FULL PAPER



Flow field designs developed by comprehensive CFD model decrease system costs of vanadium redox-flow batteries

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Abstract

Different flow field designs are known for vanadium redox-flow batteries (VFB). The best possible design to fulfil a variety of target parameters depends on the boundary conditions. Starting from an exemplary interdigitated flow field design, its channel and land dimensions are varied to investigate the impact on pressure drop, channel volume, flow uniformity and limiting current density. To find a desirable compromise between these several partly contrary requirements, the total costs of the VFB system are evaluated in dependence of the flow field's dimensions. The total costs are composed of the electrolyte, production and component costs. For those, the production technique (injection moulding or milling), the pump and nominal power density as well as depth of discharge are determined. Finally, flow field designs are achieved, which lead to significantly reduced costs. The presented method is applicable for the design process of other flow fields and types of flow batteries.

Keywords Computational fluid dynamics · Redox-flow batteries · Flow field designs · Battery costs

Introduction

Redox-flow batteries (RFB) are a promising large scale energy storage technology [1]. Great advantages of RFBs are their independent scalability and energy as well as their intrinsic safety. Vanadium redox-flow batteries (VFB), which are available in the kW to MW range, have already been intensively studied [2–4]. Currently there is a special focus on the transferability of the results from lab to operational scale [5].

Highlights

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The VFB performance is affected by numerous influences. These include the used materials, the applied designs and the operational parameters of the VFB [6]. The additional insertion of flow fields at the cell level in the bipolar plate or the electrode allows to reduce pressure losses and to improve flow characteristics. For VFB mainly serpentine and interdigitated flow field designs (IFF) were applied by experimental and simulation based studies. Thereby, typically the distance between the channels, called land width, is as large as the channel width or twice as large as it [7]. Depending on the flow field design, stagnation zones can be reduced, local mass transport is increased and a more uniform distribution of electrolyte flow, current density and potential is accessible [7–9]. For large cell sizes it was shown that in particular IFF designs lead to a reduced pump power and a high uniformity in comparison to serpentine design [8]. A hierarchically structured IFF is characterized by its additional secondary branches. In comparison to an IFF with only primary branches, those structures can encourage a further reduction of the required pump power and an improvement of the voltage efficiency [10]. Another investigated possibility is the introduction of ramps within the IFF channels, which lead to lower pressure differences, too [11]. Nevertheless, it has to be emphasised that the best flow field structure depends strongly on the boundary conditions such as electrode and electrolyte properties as well as the operational parameters [12]. Therefore, efficient flow

[•] Half-cell model of vanadium redox-flow battery consisting of interdigitated flow field and electrode

[•] Flow field design study with varied geometric flow field parameters by computational fluid dynamics simulations

Pressure drop, flow distribution, mass transport and total costs as target
parameters

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field designs have to be adjusted to these boundary conditions. For instance the observation of the pumping-corrected voltage efficiency in dependence of the channel and land dimensions as well as the flow rate allows to find favourable flow field designs [9]. Furthermore, it was shown that also topological approaches can be used for the optimisation of flow field designs [13]. By means of optimisation, the local electrode porosity was adjusted, since this also allows to improve the flow uniformity and efficiency of VFB [14]. Thereby, the aim is to adapt the properties of the electrode even better to the conditions in the RFB [15]. In this context other approaches are for instance, the variation of the electrode porosity [16] and the development of electrodes, which are structured at the micron- as well as the nano-scale [17].

Computational fluid dynamics (CFD) simulations are applicable for optimisation studies [18]. It is possible to describe the VFB's electrode in CFD models fibre dissolved or as porous media. The electrode structure and the associated material properties depend strongly on the electrode material and characteristics. By optical measurements it was shown that for instance in a carbon felt electrode, the flow distribution is not completely homogeneous [19]. For the description of the permeability of the electrode, either experimental data in dependence of the electrode's compression rate or model-based approaches can be applied [20]. The transport phenomena in RFB are assessable by the application of correlation equations for the mass transfer coefficient. Several correlation equations exist for fibrous carbon electrodes, which differ in the resulting order of magnitude for the mass transfer coefficient [21, 22].

In this study, a cell design with an IFF in the industrial scale with an active area of around 0.06 m^2 is investigated. The relations between the flow field parameters and the VFB's system parameters are presented for all channel dimensions in the observed parameter range. The considered system variables are the pressure drop, the volume of the flow field channels, the uniformity of the velocity in the electrode and the limiting current density. Subsequently, the obtained results are transferred to the system costs of the VFB. Based on the observed parameter range for the set boundary conditions, most beneficial dimensions of IFF designs are outlined.

Methods

The general setup of a VFB cell is sketched in Fig. 1. The shown main components of the VFB are the monopolar respective bipolar plates, the electrodes and the membrane as well as the electrolyte inlet and outlet for the negative (V^{2+} and V^{3+}) and the positive electrolyte (VO^{2+} and VO_2^+ , which are named by their oxidation numbers V^{4+} and V^{5+} in the following). In a VFB system, which is defined by its nominal power and capacity, several cells are combined to a stack. The electrolyte, which is stored in the tanks, is pumped during the operation through the stack respectively cells. To evaluate the performance of the VFB system, the achievable nominal power density and depth of discharge are characteristic values as well as its coulomb and energy efficiency. The results are obtained by a CFD model, which describes one VFB half cell.

