Fast and memory efficient de-hazing technique for real-time computer vision applications



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Received: 16 October 2019 / Accepted: 12 February 2020 / Published online: 20 February 2020 © Springer Nature Switzerland AG 2020

Abstract

Some features of an image may spoil due to fog or haze, smoke. These images lose their brightness due to air-light scattering. It offers troublesomeness to the people lives in hill and fog regions of the world. This paper proposed two key aspects. One is a modified dark-channel method based on the median for eliminating the refine the transmission map as well as halos and artifacts, another important aspect is a memory-efficient row-based arrangement of the pixels for real-time applications. The advantage of this method is air-light can be predicted directly from the modified dark channel and also accurate transmission map can be estimated. This method is compared with other existing four algorithms. Our proposed method analyzed in terms of Peak Signal to Noise Ratio (PSNR), Average Time cost (ATC), percentage of haze improvement (PHI), average contrast of output image (ACOI), Mean Squared Error (MSE) and Structural Similarity Index (SSIM). The quality of the output de-haze image of our algorithm over existing algorithms is more. It has taken less computation time, equal MSE, with higher SSIM and has more percentage of haze improved over existing methods.

Keywords Real-time image/video de-hazing · Median filter · Blocked random access memory (BRAM) · Row based pixel arrangement · Dark channel prior · Guided filter

1 Introduction

Environmental conditions such as mist, haze, fog, and smoke lead to degrading the quality of the scenes when captured in the outdoor area. As it changes the colors of the original scene and reduces the contrast becomes an annoying problem to photographers, it declines the visibility of the pictures and acts as a threat to the several applications like object detection, outdoor surveillance; it also declines the clarity of the underwater images and satellite images. Hence, the removal of haze from images is a vital and widely required area in computer vision. The haze transmission depends on transmission depth and, varies in different situations. Hence, noticing and eliminating the fog from the digital images is an ill-posed problem. Several methods such as histogram-based [1], saturation based and contrast based are proposed day-by-day for adroitly removing haze from images. The above methods consider a single image as input for removing the haze. Depth based and polarization-based methods [2] can effectively eliminate fog by considering many hazy images taken from the dissimilar degree of polarization for finding the transmission-depth. Tan's [3] used a contrast maximization method; it gives a de-hazed image with better visibility and has more contrast than the hazy input image. The main disadvantage of this method is more assumptions are required to increase the local contrast of the patch of the restored image. He et al. [4] proposed a dark-channel method (DCM) with refined transmission depth using an edge-preserving filter called guided filter [5]. The detailed

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SN Applied Sciences (2020) 2:454 | https://doi.org/10.1007/s42452-020-2254-x

process of image de-hazing using [4] is explained in Sect. 2. Zhu et al. [6] proposed a de-haze algorithm with the help of a linear image model. They modeled the scene depth of the hazy image under the novel prior and learn the parameters of this model with a supervised learning method. The transmission-depth information is recovered well in this method. The main disadvantage of this method is the scattering coefficient (β) considered constant. The abovementioned algorithms may not suitable for real-time applications and require more computations as the square patch has been employed. To reduce the number of computations the median channel with row-based pixel structure is proposed in this paper. The row-based pixel arrangement provides an advantage of eliminating the halos and artifacts in the recovered haze-free image. The proposed algorithm involves the following steps: converting image to a row vector model, finding the atmospheric light using the median channel, estimation of transmission depth & scene radiance and lastly, row vector model to image conversion.

The rest of the paper arranged as follows. In Sect. 1, the Dark channel prior is explained. Section 2 discussed the proposed algorithm, Sect. 3, represents the experimental results and discussion, and Sect. 4 conclusion.

2 Dark channel prior method (DCM)

DCM is an effective method for de-hazing. The first step in the de-hazing algorithm is developing a mathematical representation for the hazy image model. The formation of hazy image is depicted in Fig. 1, because of the haze particle's scattering in the atmosphere; the image captured by the camera sensor looks foggy in nature.

