**Research Article** 

# Extension of BET theory to CO<sub>2</sub> adsorption isotherms for ultra-microporosity of covalent organic polymers

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#### Abstract

Usually, nitrogen and argon adsorption–desorption isotherms are used at their respective boiling points for the determination of specific surface area via the BET theory of microporous materials. However, for ultra-micropores, where nitrogen and argon cannot access at cryogenic temperatures, the CO<sub>2</sub> adsorption–desorption isotherms have been considered as alternative options for the determination of specific surface area by extending BET theory, but the surface area determined by using CO<sub>2</sub> adsorption–desorption isotherms is not significant due to strong CO<sub>2</sub>-CO<sub>2</sub> interactions. In this study, the microporous covalent organic polymers are subjected to nitrogen and CO<sub>2</sub> adsorption–desorption isotherms and the results showed that a clear linear region is available in isotherms, which confirms the presence of ultra-micropores. The surface area determined by the CO<sub>2</sub> adsorption–desorption isotherms is higher than the surface area determined by N<sub>2</sub> adsorption–desorption isotherms. These results indicate that the microporous covalent organic polymers contain ultra-micropores where only CO<sub>2</sub> can reach, while nitrogen and argon cannot access at cryogenic conditions because their kinetic diameter is larger than CO<sub>2</sub>.

 $\label{eq:constraint} \textbf{Keywords} \ \ Covalent \ organic \ polymers \cdot BET \ theory \cdot Adsorption-desorption \ isotherms \cdot Ultra-microporosity \cdot Surface \ area$ 

## **1** Introduction

The surface area of porous materials is one of the significant properties because it significantly influences the performance of porous adsorbents in many applications including gas adsorption capacity [1–4], catalysis [5–7], and gas separations [8–11]. Brunauer–Emmett–Teller (BET) [12, 13] technique is one of the most prominent analyses based on argon or nitrogen gas adsorption–desorption isotherms to determine the surface of microporous materials [14], such as zeolites [15], metal–organic frameworks (MOFs) [16], and covalent organic polymers (COPs).

Most of the porous materials have pore texture properties generated from their specific synthesis methods such as (1) precursor particles originated from a solution that produces agglomeration and results a porous structure, (2) synthesis of crystalline compounds such as zeolites or other through hydrothermal crystallization, where the particular arrangement of building blocks yields intra-crystalline pores of molecular size, (3) the thermal treatments including burning or evaporation which may eliminate the volatile compounds or impurities and produce pores as a result of both exist ways of eliminated materials and solid rearrangements, and (4) the selective dissolution of some components that can produce molecular size cavities [17, 18]. Therefore, most of the porous materials are classified into four major groups based on their pore size including micropores (< 2 nm), ultra-micropores (< 0.7 nm), mesopores (2 nm < pore size < 50 nm), and macropores (> 50 nm) [19, 20].

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Some of the researchers have questioned the applications of BET theory to the microporous materials because the origin of this theory is based on the gas adsorption-desorption on flat surfaces of adsorbent materials. From a simulation study carried out by Walton et al. [21], they proposed that BET theory can be applied for the determination of the surface area of porous materials containing micropores with a size in the range of  $(7-20 \times 10^{-10} \text{ m})$  [22, 23]. Hence, this work aims to investigate the application of BET theory on CO<sub>2</sub> adsorption-desorption isotherms for the surface area determination for covalent organic polymers (COPs) containing ultra-micropores.

### 2 Materials and methods

Nitrogen-rich porous covalent triazine-based organic polymer has been used in the work for surface area determination through nitrogen as well as  $CO_2$  adsorption–desorption isotherms via BET analysis. The surface area was determined using N<sub>2</sub> adsorption–desorption isotherms at 77 K and  $CO_2$  adsorption–desorption isotherms at 273 K. The sample is outgassed at 393 K for 3 h to remove moisture contents.

## **3** Results and discussions

The N<sub>2</sub> and CO<sub>2</sub> adsorption-desorption isotherms obtained were further subjected to the BET analysis as shown in Fig. 1. The results show that according to the IUPAC classification of adsorption isotherms [24], the N<sub>2</sub> isotherm resembles the type III having sharp adsorption capacity while indicating the presence of broader pore size distributions, narrower mesopores, and wider micropores. The small hysteresis present in the N<sub>2</sub> adsorption–desorption isotherm is an indication of the capillary condensation phenomenon indicating the mesoporous nature [25]. There is no significant hysteresis observed in the  $CO_2$  adsorption–desorption isotherms which is an indication of easy desorption of the  $CO_2$  molecules because of thermal vibrations of molecules that are in agreement with the reported studies [26, 27].

