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# Synthesis and characterization of $K_2Pr_2O(BO_3)_2$ : structural, spectroscopic and thermogravimetric investigations of a novel potassium praseodymium oxoborate structure-type



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#### Abstract

Single crystal and polycrystalline powder samples of a new potassium praseodymium oxoborate  $K_2Pr_2O(BO_3)_2$  were prepared by high-temperature solid-state methods. The crystal structure obtained from single-crystal X-ray diffraction data was confirmed by powder X-ray data Rietveld refinement ( $P2_1/c$ , a = 1135.00(3) pm, b = 660.64(2) pm, c = 1072.03(3) pm,  $\beta = 117.128(2)^\circ$ ,  $V = 715.41(3) \times 10^6$  pm<sup>3</sup>). The bond-valence sum of the central cation for KO<sub>6/7</sub>, PrO<sub>9</sub> and BO<sub>3</sub> coordination lies close to the respective empirical value. Both Fourier-transform infrared and Raman spectroscopy demonstrated the vibrational features of the isolated BO<sub>3</sub> planar group. The diffuse UV/Vis reflectance spectra showed fundamental absorption edge at 4.49(1) eV obtained from the combined approach using Tauc and derivation of absorption spectrum fitting methods. The greenish color of the sample was identified originating from 4f-4f-electron transitions. The thermal stability was investigated by using simultaneous thermogravimetric analysis and differential scanning calorimetry. The decomposed products  $Pr_{26}O_{27}(BO_3)_8$  (90(2) wt%) and  $Pr_6O_{11}$  (10(2) wt%) were confirmed by powder X-ray diffraction data analysis, complementary to the weight-loss during the heating process. Since  $Pr^{3+}$  cation is known to show interesting photoluminescence property, this novel compound may be a prospective candidate as phosphor.

**Keywords** Potassium praseodymium borate · Crystal structure · Vibrational property · Optical property · Thermal stability

### 1 Introduction

Inorganic rare-earth borates have received intensive interests owing to their wide range of applications in nonlinear optics (NLO), laser hosts and photoluminescence materials [1–3]. Among the most attractive features of borate crystals, the key characteristics are their transparency in the wide range from mid-infrared to deep-ultraviolet [4], high optical damage threshold [5] and suitable physico-chemical stability [6]. Hitherto, Na<sub>3</sub>La<sub>9</sub>O<sub>3</sub>(BO<sub>3</sub>)<sub>8</sub> [7], La<sub>2</sub>CaB<sub>10</sub>O<sub>19</sub> [8], and YAl<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub> [9] have been widely used as NLO crystals for second harmonic generation (SHG). Since the ionic radii of the rare-earth elements are close to each other, these rare-earth borates are favorable to host optical active cations such as  $Ce^{3+}$ ,  $Nd^{3+}$  and  $Yb^{3+}$  [10]. Therefore, the rare-earth borates can further serve as an array of functional materials in optics:  $Ce^{3+}:Li_6Y(BO_3)_3$  [11] as scintillator materials for neutron detection,  $Nd^{3+}:YAl_3(BO_3)_4$  [12] as crystals for green laser emission, and  $Yb^{3+}:LiGd_6O_5(BO_3)_3$ [13] as ultrashort-pulse lasers. Rare-earth orthoborate YBO<sub>3</sub> doped with  $Eu^{3+}$  and  $Tb^{3+}$  [14] are appropriate phosphors in plasma-display panels due to their high luminous efficacy and thermally stable luminescence yield.

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Recently, Pr<sup>3+</sup> cation-doping materials have drawn an intense research attention due to their promising applications in white-light emitting diodes [15–17]. The Pr<sup>3+</sup> cation is able to release rich fluorescence spectral lines in the red, orange, green, and blue regions, which originate from the electronic transition between the 4f inner-shell configurations. For instance, in the alkali-metal borates steady and high-efficiency red emission have been detected in  $Pr^{3+}$ :KSr<sub>4</sub>(BO<sub>3</sub>)<sub>3</sub> powder [18],  $Pr^{3+}$ :Na<sub>3</sub>La<sub>9</sub>O<sub>3</sub>(BO<sub>3</sub>)<sub>8</sub> crystal [19] and Pr<sup>3+</sup> doped lithium borate glasses [20] when activated by blue or ultraviolet light due to  ${}^{3}P_{0} \rightarrow {}^{3}H_{6}$ and  ${}^{1}D_{2} \rightarrow {}^{3}H_{4}$  transitions. Despite much works on Pr<sup>3+</sup>-doped borates, purely praseodymium borates have not been extensively studied. In search of novel rare-earth borate compounds the present investigation focus on  $A_2O-Pr_2O_3-B_2O_3$  (A = alkali metal) quasi-ternary systems and their crystal-, chemico-physical properties. To the best of our knowledge, only  $Li_3Pr_2(BO_3)_3$  [21],  $LiPr_6O_5(BO_3)_3$  [22],  $Na_3Pr(BO_3)_2$  [23] and  $K_9Li_3Pr_3(BO_3)_7$  [24] were reported in these ternary systems. The alkali-metal praseodymium borate K<sub>2</sub>Pr<sub>2</sub>O(BO<sub>3</sub>)<sub>2</sub> has been found to be a new member of the K<sub>2</sub>La<sub>2</sub>(BO<sub>3</sub>)<sub>2</sub>O family [25]. The report particularly emphasizes on the synthesis, crystal structure, vibrational, optical and thermal properties of  $K_2Pr_2O(BO_3)_2$ .