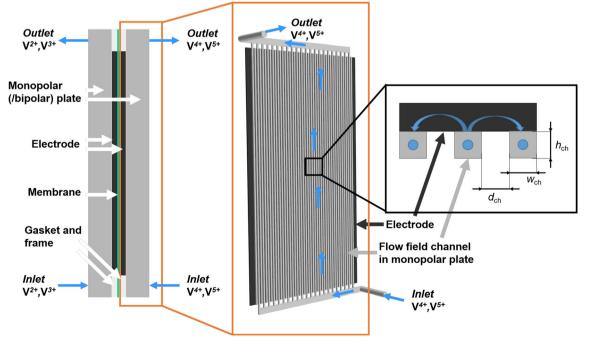


Fig. 1 VFB setup consisting of the monopolar respectively bipolar plate, the electrodes and the membrane with a closer look at the positive half cell, which is described with the CFD model

CFD model

In the model, the half cell consists of the electrode region and the flow field region. The flow field region is composed of the supply channels and the flown through channels of an IFF design. Concerning the kinetics, the reaction rate of the positive electrolyte (PE) is higher than the one of the negative electrolyte [23]. Therefore, mass transport limitation, which can be reduced by improved flow field designs, have a larger impact on the PE side. In the following, the half cell of the PE is examined.

In this study different flow field designs for VFB are evaluated. Out of the requirements, which have to be met by flow field designs, the effect of the variation of the flow field channel and land dimensions on the four major demands of Table 1 is analysed. Those are called system parameters.

Model setup and mesh

For this study, the model is set up in the commercial engineering software package Simcenter STAR-CCM+ Version 15.06.007-R8 from Siemens Digital Industries Software. For the CFD model, the fluid volume is generated as CAD designs, which geometries are sketched within the software. For all investigated designs, the inlet and outlet position as well as geometric dimensions of the electrode are fixed. The geometric input parameters of this study are the channel width w_{ch} and height h_{ch} as well as the land width d_{ch} , see the right side of Fig. 1 and Table 2. The pressure drop is supposed to be below 0.5 bar, which is necessary to avoid pressure equipment directive (PED) restrictions. Thereby, all designs with a pressure drop above this level are marked.

Additionally, design parameters are formulated in dependence of the input parameters. Those design parameters for the geometry sketch are the total number of channels, the length and the depth of the supply channels and the position of the first channel along the supply channel, see Fig. 2. Furthermore, electrode areas are considered, in which no channels are allowed to be placed during the variation of the channel and land dimensions. This is done to avoid that the electrode might dent into the channels at the electrode outer edges.

For the CFD model, a conformal polyhedral part-based mesh with three prism layers is generated, for which also the surface remesher, automatic surface repair and volume mesher are used within Simcenter STAR-CCM+. The settings of the mesh include several characteristic values, which are partly dependent on the definition of the base size in Simcenter STAR-CCM+, which is set to 0.75 mm. For instance, the surface edge length is defined generally by the target surface size of 50% relative to the value of the base size. Additionally, the minimum surface size of 20% of the base size is included. The total number of computational cells for the exemplary design is approx. 10 million. For this design, the extrapolated relative error (ERE) is estimated by Richardson extrapolation for the pressure drop, the velocity uniformity and the limiting current density after [24], see the Appendix for further information. The deviation of the results for the chosen mesh in comparison to an assumed mesh with an infinite small mesh size is very small respectively negligibly small (ERE_p = 3.3%; $\text{ERE}_{\psi} = 0.1\%$ and $\text{ERE}_{iL} = 0.2\%$). Furthermore, the differences between the simulation results for the different flow field designs in the observed parameter range are to a large extent significantly higher than the estimated error due to the mesh, see Results and Discussion section. Therefore, as the selected mesh parameters lead to reasonable mesh calculation times and simulation results, they are kept constant throughout this design study. Still, this leaves some potential for adjustments in the future, as even further adaption of the mesh settings to the geometric parameters of each design might be beneficial. We have observed that mostly less than 300 iterations are sufficient to monitor no significant changes of the pressure drop between cell inlet and outlet and the average velocity at the outlet between the iterations. Yet, to guarantee a completely converged solution for all possible designs, we set the stopping criteria to 600 iterations and monitored the pressure drop and average velocity, respectively.

Governing equations

The model is three dimensional, steady-state with turbulent, incompressible flow. The continuity equation for the fluid flow is given in Eq. (1) with the physical velocity vector **v**. Furthermore, the momentum equation of the fluid flow is

 Table 1
 System parameter and their purpose for the flow field designing process

System parameter	Purpose
Low pressure drop between cell in- and outlet	Reducing operational costs and avoiding the need of application of PED
Low volume of the flow field channels	Enabling a short and cheap production
High flow uniformity	Reducing losses of active membrane area
High limiting current density	Improving mass transport and thereby to reduce overpotentials