To investigate the application of BET theory for surface area determination using CO<sub>2</sub> adsorption isotherms, we followed a method reported by Walton and Bae [21, 28]. The BET theory was applied to CO<sub>2</sub> adsorption isotherm by plotting a graph between x as a function of the x axis and x/q(1-x) as a function of the y-axis, where x is  $P/P_o$  for CO<sub>2</sub> at 273 K and q is the adsorption capacity of CO<sub>2</sub> over COP. The intercept of the plot yields [c-1/q], while the slope yields [1/qc] in the linear region of the plot. To satisfy these criteria of calculating surface area, two conditions must be fulfilled: (1) the value of  $q(P-P_o)$  should be increased with increasing x, and (2) the y intercept in the linear region of the graph must yield a positive value, which must be greater than zero to get the meaningful value of c. Finally, the surface can be calculated using Eq. 1:

$$A = q \times \sigma_{\rm o} \times N_{\rm AV} \tag{1}$$

where *q* is the adsorption capacity of CO<sub>2</sub> at 273 K,  $\sigma_{o}$  is the cross-sectional area of CO<sub>2</sub> at 273 K, which is  $21.8 \times 10^{-10}$  m, and  $N_{AV}$  is the Avogadro's number, which is  $6.022 \times 10^{23}$  mol<sup>-1</sup>.

The graphical representation of this method is presented in Fig. 2. The surface area from  $CO_2$  adsorption isotherm is calculated using Eq. (1) at 273 K and from  $N_2$  adsorption isotherm at 77 K which is tabulated in Table 1. We now investigate the surface area determination using  $CO_2$  adsorption isotherms only in the linear region because the linearity of the BET plot is a key factor for the determination of the accurate specific surface



Fig. 1 N<sub>2</sub> and CO<sub>2</sub> adsorption-desorption isotherms at 77 K and 273 K, respectively

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Fig. 2 Application of BET theory on CO<sub>2</sub> adsorption isotherms at 273 K

Table 1 BET surface area calculated by applying BET theory on  $\rm N_2$  and  $\rm CO_2$  adsorption isotherms

Material	S <sub>BET</sub> (m²/g) from N <sub>2</sub> isotherm	S <sub>BET</sub> (m²/g) from CO <sub>2</sub> isotherm	References
СОР	22	23	This work
MOF-177	1721	47	[29]
MOF-200	3624	1265	[30]
MOF-200/GO	3359	167	[30]

area of porous materials. Since the selection of a linear region in the convex or concave-shaped plot is not difficult, it can be identified easily. However, in the selection of the linear region, it must be considered that the linear range should be in the low pressure range and there should not be any overshooting in CO<sub>2</sub> adsorption capacity. The results clearly show that the surface area calculated from CO<sub>2</sub> adsorption isotherms at 273 K is higher than the surface area calculated using N<sub>2</sub> adsorption isotherm at 77 K. It can be considered that surface area calculated by CO<sub>2</sub> adsorption isotherm may be accounted for the ultramicroporosity because of its small kinetic diameter than N<sub>2</sub> molecules. However, the diffusional resistances due to the temperature of the adsorption process are one of the significant parameters which affect the reach of adsorbate molecules into the ultra-micropores. The results are in agreement with the previously reported studies [21]. In comparison with the reported literature, Sami et al. [29] and his coworkers reported the experimental investigation of the ultra-microporosity determination in a metal-organic framework (MOF-177) by employing the CO<sub>2</sub> adsorption for BET technique. The results revealed that the absence of any ultra-micropores in the MOF-177 as the specific surface area of the MOF-177 was reduced from 1721.09 to 47.4739  $m^2/g$  when N<sub>2</sub> and CO<sub>2</sub> gases were used for BET technique, respectively. Similarly, in another work, Sami et al. [30] and his coworkers reported



the ultra-microporosity analysis of the two metal–organic frameworks: one was unfunctionalized (MOF-200) and one was functionalized with the graphene oxide (MOF-200/ GO). The results again demonstrated the loss of the specific surface areas of both metal and organic frameworks, i.e., MOF-200 (1265 m<sup>2</sup>/g) and MOF-200/GO (167 m<sup>2/</sup>g) from MOF-200 (3624 m<sup>2</sup>/g) and MOF-200/GO (3359 m<sup>2</sup>/g). This was an indication of the absence of any ultra-micropores in the MOF-177 as the surface area of the MOF-177 was reduced from 1721.09 to 47.4739 m<sup>2</sup>/g when N<sub>2</sub> and CO<sub>2</sub> gases were used for BET technique, respectively. However, both reported studies revealed that the reported method can be employed for the ultra-microporosity analysis.

#### 4 Conclusion

In this study, a porous covalent organic polymer (COP) was subjected to the BET analysis to investigate the application of BET theory for specific surface area determination using N<sub>2</sub> adsorption isotherm at 77 K and CO<sub>2</sub> adsorption isotherm at 273 K. The results showed that the surface area determined by using the CO<sub>2</sub> adsorption isotherms was higher than the surface area determined by using the  $N_2$ adsorption isotherms. The results provided a clear indication of the presence of an ultra-microporous region in the microporous structure. The results recommend the meaningfulness of CO<sub>2</sub> adsorption isotherms for the surface area determination in the ultra-microporosity using BET theory. Future research can be carried out to investigate the comparative effect of the kinetic diameter of the adsorbate molecule and diffusive resistance due to the temperature of the adsorption process on the ultra-microporosity.

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#### **Compliance with ethical standards**

**Conflict of interest** The authors have not any conflict of interest regarding the publication of this paper.

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