# 2 Experimental

# 2.1 Synthesis

Single crystals of  $K_2Pr_2O(BO_3)_2$  were obtained by means of the flux-assisted solid state reaction method. The starting materials  $K_2CO_3$ ,  $PrO_2$  and  $H_3BO_3$  with a molar ratio of 1.5: 2: 3, respectively, were thoroughly ground in an agate mortar, and put into a platinum crucible. The mixture of the starting chemicals can be regarded as the target product  $K_2Pr_2O(BO_3)_2$  together with the assisted-flux  $KBO_2$ in the molar ratio of 1:1. The crucible was heated up to 1173 K in a muffle furnace with a heating rate of 100 K/h and maintained at that temperature for 12 h. Afterward, the crucible was cooled down to room temperature with a cooling rate of 300 K/h. The obtained greenish single crystals are found to be chunk-shaped with a dimension of tens of micrometer.

The polycrystalline samples of  $K_2Pr_2O(BO_3)_2$  were prepared using a solid-state synthesis method in a platinum crucible. First, a stoichiometric batch of intimately mixed  $K_2CO_3$ ,  $PrO_2$  and  $H_3BO_3$  (analytical grade) was heated at 773 K for 12 h to completely decompose  $K_2CO_3$  and  $H_3BO_3$ . The resulting samples were then ground in agate mortar and heated further at 1123 K for 48 h. A 10% excess molar ratio of  $K_2CO_3$  was added into the samples during the sintering process to compensate the evaporation of

SN Applied Sciences A Springer Nature journal potassium. The mixtures were repeatedly heated at 1123 K with intermediate grindings until their powder X-ray diffraction pattern confirms a pure phase.

# 2.2 X-ray single crystal diffraction

The small crystals of  $K_2Pr_2O(BO_3)_2$  were isolated by mechanical fragmentation and picked using a polarization microscope. Single-crystal diffraction data were collected on a Bruker D8-Venture diffractometer in Kappa geometry with Mo<sub>k $\alpha$ </sub> radiation ( $\lambda_{k\alpha}$  = 71.0747(6) pm) at 297(2) K. A numerical absorption correction was applied to the intensity data sets. The systematic extinctions and  $|E^2 - 1|$ statistics suggested the monoclinic space group  $P2_1/c$ ; therefore the structure determination of K<sub>2</sub>Pr<sub>2</sub>O(BO<sub>3</sub>)<sub>2</sub> was performed in this space group. The structure was finely solved via the intrinsic phasing method and successfully refined on F<sup>2</sup> by full-matrix least-square methods with the ShelxT and Shelxle program packages [26, 27]. All atoms were refined with anisotropic displacement parameters and the final difference Fourier synthesis did not reveal any significant residual electron density. All relevant details of the data collection and the refinement are listed in Table 1, atomic coordinates and displacement parameters in Table 2 and the bond valence sums (BVSs) in Table 3.

Further details of the crystal structure information can be obtained from FIZ Karlsruhe, 76,344 Eggenstein Leopoldshafen, Germany (fax: +49-7247-808-666; e-mail: crysdata@fiz-karlsruhe.de) on quoting the deposition number CSD-1978814.

# 2.3 X-ray powder diffraction

The powder X-ray diffraction (PXRD) pattern was recorded on a Panalytical X'Pert Pro powder diffractometer using Bragg-Brentano geometry with CuK<sub>q1,2</sub>  $(\lambda_{ka1} = 154.05929(5) \text{ pm}, \lambda_{ka2} = 154.4414(2) \text{ pm})$  radiation. The measurement was carried out at ambient condition in a range between 5° and 130°  $2\theta$  with a step size of 0.0167° and a data collection time of 30 s/step. The fundamental parameter approach, where the fundamental parameters were fitted against a LaB<sub>6</sub> standard material, was applied for the Rietveld refinement using "Diffrac<sup>Plus</sup> Topas 6" software (Bruker AXS GmbH, Karlsruhe, Germany). The starting lattice parameters and atomic coordinates were taken from the results of the single crystal structure determination. The average crystallite size was calculated from all observed X-ray reflections, which is described as  $L_{Vol}(IB)$ by the TOPAS suite. Of notes,  $L_{Vol}(IB)$  refers to the volumeweighted mean of the coherently diffracted domain size using the integral breadth for the description of the reflection profile.