An exact realization for a foggy image according to McCartney [7] is represented in Eq. (1).

$$I(p) = J(p)t(p) + A[1 - t(p)]$$
(1)

where J(p) is de-hazed image or scene radiance,I(p) is observed hazy image, t(p) is transmission depth or



Fig. 1 Haze formation model

SN Applied Sciences A SPRINGER NATURE journat transmission map and A is global air-light. The essential objective is, obtaining a haze-free image J(p). It is possible by identifying the unknown parameters t(p) and A.

Generally, the transmission map (t) is a function of two parameters and can be expressed as:

$$t = e^{-\beta d} \tag{2}$$

where β scattering coefficient is considered constant when atmospheric condition is homogenous in nature and is highly interrelated with wavelength. The depth of the scene *d* is ranges from $[0, +\infty)$. From Eq. (2) when *d* tends to infinity, the captured image is very far from the observer and at the same time *t* tends to zero, which means that there is no transmission map. This case is ambiguous in nature, another observation from Eq. (2) is that if *t* tends to infinity, no image exists i.e., image dehazing depends on transmission map.

A global air light (A) represent the amount of brightness needed for accurate visualization of output image (J). The atmospheric light for a single channel A^c can be calculated as the 0.1% of brightest pixels in the dark channel, corresponding pixels in a hazy image considered as atmospheric light. Sorting, division and comparison operations are involved in calculations. Therefore, the determination of unknown parameter A^c is a challenging problem. Moreover, refine transmission step is used to enhance the image quality and eliminates the halos, with the help of guided-filter.

Finding the scene radiance according to [4] from the Eq. (1) as

$$J(p) = A + \left(\frac{I(p) - A}{\max(t(p), t_0)}\right)$$
(3)

The significance of t_0 , when t(p) is close to zero then J(p) may affect with noise. Therefore, a restricted parameter $t_0 = 0.1$ is used and maintained as constant throughout the process.

The Fig. 2 represents DCM [4] based de-hazing system. This method works well for large patch sizes. Hence, the patch size of 16×16 is used to find the darkest pixel among three channels, followed by finding the atmospheric light and transmission map. A refine transmission map is obtained with the help of guided-filter, which produces filtered output based on guiding (input) image. It is specially designed to preserve & smoothening the edges and plays a vital role in the performance estimation process. Since it has a high average time cost. Therefore proposed approach is based on eliminating most computational complexity step of refining transmission.



Fig. 2 Process of DCM



Fig. 3 Halo effect



Fig. 4 RGB color space of hazy image model



3 Proposed algorithm

The existing methods [4] employed the minimum channel of the pixels as a dark channel of the image. As a result, it produces halos and artifacts in the de-hazed image. The effect of employing a minimum of pixels is represented in Fig. 3. At the edges, the white region becomes shaded resulting will lead to producing undesired pixel intensity which causes the halo effect.

This problem can be resolved in our proposed method as, in Fig. 4, the points on diagonal line in the RGB cube ranges from (0, 0, 0) to (255, 255, 255). Foggy areas (Brighten pixels) in an image are mostly scattered nearby this diagonal line, indicated with blue points in Fig. 4. Whereas object related pixels are surrounded nearer to the origin which are indicated with pink points. There is less special continuity. By determining variogram (V) [8] for each pixel of the hazy image, we can get the spatial continuity of an original image.

Generally, in sky regions, the value of 'V' is very small. However, in non-sky areas, 'V' is larger. To measure 'V', we used the concept of color fluctuations. According to the depth of field, bright objects will become dimmer as the distance increases. This phenomenon is more observable under the impact of thick haze. The pink points in

Fig. 5 Convolution operation on Sub-window of the frame (X) [18]

Fig. 4 shows, an object's color is unsteady at a distance. To stretch the value of "V" and make it more effective we employed the median of the pixels.

When observing transmission maps with different window sizes, we find a tip to eliminate the refine transmission step as well as halos and artifacts in the recovered image. It can be done by estimating the median channel of the pixels instead of a dark channel. Furthermore, note that in DCM produces a good de-hazed image with a patch size of 16×16. Therefore, in the proposed method, the median channel is determined with a 16×1 patch size.

Another key aspect with memory management for real-time image processing applications, i.e., memory is the major limiting factor in the field of image processing when wish to implement on FPGAs [9]. Convolution [10] is an important operation on an image and is performed in the spatial domain. Where each pixel and its neighbors are multiplied by kernel or patch, the results are summed up and the result is used to measure the new pixel value. The process is represented in Fig. 5.

