightness.

From the 12 sets of R_L measurements and image brightness values, data can be easily clustered into three road marking groups,



Fig. 8. Relationship between paired distance and brightness of one typical example.

Table 4					
Three types	of road marki	ng materials	used in	the field	study.

Туре	Internal additives		External drop-off		
	Conventional beads*	High reflective index beads**	High reflective index beads**	Quartz sand	Conventional beads*
А	30%	10%	160 g/m^2	160g/m^2	N/A
В	30%	N/A	N/A	N/A	160 g/m^2
С	Preformed pavement r	narking tape			

* Regular beads: AASHTO M247-13 type 1, reflective index: RI=1.5 [21].

** High reflective index beads: AASHTI M247-13 type, reflective index: RI=1.64 [21].

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Paired R _L and image brightness of types A, B, and C road markings.				
		Road mar	king type	
А		В		С
$R_L (mcd/m^2/lx)$	Brightness	$R_L (mcd/m^2/lx)$	Brightness	$R_L (mcd/m^2/lx)$
141	126	50	67	310
118	129	38	69	321
139	121	50	72	318

63

Table 5 Pa

A, B, and C, as shown in Fig. 9. This result also indicates that the performance of each road marking in terms of R_L is very consistent at four locations. An exponential regression equation is shown in Eq. (4). The correlation coefficient of this non-linear equation is 0.93, which provides a relatively good explanation between these two variables. The corresponding brightness values that match the five classes of R_L, which we determined using Eq. (4), are presented in Table 6. For example, a yellow road marking image with a brightness of ≥ 95 indicates a corresponding R_L of ≥ 80 $mcd/m^2/lx$.

130

$$Y = 12.9315e^{0.0192X} \tag{4}$$

In the equation above, Y: predicted road marking R_L , mcd/m²/lx; X: computed road marking brightness.

4. Discussions and conclusions

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The R_L of road markings is a key parameter that indicates their visibility at dry nighttime, particularly when no other light except vehicle headlights resource are available. The construction



Fig. 9. Relationship between yellow road marking brightness and RL.

Table 6

Corresponding retroreflectivity classes of EN 1436/CNS15834 and yellow marking image brightness.

EN 1436/ CNS 15834		Marking image
Class	Yellow marking $R_L (mcd/m^2/lx)$	brightness
R0	No performance determined	< 95
R1	≥ 80	≥ 95
R2	-	-
R3	≥ 150	\geq 130
R4	≥ 200	≥ 145

acceptance specifications of required R_L ensure the good quality of newly placed road markings. However, the entire population of inservice road markings is rather difficult to inspect by using currently available devices.

309

Brightness 166

154 150

171

This study aims to establish a reliable relationship between R_L and the image brightness of a road marking so that the latter can be used as an efficient indicator to screen the R_L of in-service road network markings. The field experiments were conducted to collect road marking images at night using the dual-lens camera. The integrated algorithm was developed for analyzing the image brightness of the road markings at a distance 30 m ahead of a vehicle being driven. The designated 30 m is exactly the same distance as the simulated R_L measured by certified devices.

The results show a relatively high correlation between these two parameters, providing a promising research direction of using road marking image brightness to forecast the field R_L. However, given the constraints of the research scale, several restrictions and limitations exist in the study, which require further investigation. These are listed below.

- Additional types of road marking materials should be 1. included. In this study, only three types of yellow road markings were used. Although they were easily distinguishable, additional types of road markings can better provide further information to regression curves in terms of image brightness and R_L. Furthermore, white lane line road markings should also be analyzed in future studies.
- A testing vehicle was used to capture the road marking 2. images during the field experiments. The analyzed results were based on the given vehicle's headlights luminance. Given that the luminance of vehicle headlights varies by vehicle brand and model, the illumination of road markings may thus differ with various vehicles. Therefore, further studies should focus on how headlight luminance affects image brightness and distance relation and the consequent relationship between road marking R_L and image brightness.
- A dual-lens camera with 6 cm lateral distance between 3. lenses was adopted for road marking image recording. Theoretically, the lateral distance may influence the accuracy of longitudinal distance calculation of an image. In addition, the quality and image exposure condition of dual-lens may affect the calculated brightness. It is suggested that to use a wide dual-lens camera and specify the required specifications for image collection in the future study.

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Conflicts of interest: To the best of our knowledge, the named authors have no conflict of interest/competing interests.