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Table 1Crystal structuredetermination of  $K_2 Pr_2 O(BO_3)_2$ in the space group  $P2_1/c$  (No.14) from single crystal andpowder X-ray diffraction data

Crystals	Single	Powder
Dimension (μm³)/L <sub>vol</sub> (IB) (nm)	93×66×52	249(8)
<i>a</i> (pm)	1133.77(3)	1135.00(3)
<i>b</i> (pm)	660.47(2)	660.64(2)
<i>c</i> (pm)	1071.30(3)	1072.03(3)
β(°)	117.07(1)	117.13(1)
Ζ	4	4
Temperature (K)	297(2)	300(2)
Diffractometer	Bruker D8 Venture	Panalytical X'Pert Pro
Wavelength (pm)	71.0747(6)	154.1866(1)
Absorption coefficient (mm <sup>-1</sup> )	14.638	113.568(6)
Absorption correction method	Numerical	
F(000)/e <sup>-</sup>	888	888
<i>θ/2θ</i> range (°)	2.017-46.021	5–130
Range in <i>hkl</i>	$-22 \le h \le 20,$	0≤h≤13,
	$-12 \le k \le 13$ ,	0≤k≤7
	$-20 \le l \le 21$	0≤ ≤11
Reflections collected	64145	1230
Data/restraints/parameters	6129/0/119	7480/8/54
Goodness-of-fit on <i>F</i> <sup>2</sup>	1.043	1.92
$R_1/wR_2 [I > 2\sigma(I)]$	0.0318/0.0566	$R_p = 0.0588$
$R_1/wR_2$ (all data)	0.0401/0.0438	$R_{wp} = 0.07786$

### 2.4 UV/Vis spectroscopy

The UV/Vis diffuse reflectance measurement was collected from 200 to 850 nm with a step of 1 nm on a UV-2700 spectrophotometer (Shimadzu, Japan) equipped with an ISR-2600 plus two-detector integrating sphere (Pike Technologies, USA). The baseline correction was carried out against BaSO<sub>4</sub> powder.

#### 2.5 Vibration spectroscopy

The Fourier transform infrared (FTIR) spectrum was recorded on a Bruker IFS66v/S spectrometer using the standard KBr method between 370 and 4000 cm<sup>-1</sup>. KBr pallets consist of 2 mg sample mixed with 200 mg KBr (sample) and 200 mg KBr (reference), pressed at 100 kN, forming disks of 12 mm in diameter.

Due to laser induced susceptibility of the 4*f*-electronic transitions the Raman spectra were measured at ambient condition using at least three lasers (532 nm, 633 nm and 785 nm), and found that the band numbers and the respective frequency positions are laser-independent. To avoid the absorption areas (see UV–Vis reflectance spectrum below), the 785 nm laser was chosen for better spectral resolution. Temperature-dependent Raman spectra were recorded on a LabRam ARAMIS (Horiba Jobin Yvon) Micro-Raman spectrometer equipped with a laser working at 785 nm and less than 5 mW power on the sample

surface. The use of a 50×long working distance objective (Olympus) with a numerical aperture of 0.55 provides a focus spot of about 2 µm diameter when closing the confocal hole to 200 µm. Raman spectra were collected in the range 85–1700 cm<sup>-1</sup> with a spectral resolution of approximately 1.1 cm<sup>-1</sup> using a moving grating of 1800 grooves/ mm and a thermoelectrically cooled CCD detector (Synapse, 1024 × 256 pixels). The spectral positions were calibrated against the Raman mode of Si before and after the sample measurements. The position of the Si peak was repeatedly measured against the Rayleigh line  $(0.0 \text{ cm}^{-1})$ yielding a value of  $520.7 \pm 0.1$  cm<sup>-1</sup>. The linearity of the spectrometer was calibrated against the emission lines of a neon lamp. For the low-temperature measurements, a pressed pellet of powder sample was placed on a Linkam cooling stage (THMS600) attached to a pump (LNP95 Cooling Pump) that provides a continuous flow of liquid nitrogen. The measurements were carried out between 78 and 300 K. A ramp rate of 5 K/min and a holding time of 5 min were followed to properly equilibrate the temperature. For the spectrum at ambient condition the baseline was linearly corrected, bands were fitted with Pseudo-Voigt lineshape.