For several reasons, among many image/video restoration algorithms we focused on this iterative algorithm. This exhibits a pattern of local computations due to the dependence of a restored pixel value on its 1-neighbors. These computations make it possible to implement spatially. The same process is repeated on a significant amount of data for a number of iterations. There have also been some difficulties related to this algorithm. The process is expected to be sequential, i.e. until the next iteration step can begin, all pixels of the image will move through the current restoration stage. This requires a fast and wider bandwidth.

Another key aspect proposed in this paper is about memory. To address this issue, assume that the 'X' image or frame will be stored as an array (A) of 8-bit elements. The 'A' array has columns and rows and is usually stored in BRAM [11] like a row by row or a column by column manner (*ixj*). Generally, the computer or processor does not keep track of each element of an array's address. Relatively,





Array-based pixel arrangement

it keeps track of address of the first pixel A(0,0) and is called the base address. It can use measure the specific pixel's address A(i, j).

$Loc[A(i,j)] = Base_adrs + (no.of_columns or rows * i) + j$ (4)

The moment of mask or patch in the image is varying from top to bottom as well as left to right end. In a particular row, when elements are finished, the mask moves one position right and down. Therefore, nine-pixel numbers (if patch size- 3×3) are involved during the convolution process at each step. Sequentially, it extracts nine pixels in each step. Because a single pixel's data is replicated, therefore this strategy is costly in terms of memory storage. Hence, a sequential pattern of pixels employed like a row vector manner. Most exceptional de-hazed output can be obtained by combing the above light of ideas. The process of proposed method as:

Initially, an image is converted to a row vector model. As a result, the square patch will be changed as rectangular. Figure 6 indicates the patch moment in existing and proposed algorithm respectively.

In the next step, the median [12] of the pixels is employed as a dark channel. Since the information of any image will hide in the middle of the image so, instead of finding the minimum of pixels in [4] we proposed the median. Median is nothing but middle value or average of the central values within the list. It is a non-linear signal processing technique based on statistics. The noisy value of any digital image or the sequence is replaced with its median value of the neighborhood (mask). Generally, noise elimination is employed at a pre-processing step to improve the outcomes in post-processing (ex:

Vector-based Pixel arrangement



Fig. 7 Architecture of proposed algorithm (input hazy image, array based arrangement, median of the pixels in each channel, Transmission map, atmospheric light estimation and de-hazed image from left to right)

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Fig. 8 Block diagram of proposed algorithm

Edge detection). The pixels within the mask are ranked in the order of their gray levels, and the median value of the group is stored to replace the noisy value. The median of the pixels can be obtained as

$$M(x,y) = med\{I(x-i,y), i \in W\}$$
(5)

where M(x, y), l(x, y) are output de-noise image and the original noisy image respectively, W is a single-dimensional mask. Sometimes the mask shape may be linear, circular, cross and square. In our method, we considered linear mask with size $W = 16 \times 1$. Then, Eq. (1) can be modified as

Step 1 Taking the median in the local patch in the hazy input image individually on each R, G&B channels from Eq. (1)

$$p \in \Omega(p) \left(I^{\mathsf{C}}(p) \right) = t(p) p \in \Omega(p) \left(J^{\mathsf{C}}(p) \right) + A^{\mathsf{C}}(1 - t(p))$$
(6)

Step 2 Applying normalization with air-light then Eq. (8) can be re-written as

$$p \stackrel{\text{median}}{\in} \Omega(p) \left(\frac{I^{c}(p)}{A^{c}} \right) = t(p) p \stackrel{\sim}{\in} \Omega(p) \left(\frac{J^{c}(p)}{A^{c}} \right) + (1 - t(p))$$
(7)

Step 3 Obtaining the minimum value of pixel from three RGB color channels as

$$\min_{c} \left(p \in \Omega(p) \left(\frac{I^{c}(p)}{A^{c}} \right) \right)$$
$$= t(p) \min_{c} \left(p \in \Omega(p) \left(\frac{J^{c}(p)}{A^{c}} \right) \right) + (1 - t(p))$$