Table 2Input parameters andtheir explained values

Input parameter	Value	Explanation
Channel width	Minimum: 1 mm Maximum: 5 mm	> Electrode might dent due to wider channels
	Step size: 1 mm	
Channel height	Minimum: 1 mm Maximum: 3 mm	> Limited by thickness of the bipolar plates
	Step size: 1 mm	
Land width	Minimum: 2 mm Maximum: 50 mm	➢ Pressure drop gets too large
	Step size: 4 mm	

shown in Eq. (2) including the stress tensor T. The electrode is defined by the porous media model. For the fluid flow through the porous media, the continuity equation is given in Eq. (3). In the momentum equation with the pressure p and the stress tensor T of Eq. (4), the tensor for the porous viscous resistance \mathbf{P}_{v} and the porous inertial resistance \mathbf{P}_{i} are included. The vector of the superficial velocity \mathbf{v}_s results from the porosity ε and the physical velocity v (Eq. (5)). The electrode's permeability K is included by Eq. (6) in the porous viscous resistance \mathbf{P}_{v} and by the Forchheimer constant $\beta_{\rm F}$ of Eq. (7) in the porous inertial resistance P_i . Thereby, the Forchheimer constant is defined in Eq. (8) in dependence of the electrode's tortuosity τ and porosity ε (Eqs. (9) and (10)), after [25, 26]. Additionally, they change in dependence of the state of charge (SoC). The SoC dependence of the density ρ_{PE} is given by Eq. (11) and the dynamic viscosity $\mu_{\rm PE}$ in Eq. (12) after [21]. For

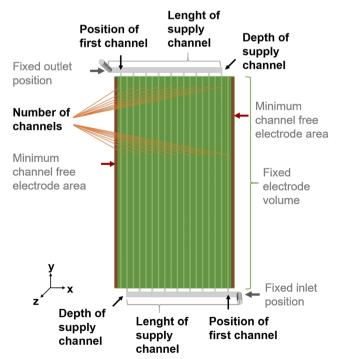


Fig. 2 Geometry setup with fixed and flow field dependent design parameters

the mo-del, a one electrode layer design with a compressed carbon felt electrode is chosen. Its material data such as its porosity ε and permeability *K* correspond to the characteristics of a SGL Sigracell® GFD 2.5 EA carbon felt electrode (SGL Group, Germany) with a compression rate of 20%, see Table 3.

$$\nabla \cdot (\rho_{\rm PE} \mathbf{v}) = 0 \tag{1}$$

$$\nabla \cdot (\rho_{\rm PE} \mathbf{v} \mathbf{v}) = \nabla \mathbf{T} \tag{2}$$

$$\nabla \cdot (\varepsilon \rho_{\rm PE} \mathbf{v}) = 0 \tag{3}$$

$$\nabla \cdot (\varepsilon \rho_{\rm PE} \mathbf{v} \mathbf{v}) = -\varepsilon \nabla p - \nabla \cdot (\varepsilon \mathbf{T}) - \varepsilon \mathbf{P}_{\rm v} \mathbf{v}_s - \varepsilon \mathbf{P}_{\rm i} |\mathbf{v}_s| \mathbf{v}_s \tag{4}$$

$$\mathbf{v}_s = \varepsilon \mathbf{v}$$
 (5)

$$\mathbf{P}_{\mathbf{v}} = \frac{\mu_{\mathrm{PE}}}{K} \tag{6}$$

$$\mathbf{P}_{\mathbf{i}} = \varepsilon \rho_{\mathrm{PE}} \beta_{\mathrm{F}} \tag{7}$$

$$\beta_{\rm F} = 2,88 \cdot 10^{-6} \frac{\tau}{\varepsilon K} \tag{8}$$

$$\tau = \frac{1}{\varepsilon^{1/2}} \tag{9}$$

$$\varepsilon = 1 - \frac{1 - \varepsilon_0}{V_{\rm C}/V_0} \tag{10}$$

$$\rho_{\rm PE}(\rm SoC) = (1330 + 20 \cdot \rm SoC) \frac{kg}{m^3} \tag{11}$$

$$\mu_{\rm PE}(\rm SoC) = (4.53-0.76 \cdot SoC) \, mPa \, s \tag{12}$$

The fluid is defined as a multi-component liquid. Its mass fractions are corresponding to the vanadium electrolyte solution, which consists of the vanadium species, water, sulphate and others including phosphoric acid and further additives, from GfE (Gesellschaft für Elektrometallurgie mbH, Germany) after [27]. The total molar vanadium concentration is around 1.6 kmol/m³ with 4 kmol/m³ sulphate. At the velocity inlet, the SoC and the velocity are specified. Generally, mass transport limitations occur for charging at a high SoC. Nevertheless, for this CFD model a quite low value of 20% for

the SoC is chosen, as this allows to observe the effect of the flow field design on the local vanadium concentration. The distribution of the vanadium concentration thereby depends on the selected mass transport correlation, which is explained further on. Assuming an average current density of 200 mA/ cm² and a concentration gradient of 10% between cell inlet and cell outlet, the inlet velocity is calculated by applying Faraday's law. The cell outlet is set as pressure outlet with atmospheric pressure. In this study, the case of charging is investigated in the CFD model. In Eq. (13), the species transport in the electrode includes for the mass fraction Y_i the effect of the diffusion and the source term S_{Y_i} , which is given in Eq. (16). The mass fraction Y_i results from the molar concentration c_i of the species *i* (Eq. (14)). The source term S of the vanadium species is defined after [28] and is adjusted for this model by the molecular weight W_i (Eq. (15)). Furthermore, the definition of the species source term follows the assumption of [29]. According to the explanations given there, the application of the volumetric limiting current density i_{lim} allows to evaluate the electrolyte's availability under mass transport limitation (Eq. (17)). The limiting current density depends on the mass transfer coefficient $k_{\rm m}$, which is determined by the mass transport correlation equation (Eq. (18)). Within this study, the correlation equations after [21] is applied (Eq. (19)).