#### 2.6 Thermal analysis

Simultaneous thermogravimetric analysis/differential scanning calorimetry (TGA/DSC) measurements were

Table 2	Crystal structural data
of K <sub>2</sub> Pr <sub>2</sub>	$O(BO_3)_2$

Atom	Wyckoff	SOF	X	у	Z	U <sub>eq</sub>	B <sub>iso</sub>
Pr1	4e	1	0.51850(2)	0.04466(2)	0.31939(2)	49.0(2)	-
			0.5184(3)	0.0452(4)	0.3202(3)	-	0.46(5) <sup>a</sup>
Pr2	4e	1	0.32360(2)	0.41647(2)	0.41561(2)	56.3(2)	-
			0.3230(3)	0.4159(4)	0.4162(3)	-	0.46(5) <sup>a</sup>
K1 4e	1	0.03193(5)	0.06011(7)	0.26414(5)	129.9(8)	-	
			0.0320(9)	0.0569(15)	0.2666(10)	-	0.55(18) <sup>b</sup>
K2	4e	1	0.11866(5)	0.74422(8)	0.05575(5)	137.7(3)	-
			0.1200(9)	0.7564(15)	0.0596(12)	-	0.55(18) <sup>b</sup>
B1	4e	1	0.6946(2)	0.3446(3)	0.1441(2)	67(3)	-
			<i>0.6946</i> <sup>d</sup>	0.3446 <sup>d</sup>	0.1441 <sup>d</sup>	-	0.529 <sup>d</sup>
B2	4e	1	0.1978(2)	0.2469(3)	0.0897(2)	73(3)	-
			0.1978 <sup>d</sup>	0.2469 <sup>d</sup>	0.0897 <sup>d</sup>	-	0.576 <sup>d</sup>
01	4e	1	0.79983(15)	0.2513(2)	0.14046(17)	103(3)	-
			0.808(3)	0.258(5)	0.144(3)	-	1.5(3) <sup>c</sup>
O2	4e	1	0.12430(16)	0.3490(3)	0.46490(17)	114(3)	
			0.128(3)	0.327(4)	0.482(3)		1.5(3) <sup>c</sup>
O3	4e	1	0.14560(16)	0.3469(3)	0.16568(17)	119(3)	-
			0.154(2)	0.363(4)	0.169(3)	-	1.5(3) <sup>c</sup>
O4	4e	1	0.63161(15)	0.2468(2)	0.21263(17)	90(3)	-
			0.622(3)	0.267(4)	0.221(3)	-	1.5(3) <sup>c</sup>
O5	4e	1	0.52705(15)	0.3776(2)	0.40277(16)	77(2)	-
			0.528(3)	0.395(4)	0.419(3)	-	1.5(3) <sup>c</sup>
O6	4e	1	0.33651(15)	0.2428(2)	0.13950(17)	97(3)	-
			0.346(3)	0.233(4)	0.142(3)	-	1.5(3) <sup>c</sup>
07	4e	1	0.35215(16)	0.0341(2)	0.41402(17)	92(3)	-
			0.361(2)	0.010(4)	0.402(3)	-	1.5(3) <sup>c</sup>

The isotropic  $(B_{iso}/10^4 \times pm^2)$  and equivalent isotropic  $(U_{eq}/pm^2)$  atomic displacement parameters are obtained from powder X-ray and single crystal X-ray diffraction data analysis, respectively

<sup>a,b,c</sup>Values with the same letters were constrained to each other during the refinements

<sup>d</sup>These values were fixed during the refinement. U<sub>ii</sub> tensors can be obtained from CSD-1978814

performed on TGA/DSC 3<sup>+</sup> STAR<sup>e</sup> system of Mettler Toledo. The sample was measured with a heating rate of 10 K/min and a continuous N<sub>2</sub> flow of 20 mL/min from 300 to 1473 K. Afterward, the data were normalized to their respective mass. Approximately 16.159 mg of K<sub>2</sub>Pr<sub>2</sub>O(BO<sub>3</sub>)<sub>2</sub> was measured relative to an empty corundum crucible as the reference. A drift correction was applied based on empty crucible data.

# **3** Results and discussion

### 3.1 Crystal structure of K<sub>2</sub>Pr<sub>2</sub>O(BO<sub>3</sub>)<sub>2</sub>

K<sub>2</sub>Pr<sub>2</sub>O(BO<sub>3</sub>)<sub>2</sub> crystallizes in a new structure type in the monoclinic space group  $P2_1/c$  (no. 14) with lattice parameters of a = 1133.77(3) pm, b = 660.47(2) pm, c = 1071.30(3) pm,  $\beta = 117.072(1)^\circ$ , and Z = 4. The structural building units of K<sub>2</sub>Pr<sub>2</sub>O(BO<sub>3</sub>)<sub>2</sub>, as shown in Fig. 1, can be regarded as PrO<sub>8</sub>