We considered an assumption according to the DCM, minimum value of median of three color channels approximated to zero. This can be represented as

$$J^{dark}(p) = \min_{p \in \Omega(p)} \left(\underset{c \in \{r,g,b\}}{median} \left(J^{c}(p) \right) \right) \cong 0$$
(8)

Step 4 The patch transmission obtained as

$$\tilde{t}(p) = 1 - \min_{c} \left(\underset{p \in \Omega(p)}{median} \left(\frac{l^{c}(p)}{A^{c}} \right) \right)$$
(9)

The existence of haze is a basic indication for a human to identify depth. Even, if the pictures are captured in good weather conditions, the image will appear to be abnormal if the entire haze is removed and it seems to depth may be lost.

It can be defeated by adding a small quantity of fog $(\omega = 0.25)$, with the constant parameter $(0 \le \omega \le 1)$ in the above equation.

$$\tilde{t}(p) = 1 - w\min_{c} \left(median_{p \in \Omega(p)} \left(\frac{l^{c}(p)}{A^{c}} \right) \right)$$
(10)

Here the combining patch's transmission is equal to transmission depth of the entire image. Once, the transmission and air-light is known the scene radiance J(p) can be determined as

Step 5

$$J(p) = \left(\frac{I(p) - A}{\max(t(p), t_0)}\right) + A$$

The above whole process is done in the row vector model. At last, after finding the scene radiance for a row vector, it is reshaped into the matrix (image) form. The architecture of the proposed algorithm with array-based pixel arrangement and corresponding rectangular patch moment is represented in Fig. 7. To understand the variation of the image at each succeeding step, we demonstrated the architecture with images.

Figure 8, represents the block diagram and pseudo code of the proposed method is represented in algorithm 1. Initially, matrix-based pixel arrangement converted to the vector-based manner and then with a patch size of 16×1 the median of pixels is obtained. Later, atmospheric light, transmission map, and scene radiance are predicted according to Sect. 2. Finally, vector-based arrangement converted to a matrix-based manner for visualization purposes.

Table 1 Comparison of proposed algorithm with existing methods	Database	Method	PSNR in dB	ATC in Sec	ACOI	MSE	PHI	SSIM
	Play table	Zhu et al.	22.99	1.44128	0.0123	1.63	12.1976	0.7612
		Tarel et al.	22.99	2.885601	0.0123	1.63	10.3668	0.0482
		He et al.	22.99	2.038838	0.0123	1.63	7.4004	0.6813
		Tripathi et al.	21.76	1.628883	0.4578	2.35	25.5258	0.7423
		Proposed	23.95	1.597643	1.4617	1.98	29.5147	0.9882
	Canon	Zhu et al.	23.42	1.857462	0.1238	2.07	15.2154	0.6270
		Tarel et al.	23.42	1.258642	0.0341	2.07	14.3258	0.1042
		He et al.	23.42	1.647523	-0.0195	2.07	19.2158	0.6994
		Tripathi et al.	23.44	1.525874	0.6560	2.07	22.2174	0.8910
		Proposed	23.52	1.104532	1.7119	2.07	23.2587	0.9881
	Vintage	Zhu et al.	22.08	4.295092	0.0495	2.49	16.0677	0.7898
		Tarel et al.	0.765	1.750527	0.6080	2.49	48.5453	0.1320
		He et al.	22.05	1.987452	0.1857	2.54	16.5410	0.2365
		Tripathi et al.	25.18	1.841230	1.8547	2.49	11.2654	0.4163
		Proposed	25.92	1.325487	2.7458	2.49	18.9784	0.9955
	Motor Cycle	Zhu et al.	23.16	1.418704	0.0329	1.51	3.2373	0.6854
		Tarel et al.	23.16	1.906796	0.0341	1.51	6.6550	0.2098
		He et al.	23.16	2.029526	-0.0195	1.51	4.1131	0.4782
		Tripathi et al.	23.16	1.619069	0.1238	1.51	25.9353	0.5843
		Proposed	24.58	1.597488	2.1254	1.03	20.3847	0.9889
	Flowers	Zhu et al.	25.18	1.425781	0.0478	2.42	18.1245	0.8408
		Tarel et al.	25.18	1.754215	0.7584	1.59	18.4758	0.2579
		He et al.	25.18	1.914254	-0.2548	2.42	17.4789	0.8638
		Tripathi et al.	25.18	1.574123	0.9954	2.42	16.2587	0.6587
		Proposed	25.72	1.072587	1.8222	2.42	19.0012	0.9953
	Play Room	Zhu et al.	28.64	1.547842	0.1258	1.55	16.6764	0.7226
		Tarel et al.	28.67	2.754218	0.0258	1.55	7.6522	0.2093
		He et al.	28.67	2.147896	0.1458	1.55	13.1743	0.7910
		Tripathi et al.	28.67	1.785421	0.9985	1.55	18.9678	0.8425
		Proposed	28.52	1.058414	1.5285	1.55	23.6419	0.9893
	Toys	Zhu et al.	25.45	1.574562	0.017	1.29	11.1458	0.7239
		Tarel et al.	25.45	1.975125	0.0257	1.29	16.1249	0.1575
		He et al.	25.45	1.587452	-0.0265	1.29	18.1246	0.8480
		Tripathi et al.	25.45	1.254789	0.206	1.29	20.0128	0.5483
		Proposed	25.45	1.160618	1.4858	1.29	22.0196	0.9870
	Bicycle	Zhu et al.	22.08	1.472224	0.0382	2.49	16.3358	0.7719
		Tarel et al.	22.08	1.898116	0.1195	2.49	15.7125	0.2270
		He et al.	22.08	1.987793	0.0059	2.49	23.2702	0.7494
		Tripathi et al.	22.07	1.542246	0.608	2.49	28.5453	0.7675
		Proposed	22.58	1.452662	2.7532	2.19	29.2658	0.9928