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Reference

- Federal Highway Administration, Summary of the MUTCD pavement marking retroreflectivity standard. (FHWA, 2010). https://safety.fhwa.dot.gov/roadway_dept/night_visib/fhwas a10015/. Accessed 3 June 2020.
- [2] American Society for Testing and Materials, Standard Specification for Thermoplastic Pavement Markings in Non-Snow Plow Areas. ASTM D7942-15. ASTM International, West Conshohocken, PA, USA, 2015.
- [3] The Central, East and West Nippon Expressway Company Limited, Lane marking construction management guidelines, Japan (in Japanese), Tokyo, Osaka, and Nagoya, Japan, 2015.
- [4] Hong Kong Highways Department, Guidance notes on road markings, Appendix 1: sample particular specification for road markings, Hong Kong, China. 2015.
- [5] European Committee for Standardization, Road markings materials: Road marking performance for road users. CEN-EN 1436. CEN, Brussels, Belgium, 2018.
- [6] National Standards of the Republic of China, Standard Test Method for Measuring the Characteristics of Pavement Marking Materials, Taiwan Bureau of Standards, Metrology, and Inspection. CNS 15834. CNS, Taipei, Taiwan, Republic of China, 2015.
- [7] R. J. Benz, A. M. Pike, S. P. Kuchangi, Q. Brackett, Serviceable pavement marking retroreflectivity levels: Technical report. College Station, Texas. Texas Transportation Institute, Texas A & M University System College Station, Texas, USA, 2009.
- [8] T. Horberry, J. Anderson, M. A. Regan, The possible safety benefits of enhanced road markings: a driving simulator

evaluation, Transp. Res. Part F: Traffic Psychology Behaviour 9 (1) (2006) 77-87.

- [9] B. Li, D. Song, H. Li, A. Pike, P. Carlson, Lane Marking Quality Assessment for Autonomous Driving, 2018 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS), Madrid, Spain, 2018 https://doi: 10.1109/IROS.2018.8593855.
- [10] American Society for Testing and Materials, Standard Test Method for Measurement of Retroreflective Pavement Marking Materials with CEN-Prescribed Geometry Using a Portable Retroreflectometer. ASTM E1710-11. ASTM International, West Conshohocken, PA, USA, 2011.
- [11] American Society for Testing and Materials, Standard Test Method for Measuring the Coefficient of Retroreflected Luminance (RL) of Pavement Markings in a Standard Condition of Wetness. ASTM E2177-11. ASTM International, West Conshohocken, PA, USA, 2011.
- [12] R. Girshick, J. Donahue, T. Darrell, J. Malik, Rich feature hierarchies for accurate object detection and semantic segmentation, 2014 IEEE conference on computer vision and pattern recognition, Washington DC, USA, 2014, pp 1–10.
- [13] R. Girshick, Fast R-CNN, IEEE International Conference on Computer Vision (ICCV), Santiago, Chile, 2015, pp. 1440-1448.
- [14] S. Ren, K. He, R. Girshick, J. Sun, Faster R-CNN: Towards real-time object detection with region proposal networks, Adv. Neural Information Processing Systems, Montreal, Canada, 2015, pp. 91-99.
- [15] K. He, G. Gkioxari, P. Dollár, R. Girshick, Mask R-CNN, IEEE International Conference on Computer Vision (ICCV), Venice, Italy, 2017, pp. 2961-2969.
- [16] A. Saxena, S. H. Chung, A. Y. Ng, Learning depth from single monocular images, Advances in neural information processing systems, Vancouver, Canada 2006, pp. 1161-1168.
- [17] M. Pollefeys, D. Nistér, J. M. Frahm, A. Akbarzadeh, P. Mordohai, B. Clipp, C. Engels, et al., Detailed real-time urban 3D reconstruction from video, Inter. J. Comput. Vision 78 (2-3) (2008) 143–167 https://doi.org/10.1007/s11263-007-0086-4.
- [18] C. Olaverri-Monreal, G. C. Krizek, F. Michaeler, R. Lorenz, M. Pichler, Collaborative approach for a safe driving distance using stereoscopic image processing, Future Generation Comput. Syst. 95 (2019) 880–889 https://doi.org/10.1016/j.future.2018.01.050
- [19] S. V. Stehman, Selecting and interpreting measures of thematic classification accuracy, Remote Sensing Environ.
 62 (1) (1997) 77–89 https://doi.org/10.1016/S0034-4257(97)00083-7
- [20] S. Ranjbar, F. M. Nejad, H. Zakeri, An image-based system for pavement crack evaluation using transfer learning and wavelet transform, Inter. J. Pavement Res. Technol. (2020) https://doi.org/10.1007/s42947-020-0098-9
- [21] American Association of State Highway and Transportation Officials, Standard Specification for Glass Beads Used in Pavement Markings. AASHTO M247-13. AASHTO, Washington DC, USA, 2018.