SN Applied Sciences A Springer Nature journal dodecahedra, KO<sub>6</sub> octahedra and KO<sub>7</sub> pentagonal bipyramid together with isolated trigonal planar BO<sub>3</sub> groups. Both Pr(1) and Pr(2) form distorted PrO<sub>8</sub> dodecahedra, where the Pr-O bond lengths vary from 235.9(2) pm to 260.1(2) pm in Pr(1)O<sub>8</sub>, and from 234.6(2) to 274.6(2) pm in  $Pr(2)O_8$ . The  $Pr(1)O_8$  dodecahedra are axially connected with its neighbors via sharing two triangular faces to construct an infinite zig-zag chain along the *b*-axis (Fig. 1b). These zig-zag chains are further joined together by edgesharing to form infinite two dimensional  $Pr(1)O_{(3+3+2)/2}$ layers with elongated hexagonal voids in the *bc*-plane. Such a 2D REO<sub>n</sub> layer with "honeycomb-like" voids was also found in other rare-earth borates, for instance, in Na<sub>3</sub>La<sub>2</sub>(BO<sub>3</sub>)<sub>3</sub> [28]. By contrast, two Pr(2)O<sub>8</sub> dodecahedra share their O(5)-O(5) edge to construct  $Pr(2)_2O_{14}$  dimers that fill into those "honeycomb-like" voids (Fig. 1c). It is interesting to mention that O(5), the isolated oxygen anion in  $K_2Pr_2O(BO_3)_2$ , connects only to Pr-atoms and plays an important role in the formation of a  $Pr(2)_2O_{14}$  dimer.

Table 3 Interatomic bond distance/pm and bond valence (BV/v.u.) and bond valence sum (BVS/v.u.) of the  $PrO_8$ ,  $KO_{6,7}$  and  $BO_3$  polyhedra in  $K_2Pr_2O(BO_3)_2$ 

Bond	Bond length	BV	Bond	Bond length	BV
Pr10 <sub>8</sub>			Pr2O <sub>8</sub>		
Pr1-05	235.9(2)	0.551(2)	Pr2-05	234.6(2)	0.570(2)
Pr1-05	245.6(2)	0.424(2)	Pr2-05	238.6(2)	0.511(3)
Pr1-06	246.3(2)	0.416(1)	Pr2-01	253.9(2)	0.339(1)
Pr1-O4	246.4(2)	0.415(2)	Pr2-07	254.7(2)	0.331(1)
Pr1-06	249.3(2)	0.384(2)	Pr2-03	255.6(2)	0.323(1)
Pr1-07	251.6(2)	0.360(2)	Pr2-06	256.2(2)	0.318(2)
Pr1-04	252.0(2)	0.356(1)	Pr2-02	258.25(2)	0.301(2)
Pr1-07	260.1(2)	0.286(1)	Pr2-04	274.6(2)	0.193(1)
	BVS(Pr1)	3.190(5)		BVS(Pr2)	2.886(5)
K1O <sub>6</sub>			K2O <sub>7</sub>		
K1–O1	265.9(2)	0.241(1)	K2-01	265.4(2)	0.244(1)
K1–O1	266.5(2)	0.237(1)	K2-O2	275.0 (2)	0.188(1)
K1–O2	267.3(2)	0.232(1)	K2-04	278.91(2)	0.169(1)
K1–O2	270.4(2)	0.213(1)	K2-O3	283.51(2)	0.149(1)
K1–O3	275.7(2)	0.185(1)	K2-O2	286.8(2)	0.137(1)
K1–O3	282.4(2)	0.154(1)	K2-O3	291.5(2)	0.121(0)
			K2-01	295.1(2)	0.109(1)
	BVS(K1)	1.261(1)		BVS(K2)	1.118(1)
B1O <sub>3</sub>			B2O <sub>3</sub>		
B1-O1	135.9(3)	1.033(8)	B2-O2	136.7(3)	1.011(7)
B1-07	139.1(3)	0.948(6)	B2-O3	137.3(3)	0.992(9)
B1-04	139.3(3)	0.939(8)	B2-O6	141.3(3)	0.894(7)
	BVS(B1)	2.920(13)		BVS(B2)	2.897(13)