$$\nabla \cdot \left(\rho_{\rm PE} \mathbf{v} Y_i\right) = \nabla \cdot \left[\frac{\varepsilon}{\tau} \rho D_i \nabla Y_i + \frac{\mu_t}{\sigma_t} \nabla Y_i\right] + S_{Y_i} \tag{13}$$

$$Y_i = \frac{c_i \cdot W_i}{\rho_m} \tag{14}$$

$$S_{Y_i} = S \cdot W_i \tag{15}$$

$$S = -a \cdot k_{\rm m} \cdot c_{\rm V} \tag{16}$$

$$i_{\rm lim} = z \cdot a \cdot k_{\rm m} \cdot c_{\rm V} \cdot F \tag{17}$$

$$Sh = k_{\rm m} \cdot \frac{d_{\rm f}}{D_i} \tag{18}$$

$$Sh = 0.07 \ Re^{0.66} Sc^{0.45} \tag{19}$$

The flow distribution in the electrode volume is evaluated by the uniformity index Ψ_{uni} of Eq. (20), which is defined within the software package Simcenter STAR-CCM+ after [30, 31]. For the calculation of the uniformity index Ψ_{uni} , the local velocity magnitude v_c is compared to the overall volume average of the velocity magnitude \overline{v} under consideration of the cell volume $V_{\rm c}$.

$$\psi_{\rm uni} = 1 - \frac{\sum_{\rm c} \left| v_{\rm c} - \overline{v} \right| V_{\rm c}}{2 \left| \overline{v} \right| \sum_{\rm c} V_{\rm c}}$$
(20)

Cost model

Based on the previously described CFD model, the total costs are estimated for a VFB system in the MW-range. The system's characteristic values for the nominal power P_N and nominal capacity Q_N are given in Table 4. The beforehand named four requirements are taken into account in the estimation of the total costs as follows:

- Low pressure drop \rightarrow low pumping power
- Low volume of flow field channels → low specific production costs
- High flow uniformity → high nominal power density and high depth of discharge (DoD)
- High limiting current density → high nominal power density and high DoD

VFB system costs

The resulting interrelations are explained further on in detail. The introduced total costs of the VFB system include the costs for the electrolyte $C_{\text{electrolyte}}$ as well as the specific costs for the cell respectively stack components $c_{\rm comp}$ and for the production c_{prod} (Eq. (21)). The costs of the electrolyte $C_{\text{electrolyte}}$ depend on the given nominal capacity $Q_{\rm N}$ and an additional operational term to cover the needed pump power P_{Pump} . Moreover, the electrolyte costs $C_{\text{electrolyte}}$ are determined by the DoD and the specific electrolyte costs $c_{\text{electrolyte}}$, which are assumed to be 102 \in /kWh after [34, 35], see Eqs. (22) and (23). The needed pump power P_{Pump} results from the beforehand observed pressure drop Δp between cell inlet and cell outlet. Furthermore, it depends on the pump efficiency η_{Pump} , the total number of cells n_c and the volume flow rate, which is defined by the velocity at the cell inlet v_{in} and the inlet area A_{in} . As the pressure drop has to be overcome for both half cells, for

Table 3 N	Aodel constants	for fluid	and electrode
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Parameter	Name	Value	Unit	Reference
$ \begin{array}{c} \overline{v_{\text{in}}} \\ d_{\text{f}} \\ a \\ K \\ \varepsilon_{\theta} \\ D_{\text{V}}^{4+} \end{array} $	Velocity magnitude at the inlet Carbon felt fibre diameter Specific surface area Permeability Open porosity V ⁴⁺ diffusion coefficient	$\begin{array}{c} 0.162 \\ 10 \\ 60,000 \\ 1\cdot 10^{-10} \\ 0.94 \\ 1.6\cdot 10^{-10} \end{array}$	$\begin{array}{c} m/s \\ \mu m \\ m^2/m^3 \\ m^2 \\ - \\ m^2/s \end{array}$	Chosen [32] Estimated Estimated [33] [21]

reasons of simplicity the factor 2 is included in Eq. (24). Still, this assumption neglects the fact that the pressure drop differs depending on the half cell due to the electrolyte's properties. The cell area is equal to the electrode area $A_{\text{electrode}}$ and therefore, the relation between the total number of cells n_c and the total area of all cells A_{total} is given by Eq. (25). In this context, the total area A_{total} is not only defined by the ratio of set nominal power P_{N} to the nominal power density p_{N} , but again an additional term is included in Eq. (25) to consider the needed pump power P_{Pump} .