Fig. 9 De-haze result of proposed method. **a** Hazy input image, **b** median channel of hazy image, **c** Transmission depth map, **d** De-haze output image

Algo	rithm 1: Pseudo code of proposed method					
1.	input im=imread(imgname)					
2.	2. for each channel of input im do					
3.	im_row=reshape of input_im					
4.	Initialize r_hmed as median of pixel					
5.	for i=1:number of pixels do					
6.	r_hmed=median(patch of im_row)					
7.	end for					
8.	Initialize air_light,temp_variable=0;					
9.	for i=0.1% of brightest pixels in r_hmed do					
10.	if (air_light <r_hmed&& max="" pixel="" r_hmed<="" th="" value="" within<=""></r_hmed&&>					
	the image)					
11.	temp_variable= r_hmed;					
12.	end if					
13.	end for					
14.	for each pixel of r_hmed do					
15.	air_light = air_light+temp_variable;					
16.	end for					
17.	atmospheric_light= average value of air_light					
18.	for each pixel of image do					
19.	nr_hmed=normalize original hazy image each channel with					
	atmospheric_light					
20.	end for					
21.	for i=1: number of pixels in r_hmed do					
22.	transmission = 255*(1 - (0.75.* nr_hmed));					
23.	end for					
24.	while (elements in r_hmed) do					
25.	radiance=atmospheric_light+(im_row-air_light)./max(transmission,t0);					
26.	end while					
27.	De-haze=radiance					
28.	Reshape row to matrix model					
29.	end for					

4 Experimental results and discussion

The simulations are performed in MATLAB 17a running on Intel i5 CPU 3 GHz and 8 GB memory with OS window 8.1. To verify the validity of our proposed algorithm, we choose a well-known standard database Middlebury [13]. This database covers all the challenging factors. Our proposed algorithm compared for an image size of 640×480 with a patch size 16×16. They are Zhu et al. [6], Tarel et al. [14], He et al. [4] and Tripathi et al. [15] in terms of MSE, PSNR, Average Time cost, Average Contrast of the output image and visibility analysis (percentage of haze improvement). From the comparison Table 1, the proposed approach taking minimum average time cost; produces output with high contrast and equal mean square error (MSE) i.e., for canon image the MSE is 2.07 similar for other methods and haze improvement of the proposed algorithm gives a significant result. In the motorcycle database, He et al. and Tripathi et al. produces halos and artifacts. Whereas, in the proposed method we employed the median of the pixels along with row-based patch moment, which performs well on removing artifacts and halos around the depth discontinuities. Zhu et al. produces contrast-enhanced output and they look unnatural. Tarel et al. produces natural de-hazed as an output but recovered image has noticeable haze. Proposed method has highest SSIM value among other state-of-the-art methods. These evaluations parameters are more trustworthy for analysis and the bold value in the Table 1 indicates the better evaluation metric value produced by the corresponding method.