Therefore,  $[Pr_2O(BO_3)_2]^{2-}$  sheets are composed of Pr(1)  $\rm O_{(3+3+2)/2}$  layers,  $\rm Pr(2)_2O_{14}$  dimers, isolated B(1)O\_3 and B(2) O<sub>3</sub> planar groups via corner and edge sharing in the acplane. Two adjacent  $[Pr_2O(BO_3)_2]^{2-}$  sheets in the structure are regulated by the inversion center (Fig. 1d). Two types of potassium K(1) and K(2) are found to occupy the intersheet space and separate the  $[Pr_2O(BO_3)_2]^{2-}$  sheets along the a-axis. Similar stacking modes were also observed in other layered alkali-metal rare-earth borates such as K<sub>9</sub>Li<sub>3</sub>Nd<sub>3</sub>(BO<sub>3</sub>)<sub>9</sub> [24] and Rb<sub>2</sub>LiNd(BO<sub>3</sub>)<sub>2</sub> [24]. K(1) is six-fold coordinated to form a distorted K(1)O<sub>6</sub> octahedron while K(2) connects to seven oxygens in exhibition of a distorted pentagonal bipyramid K(2)O7. The K–O distances range from 265.9(2) to 282.4(2) pm with mean values of 273.6(2) pm and 282.3(2) pm for  $K(1)O_6$  and  $K(2)O_7$  polyhedra, respectively. These values fit well with the sum of the ionic radii of oxygen and potassium in sixfold and sevenfold coordination [29]. In the unit cell, both B(1) and B(2) atoms are three-coordinated to oxygen atoms, forming isolated planar BO<sub>3</sub> groups. The B-O distances range from 134.2(5) to 141.0(6) pm with an averaged bond length of 137.0(3) pm for  $B(1)O_3$  and 137.9(3) pm for  $B(2)O_3$ , respectively. These values are in agreement with those of other alkalimetal rare-earth borate-containing isolated BO<sub>3</sub> groups, for instance 137.1 pm in K<sub>3</sub>Sm(BO<sub>3</sub>)<sub>2</sub> [30], 137.4 pm in Li<sub>3</sub>K<sub>3</sub>Y<sub>7</sub>(BO<sub>3</sub>)<sub>9</sub> [31] and 137.6 pm in K<sub>9</sub>Li<sub>3</sub>Nd<sub>3</sub>(BO<sub>3</sub>)<sub>7</sub> [24]. The bond valence sums (BVS) calculation was performed for K<sub>2</sub>Pr<sub>2</sub>O(BO<sub>3</sub>)<sub>2</sub> using the Bondstr software of the FullProf suite [32], which are listed in Table 3. The structural BVSs of the atoms correspond well with the formal integer charge of the respective atoms. To confirm the single crystal structure of its bulk representative as well the purity of the assynthesized  $K_2Pr_2O(BO_3)_2$  polycrystalline powder sample, X-ray powder data Rietveld refinements were performed. The corresponding Rietveld plot is shown in Fig. 2. The metric parameters (a = 1135.00(3) pm, b = 660.641(15) pm, c = 1072.03(3) pm,  $\beta = 117.128(2)^{\circ}$  and  $V = 715.41(3) \times 10^{6}$ pm<sup>3</sup>) are in excellent agreement with those obtained from the single crystal structure determination (Tables 1, 2).

#### 3.2 UV/Vis spectrum

The UV/Vis reflectance spectrum of  $K_2Pr_2O(BO_3)_2$  in the range of 200–850 nm is shown in Fig. 3. The optical absorption in the visible range accounts for the green color of  $K_2Pr_2O(BO_3)_2$  and also corresponds well to the presence of  $Pr^{3+}$  cation. All visible absorption bands in  $K_2Pr_2O(BO_3)_2$ result from the inner-shell 4f<sup>2</sup>-configuration electronic transitions from the ground state  $({}^{3}H_{4})$  to various excited states. According to the energy level scheme proposed by Dieke and Crosswhite [33], these bands from 400 to 520 nm can be assigned, respectively to  ${}^{3}H_{4} \rightarrow {}^{3}P_{2}$ ,  ${}^{3}P_{1}$ , and <sup>3</sup>P<sub>0</sub>, while the band in the range of 550–650 nm ascribed to  ${}^{3}H_{4} \rightarrow {}^{1}D_{2}$ . Of particular notes, we clearly observe the Stark splitting of <sup>3</sup>P<sub>2</sub>, <sup>3</sup>P<sub>1</sub>, and <sup>3</sup>P<sub>0</sub> and <sup>1</sup>D<sub>2</sub> multiplets, which may help calculate the crystal field levels of Pr<sup>3+</sup> cation in K<sub>2</sub>Pr<sub>2</sub>O(BO<sub>3</sub>)<sub>2</sub>. The monotonic drop of the reflectance between 290 and 270 nm (Fig. 3) corresponds to the valence-to-conduction-band absorption edge. The Kubelka-Munk function [34] treatment followed by the Tauc method [35] are often used to estimate the corresponding bandgap energy by finding the intercept of the abscissa from the following relations:

$$F(R) = \frac{(1-R)^2}{2R}$$
$$F(R)(h\nu) = B(h\nu - E_g)^n$$

where *R* is the reflectance [%] in the UV/Vis spectra, *h* the Planck's constant, v the frequency of light,  $E_g$  the bandgap in eV, and *n*-the type of optical transition. That is, n = 2 for an indirect transition (plotted as  $[F(R) \cdot (hv)]^{1/2}$  vs. hv) and n = 1/2 for a direct transition (plotted as  $[F(R) \cdot (hv)]^2$  vs. hv). The intercepts of the abscissa (Fig. 3) demonstrates bandgap values of 4.40(1) eV and 4.50(1) eV for an indirect and