$$C_{\text{total}} = C_{\text{electrolyte}} + \left(c_{\text{comp}} + c_{\text{prod}}\right) \cdot A_{\text{total}}$$
(21)

$$C_{\text{electrolyte}} = c_{\text{electrolyte}} \cdot \frac{Q'}{\text{DoD}}$$
(22)

$$Q' = Q_{\rm N} \cdot \left(1 + \frac{P_{\rm Pump}}{P_{\rm N}}\right) \tag{23}$$

$$P_{\text{Pump}} = \Delta p \cdot \eta_{\text{pump}} \cdot n_{\text{c}} \cdot v_{\text{in}} \cdot A_{\text{in}} \cdot 2$$
(24)

$$A_{\text{total}} = A_{\text{electrode}} \cdot n_{\text{c}} = \frac{P_{\text{N}} + P_{\text{Pump}}}{p_{\text{N}}}$$
(25)

Nominal power and depth of discharge

The nominal power density p_N as well as the DoD are linked to the limiting current density $i_{\text{lim, 20\%}}$ and the uniformity index ψ_{uni} . The listed three calculation parts are needed to gain the nominal power density and the DoD from the limiting current density and the uniformity index.

Part I: Description of charge/discharge behaviour based on limiting current density and uniformity index

Table 4 Model constants for the VFB cell and system

Parameter	Name	Value	Unit
$A_{\rm in}$	Area of the inlet	0.5027	cm ²
η_{pump}	Pump efficiency	80	%
V _{feed,EM}	Feed rate EM	2	m/min
$c_{\rm EM}$	Specific machine costs for EM	100	€/h
$C_{\text{wear,EM}}$	Specific costs for cutter wear	0.1	€/m
$P_{\rm N}$	Nominal power	1	MW
$Q_{\rm N}$	Nominal capacity	6	MWh
R_0	Specific cell resistance	1	$\Omega \mathrm{cm}^2$
E_0	Equilibrium voltage	1.42	V
U_{\min}	Minimum voltage	0.9	V
$U_{\rm max}$	Maximum voltage	1.65	V
$\eta_{\rm CE}$	Coulomb efficiency	95	%
$\eta_{\rm EE}$	Energy efficiency	80	%

Part II: Calculation of discharge voltage for a set voltage efficiency

Part III: Identification and calculation of the nominal power density and DoD by using the discharge voltage from *part II* to find the corresponding discharge voltage in the results of *part I*

For *part I*, the dependences for charging and discharging between cell voltage U_{cell} , current *i* and power density *p* are calculated for a SoC of 50%. The limiting current density *i*-lim,20% from the CFD simulations is transferred to the desired limiting current density i_{lim} for a SoC of 50% by Eqs. (26) and (27). Based on this adjusted limiting current density, the cell voltage U_{cell} is calculated after Eq. (28) for charging and after Eq. (29) for discharging in dependence of the open circuit voltage U_{OCV} . Thereby, the dependence of the open circuit voltage U_{OCV} on the SoC is given in Eq. (30). Furthermore, Eqs. (28) and (29) include the overpotentials due to ohmic losses by the specific cell resistance R_0 and due to mass transport limitations. From the cell voltage U_{cell} and the current density *i*, the power density *p* for charging and discharging results according to Eqs. (31) and (32).

$$i_{\text{lim,ch.}} = -i_{\text{lim,20\%}} \cdot \frac{1 - \text{SoC}}{(100\% - 20\%)}$$
 (26)

$$i_{\text{lim,dis.}} = i_{\text{lim,20\%}} \cdot \frac{\text{SoC}}{(100\% - 20\%)}$$
 (27)

$$U_{\text{cell,ch.}} = U_{\text{OCV}} - i_{\text{ch.}} \frac{R_0}{\psi_{\text{uni},\nu}} + 2\frac{RT}{F} ln \left(\frac{-i_{\text{lim,ch.}}}{i_{\text{ch.}} - i_{\text{lim,ch.}}}\right)$$
(28)

$$U_{\text{cell,dis.}} = U_{\text{OCV}} - i_{\text{dis.}} \frac{R_0}{\psi_{\text{uni},\nu}} + 2\frac{RT}{F} ln\left(\frac{i_{\text{lim,dis.}} - i_{\text{dis.}}}{i_{\text{lim,dis.}}}\right)$$
(29)

$$U_{\rm OCV} = U_0 + \frac{RT}{F} \ln\left(\frac{\rm SoC^2}{\left(1 - \rm SoC\right)^2}\right)$$
(30)

$$p_{\rm ch.} = U_{\rm cell, ch.} \cdot i_{\rm ch.} \tag{31}$$

$$p_{\rm dis.} = U_{\rm cell, dis.} \cdot i_{\rm dis.} \tag{32}$$

In *part II*, the voltage efficiency η_{VE} arises from the energy efficiency η_{EE} and coulomb efficiency η_{CE} (Eq. (33)), see Table 4. Assuming that the voltage efficiency is equal for charging and discharging, the cell voltage for discharging $U_{cell,dis.}$ is determined by Eq. (34). For the estimation of a reasonable operation, the SoC is again set to 50%, in contrast to the SoC of 20% at the inlet in the CFD model.

$$\eta_{\rm VE} = \frac{\eta_{\rm EE}}{\eta_{\rm CE}} \tag{33}$$

$$U_{\text{cell,dis.}} = U_{\text{OCV}} \cdot \sqrt{\eta_{\text{VE}}} \tag{34}$$

In *part III*, the calculated discharge cell voltage $U_{cell,dis.}$ of *part II* is used to search for a similar cell voltage U_{cell} in *part I*.