An example of a bi-cycle image from a standard database chosen for illustration, Fig. 9a denotes a bi-cycle hazy image with a resolution of 800×600 and it's median, transmission depth and de-hazed output image represented in Fig. 9b–d respectively. Figure 10 shows the qualitative comparison of five state-of-the-art algorithms on different real-world images. The Figs. 11, 12, 13, 14 15, and 16 shows the results comparison with help of bar charts in terms of PSNR, ATC, ACOI, MSE, PHI and SSIM of different De-hazing algorithms respectively. Our algorithm gives less computational time for all standard databases. The percentage of haze improvement as well as SSIM is significantly high for all the databases.

4.1 Performance evaluation metrics

Evaluation metrics basically gives information about which scheme of method can be preferable. In this paper five performance metrics are used for evaluating the efficiency of proposed algorithm.

4.1.1 PSNR and MSE

PSNR [16] and MSE are well-identified performance metric for measuring the degree of error because these represent overall error content in the entire output image.

PSNR is defined as the "logarithmic ratio of peak signal energy (P) to the mean squared error (MSE) between output N_i and input M_i images". It can be expressed as



Fig. 10 Qualitative comparison of different Dehazing algorithms on Middlebury standard challenging database



Fig. 11 PSNR: Peak Signal to Noise Ratio

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Zhu et. al. Tarel et. al. He et. al. Tripathi et. al. Proposed

Fig. 12 ATC: Average Time Cost



■Zhu et. al. ■Tarel et. al. ■He et. al. ■Tripathi et. al. ■Proposed

Fig. 13 ACOI: Average Contrast of Output Image



Fig. 14 MSE: Mean Square Error

where, *P* is maximum value of the pixel in an image (typical value of P=255), *MSE* is Mean Squared Error, *k*, *n* are the no. of rows, no. of columns of the image respectively and M_i , N_j are the input image, output image respectively. Generally, the value of PSNR would be desirably high.



Zhu et. al. Tarel et. al. He et. al. Tripathi et. al. Proposed

Fig. 15 PHI: Percentage of Haze Improvement



Fig. 16 SSIM: Structural Similarity index

4.1.2 Computation time or average time cost

It represents the amount time needed to complete an algorithm in MATLAB. Using commands 'tic' &'toc', the computational time is calculated. The unit are in seconds.

The average time cost of our proposed algorithm is estimated with other four existing algorithms in 21 number of iteration.

4.1.3 Average contrast of de-hazed image

$$C = \frac{1}{MN} \left(\max \left(\frac{L_{\max} - L_{\min}}{L_{\max} + L_{\min}} \right) \right)$$

Here L_{min} , L_{max} is the minimum, maximum luminance of an output image correspondingly. *M*, *N* row and column of an output image respectively. Generally, the maximum value of it directs that an image is more quality.

4.1.4 Structural Similarity Index (SSIM) [17]

It is a method for quantifying the similarity between two images. The SSIM can be observed as a quality measure of one of the images being compared with the other image is regarded as of perfect quality.

5 Conclusion

Based on qualitative and quantitative metrics we concluded that the proposed approach took minimum computation time; produces output with high contrast and has almost equal mean squared error (MSE). The haze improvement of the proposed algorithm gives a better result than state-of-the-art methods.

Our method has a common limitation like all de-hazed algorithms: the haze imaging model is valid only for nonsky regions and it has another drawback of dealing with hazy images which are obtained at long distance, e.g. aerial images. In the future, we will focus on the above aspects.

Acknowledgements This work is supported by the Science and Engineering Research Board (SERB) India, under the Grant of EEQ/2016/000556.

Compliance with ethical standards

Conflict of interest The authors declare that they have no conflict of interest.

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