**Fig. 1** Crystal structure of  $K_2Pr_2O(BO_3)_2$ , showing polyhedral structural units (**a**) connectivity of  $Pr(1)O_8$  dodecahedra (**b**),  $Pr(2)_2O_{14}$  polyhedral dimer (**c**), and view of the structure of  $K_2Pr_2O(BO_3)_2$  along the *b*-axis (**d**)

direct transition, respectively. These bandgap values of  $K_2Pr_2O(BO_3)_2$  are smaller than those of 4.96 eV for  $\lambda$ -PrBO<sub>3</sub> [36] and 6.32 eV for Rb<sub>2</sub>LiLaB<sub>2</sub>O<sub>6</sub> [37]. Recently, the derivation of absorption spectrum fitting (DASF) method was proposed by Souri et al. [38] for thin films to calculate the bandgap energies without any presumption of the nature of the transition. Notably, the DASF method can also be expressed as follows proposed by Kirsch et al. [39, 40] for powder samples:

$$\frac{\mathrm{dInF(R)}}{\mathrm{d}h\nu} = \frac{\mathrm{n}}{h\nu - Eg}$$

The obtained bandgap of 4.49(1) eV using the DASF method is similar to the determined bandgap of 4.50(1) eV for a direct transition within the estimated

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### 3.3 FTIR and Raman spectra

The observed FTIR and Raman spectra along with the fitted compound and component models are shown in Fig. 4. Since the crystal structure of  $K_2Pr_2O(BO_3)_2$  adopts  $P2_1/c$  space group, factor group analysis predicts 156 vibrational modes at the zone center  $(39A_g + 39A_u + 39B_g + 39B_u)$ , where 75 modes  $(38A_u + 37B_u)$  are IR active, 78 modes  $(39A_g + 39B_g)$  are Raman active and 3 are acoustic modes  $(A_u + 2B_u)$ . To fit the observed IR spectrum, it requires 41 bands. The bands between 400 and 550 cm<sup>-1</sup> can be attributed to bending of Pr–O, which was explicitly characterized in other praseodymium oxides [41, 42] The bands



Fig. 2 X-ray powder data Rietveld plots of K<sub>2</sub>Pr<sub>2</sub>O(BO<sub>3</sub>)<sub>2</sub> and of the decomposition products as inset



**Fig. 3** Reflectance spectrum of K<sub>2</sub>Pr<sub>2</sub>O(BO<sub>3</sub>)<sub>2</sub> (top left), Tauc plots for indirect (bottom left) and direct (top right) optical transitions, and DASF plot (bottom right)

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Fig. 4 FTIR (left top) and Raman (left bottom) spectra of K<sub>2</sub>Pr<sub>2</sub>O(BO<sub>3</sub>)<sub>2</sub> at ambient condition along with fitted compound and component models. Temperature-dependent Raman spectra (right); temperature increases upward from 78 to 300 K

between 600 and 1600 cm<sup>-1</sup> owing to vibration of planar  $BO_3^{3-}$  groups, can be categorized into four different types [37, 43, 44]: the in-plane bending (v4; 550–700 cm<sup>-1</sup>), out-of-plane bending (v2; 740–780 cm<sup>-1</sup>) of BO<sub>3</sub>, B–O symmetric stretching (v1; ~903 cm<sup>-1</sup>) and B–O asymmetric stretching (v3; 1000 cm<sup>-1</sup> and 1500 cm<sup>-1</sup>). Clearly, the v2 and v3 modes have much stronger absorption than that of v3 and v1. Group analysis of an ideal planar BO<sub>3</sub> group possesses  $D_{3h}$  symmetry, where v2 and v3 are IR active, whereas the v1 is IR inactive. The clear appearance of v1 in the IR spectrum indicates that the BO<sub>3</sub> groups in K<sub>2</sub>Pr<sub>2</sub>O(BO<sub>3</sub>)<sub>2</sub> are distorted from an ideal symmetry.