For this cell voltage U_{cell} , the corresponding discharge power density $p_{dis.}$ is selected out of the investigated values of *part I*. Assuming an equal discharge and charge power density, the associated cell voltage for charging is identifiable as well. The wanted nominal power density p_N results from the average value of the determined discharge power density $p_{dis.}$ and charge power density $p_{ch.}$ (Eq. (35)). The minimum limiting current density $i_{lim,dis.,min}$ and maximum limiting current density $i_{lim,dis.,min}$ and maximum limiting current density $a_{dis.}$ and the set minimum voltage U_{min} and the maximum voltage U_{max} (Eqs. (36) and (37)). The voltage limits are given in Table 4. Finally, the searched DoD is determined from the minimum and the maximum SoC after Eq. (38). Thereby, the values for the SoC are calculated after Eqs. (39) and (40).

$$p_{\rm N} = \frac{p_{\rm dis.} + p_{\rm ch.}}{2} \tag{35}$$

$$i_{\rm lim,dis.,min} = \frac{p_{\rm N}}{U_{\rm min}} \tag{36}$$

$$i_{\rm lim,dis.,min} = \frac{p_{\rm N}}{U_{\rm min}} \tag{37}$$

$$DoD = SoC_{max} - SoC_{min}$$
(38)

$$SoC_{min} = \frac{i_{lim,dis,min}}{i_{lim,20\%}} \cdot (100\% - 20\%)$$
(39)

$$SoC_{max} = 100\% - \frac{l_{lim,dis,max}}{i_{lim,20\%}} \cdot (100\% - 20\%)$$
(40)

Component and production costs

Coming back to the explained total costs C_{total} , the specific component costs c_{comp} are also part of Eq. (21). They include

the average specific costs for the membrane (300 €/m^2), the bipolar plate (100 \notin /m²) and the electrode (53 \notin /m²) [34]. Since for each cell, two electrodes are needed, the specific component costs c_{comp} are in total 506 ϵ/m^2 . Finally, the specific production costs c_{prod} are taken into account in Eq. (21) to consider the financial effort, which is needed to produce the desired flow field design. The specific production costs $c_{\rm prod}$ depend strongly on the observed flow field production technique. In this context, only those production costs are taken into account, which arise from changing the plane bipolar plate surface into a surface with a flow field design. Thereby, further costs of the production such as the investment costs of the different processes are neglected. In the following, the production techniques injection moulding (IM) and end milling (EM) are investigated. In general, the beforehand observed channel volume gives a first reference on the expectable specific production costs.

For the production of the flow field design via IM, it is assumed that the variation of the input parameters does not affect the specific costs. Therefore, the specific production costs for IM $c_{\text{prod,IM}}$ amount zero. This can be explained by the fact that the flow field is directly inserted in the plate during the IM process and only minimal further processing steps are needed to complete the insertion of the flow field's structure.

In comparison, EM is a production technique, which is used for the insertion of flow field designs after the fabrication of plane plates. The expenses for machine time have to be considered by the production time t_{prod} , which includes again the factor 2 to consider both half cells. The chosen feed rate for EM $v_{\text{feed},\text{EM}}$ is given in Table 4. Furthermore, a machine cost factor c_{EM} as well as cutter wear is taken by the cost factor c_{wear} the is taken into account (Eq. (41)). As it is expected that for EM a single cutter is used, the production time for EM

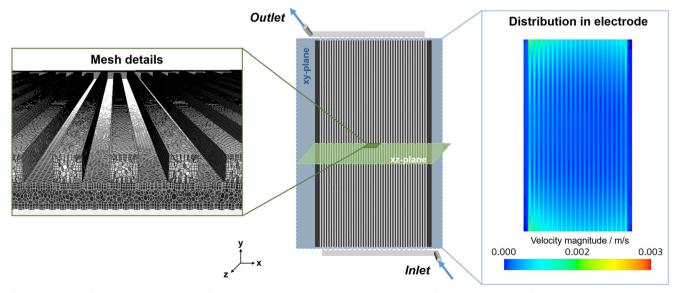


Fig. 3 Mesh details and velocity distribution for an exemplary IFF design, which was picked out of the resulting designs from the variation of the channel and land dimensions

 $t_{\text{prod,EM}}$ depends on the length of all channels. Additionally, the channel height h_{ch} is considered in Eq. (43). It is assumed that for an acceptable production quality, the cutter has to pass more often through deep channels than through flat ones. For EM, first a step for roughing and thereafter a step of finishing is needed. Therefore, a factor of 2 is implemented in Eq. (43).

$$C_{\text{prod,EM}} = c_{\text{EM}} \cdot t_{\text{prod,EM}} + l_{\text{prod,EM}} \cdot c_{\text{wear,M}}$$
(41)

$$t_{\text{prod,EM}} = 2 \cdot \left[\frac{l_{\text{prod,EM}}}{\nu_{\text{feed,EM}}} \right]$$
(42)

$$l_{\text{prod,EM}} = \frac{n_{\text{ch}}}{0.0005 \,\text{m}} \cdot (2 \cdot n_{\text{ch}} \cdot l_{\text{ch}}) \cdot 2 \tag{43}$$

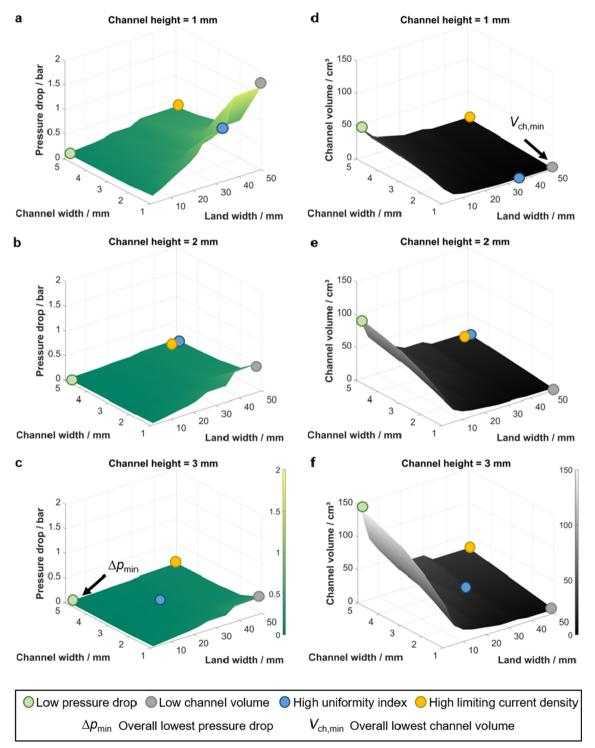


Fig. 4 Pressure drop (a-c) and channel volume (d-f) in dependence of the channel height and width as well as land width. Highlights are set on the specifications for the best design regarding the observed system parameter

Results and discussion

The CFD-based results of this study are presented as follows. First, the results of an exemplary IFF design are explained. Subsequently, the simulation results for four observed system parameters, which are the pressure drop, the volume of the flow field channels, the uniformity index and the limiting current density, are illustrated for different land and channel width as well as channel height. Further, the designs, which lead to the desired value of each system parameter, are analysed in detail. Thereafter, the results of the pump and nominal power density are visualized in dependence of the channel dimensions. These

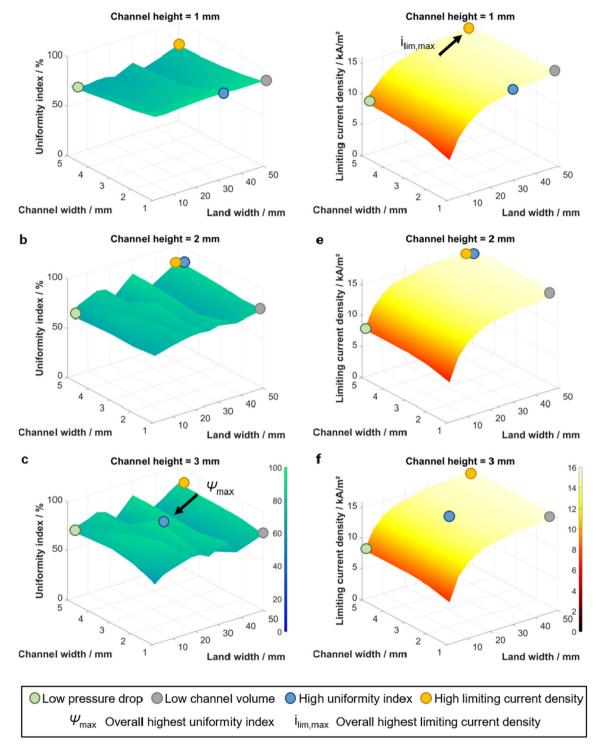


Fig. 5 Uniformity index (a-c) and limiting current density (d-f) in dependence of the channel and land width with highlights on the specifications for the best design regarding the observed system parameter

are included in the estimation of the electrolyte, component and total costs. The dependence of the total costs on the flow field production method as well as the channel dimensions are presented with a focus on the designs, which have the lowest total costs. Finally, the dimensions of the flow field designs, which fulfil best the beforehand observed system parameters or have the lowest total costs, are compared with each other.

CFD simulation results at cell level

The variation of the land and channel width as well as channel height of an IFF design allows to analyse the results for the whole parameter range of the observed flow field dimensions. From this parameter range, the flow characteristics of the modelled VFB half-cell are explained on the example of the IFF design, which is depicted in Fig. 3. Its channel and land dimensions are equal ($w_{ch} = 2 \text{ mm}$, $h_{ch} = 2 \text{ mm}$, $d_{ch} = 2 \text{ mm}$) and are part of the observed parameter range, which is given in Table 2 of the methods section. For this geometry, the equations of the CFD model are solved on the shown conformal mesh, see Fig. 1. For the illustrated design, the uniformity index of the velocity magnitude in the electrode volume amounts to 65%. The distribution of the velocity magnitude in the electrode depends on the distance between the channels of the flow field, which is for instance visible in a plane through the electrode centre, see Fig. 3. The shown velocity