The observed Raman spectrum of  $K_2Pr_2O(BO_3)_2$  at ambient condition could be fitted with 56 component peaks (Fig. 4). Several intense bands below 550 cm<sup>-1</sup> can be ascribed to the bending and stretching vibrations of K–O and Pr–O bonds as well as the lattice vibrations. The bands observed in the range of 600–700 cm<sup>-1</sup> and 700–800 cm<sup>-1</sup> correspond to the v4 and v2 modes, respectively. The most intense bands occur at 915 cm<sup>-1</sup> resulting from the v1 mode. The symmetric stretching mode (v1) of BO<sub>3</sub><sup>3–</sup> group is a strong Raman active vibration as known from other Pr<sup>3+</sup>-containing orthoborates such as  $\lambda$ -PrBO<sub>3</sub> [37, 43, 44] and KCaPr(BO<sub>3</sub>)<sub>2</sub> [45]. Above 1000 cm<sup>-1</sup>, one peak locating at 1050 cm<sup>-1</sup> and several border bands are found and can be ascribed to the v3 mode of BO<sub>3</sub><sup>3–</sup> groups. Of notes, the Raman spectrum also clearly confirms the vibrational features of BO<sub>3</sub> and PrO<sub>x</sub> groups in K<sub>2</sub>Pr<sub>2</sub>O(BO<sub>3</sub>)<sub>2</sub>. The temperature-dependent Raman spectra of K<sub>2</sub>Pr<sub>2</sub>O(BO<sub>3</sub>)<sub>2</sub> from 78 to 300 K (Fig. 4) show that the overall global quasi-harmonic change is not significant within the investigated low-temperature range. For instance, the intense band at 916.2(1) cm<sup>-1</sup> at 78 K shifts only to 914.6(1) cm<sup>-1</sup> at 300 K. Any phase transition driven by any optical soft-mode was not observed during the sample cooling from 300 to 78 K. Extrapolation of the frequency of this mode down to 0 K suggests that the compound K<sub>2</sub>Pr<sub>2</sub>O(BO<sub>3</sub>)<sub>2</sub> would be stable, a guideline for the phonon calculation using density functional theory calculation.

#### 3.4 Thermal analysis

For the bulk single-crystal growth of inorganic compounds, determination of the melting point or the decomposition temperature is indispensable. The thermal behavior of  $K_2Pr_2O(BO_3)_2$  was investigated by using simultaneous TGA and DSC methods. As shown in Fig. 5, the DSC curve demonstrates one sharp endothermic signal peak at 1318(1) K as well as one border and tiny peaks after 1400 K. The distinct endotherm in the range of 1273(3) K and 1330(3) K corresponds to melting or thermal decomposition. From the TG curve a weight-loss of 21.96(1)% is found to be at 1273(3) K. After the TGA /DSC experiment, X-ray powder data Rietveld refinement (inset Fig. 2)



Fig. 5 Thermogravimetry (TG) and differential scanning calorimetry (DSC) curves of K<sub>2</sub>Pr<sub>2</sub>O(BO<sub>3</sub>)<sub>2</sub>

demonstrates that the residual consists of  $Pr_{26}O_{27}(BO_3)_8$ and  $Pr_6O_{11}$  phases. It is worthwhile to note that we used  $Nd_{26}O_{27}(BO_3)_8$  [46] as the starting model and replaced Nd -atom with Pr-atom in the same Wyckoff position during the Rietveld refinement. For the obtained isotypic  $Pr_{26}O_{27}(BO_3)_8$  lattice parameters of a = 676.160(17) pm, b = 1269.56(4) pm, c = 1432.28(3) pm,  $a = 89.9979(17)^\circ$ ,  $\beta = 99.9008(17)^\circ$ ,  $\gamma = 89.9995(19)^\circ$  were calculated. From the distinct weight loss during the heating process one can safely assume that  $K_2Pr_2O(BO_3)_2$  decomposes into  $Pr_{26}O_{27}(BO_3)_8$ ,  $Pr_6O_{11}$  and potassium borates which eventually evaporates at the high-temperature regime. The TGA /DSC also confirms that  $K_2Pr_2O(BO_3)_2$  possess an incongruent melting point, suggesting that the flux method would be necessary for the growth of its bulk crystal.

### 4 Conclusion

The detailed structural, spectroscopic and thermal analysis reveal that the synthesized alkali metal praseodymium borate  $K_2Pr_2O(BO_3)_2$  belongs to the new member of the  $K_2La_2(BO_3)_2O$  family [25] providing also a new structure type. The crystal structure consists of 2D  $[Pr_2O(BO_3)_2]^{2-}$  sheets and K<sup>+</sup> cations in a layered

stacking along the *a*-axis. The greenish color stems from the electronic transitions from the ground state to various excited states within the 4f<sup>2</sup>-configuration rather than from the fundamental absorption edge that lies in the UV-region. Since Pr<sup>3+</sup> cation is of interest due to its photoluminescence property, K<sub>2</sub>Pr<sub>2</sub>O(BO<sub>3</sub>)<sub>2</sub> may be a prospective red phosphor under the radiation of blue light [15–17]. Density functional theory (DFT) calculation would be necessary to distinguish the observed Raman and infrared bands between phonon at the zone-center and photoluminescence as well as for a fuller assignment of the modes. However, the 4f-electrons of the rare-earth elements are over delocalized, sometimes leading to unrealistic/unphysical potentials and may provide inaccurate phonon calculations. Therefore, additional cares must be taken of in calculating the phonon spectra of the compound, which may be computationally very expensive. Given that  $K_2Pr_2O(BO_3)_2$  is an incongruent melting compound, the bulk crystals may be grown via high-temperature flux method, which would help elucidate possible anisotropic properties.

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### **Compliance with ethical standards**

**Conflict of interest** The authors declare that they have no conflict of interest.

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