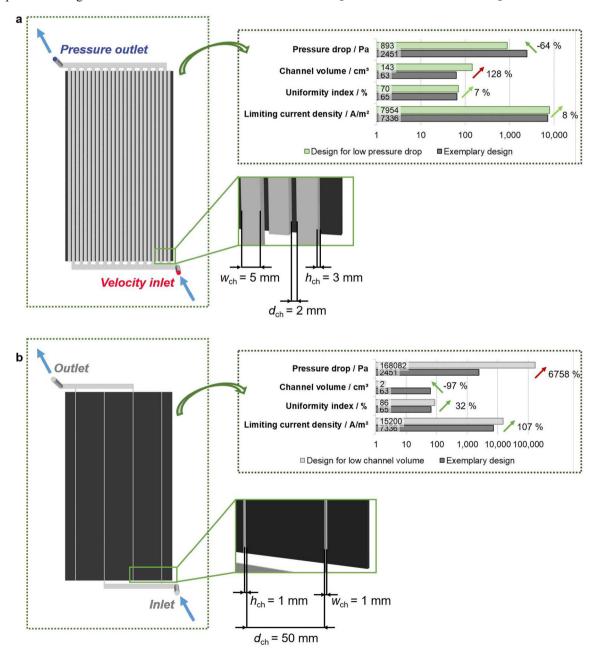


Fig. 6 IFF design with geometric dimensions and simulation results for minimum pressure drop (a) and minimum channel volume (b)

values are quite unevenly distributed and the uniformity index is quite low. Therefore, the observation of the velocity in the plane through the electrode centre allows to draw first conclusions about the flow uniformity in the entire electrode volume. On the outer edges of the electrode, stagnation zones are noticeable, which stand out by their very low velocity magnitude's values.

For different channel and land widths in dependence of the channel height, the simulations results for the four system parameters are explained. These system parameters are, on the one hand, the pressure drop between the cell inlet and cell outlet and the volume of all flow field channels, see Fig. 4. On the other hand, the relations between the flow field dimensions and the uniformity index as well as the limiting current density are presented in Fig. 5. The channel and land dimension are varied for the values, which are given in the methods section in Table 2. The specifications, which lead to the desired value of each system parameter, are highlighted by a coloured point in Figs. 4 and 5.

Starting with the investigation of the results towards a low pressure drop between the cell inlet and cell outlet, it is evident that the channel and land dimensions have a strong effect on the pressure drop, see Fig. 4a-c. Thereby, a large channel height and width as well as a small land width lead to a low pressure drop. The green points in the diagrams of Fig. 4 highlight those configurations, which satisfy best the demand of a low pressure drop depending on the observed channel height. An opposite behaviour can be observed for the flow field channel volume, see Fig. 4d-f. Obviously, the channel volume gets smaller as the flow field dimensions decrease and the land width increases.

The uniformity index does not follow a general trend depending on the channel and land dimensions, see Fig. 5a-c. It mainly differs depending on the number and position of the flow field channels. The land and channel width for the highest value of the uniformity index depend on the channel height.

The behaviour of the limiting current density in dependence of the flow field dimensions is different (Fig. 5). It increases as the average velocity in the electrode rises, which enhances the mass transfer coefficient. This is the case for a growing distance between the channels, which results from an increasing land width, see Fig. 5. This is analogous for the channel width. Nevertheless, the limiting current density barely increases due to changes of large land width values. This is due to the selected boundary conditions and in particular, due to the chosen correlation equation as well as inlet SoC, see methods section Eq. (19) and Table 3. In this case, a further increase in the land width does not lead to a significant increase of the limiting current density, as the SoC at the outlet is already very close to a value of 100%. Yet, the position, where the SoC of almost 100% is reached, changes due to an increase of the land width, see later on Fig. 8. Therefore, also the visible effect in Fig. 5d-f of the channel depth on the limiting current density is comparatively low. Assuming a correlation equation, which leads to lower values of the mass transfer coefficient, clarifies that the limiting current density is the largest for a low channel height and a large land width. This design is marked in Fig. 5d.

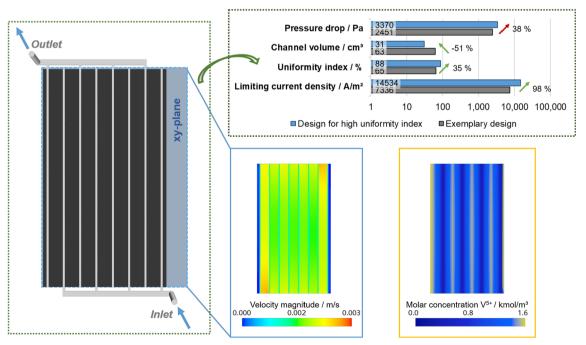


Fig. 7 Best IFF design for a very high uniformity index with its distribution of the velocity and the molar concentration in a plane through the electrode centre

In the following, the IFF designs, which best fulfil one of the system parameters, are investigated in more detail. The IFF design, which achieves the overall lowest pressure drop, is shown in Fig. 6a. The thick, deep and narrow flow field channels are clearly visible on the geometry scene. Those lead to a decreased path length of the fluid through the porous electrode and therefore to a reduced pressure drop. However, the channel volume is drastically increased in comparison with the exemplary design, compare Fig. 3. The best design for a low channel volume has completely opposite channel and land specifications than the one for a low pressure drop. The lowest channel volume is achieved by applying the minimum values for the channel dimensions and the maximum land width, which also leads to a high limiting current density, see Fig. 6b. The pressure drop is the highest for this design and exceeds the limit of 0.5 bar for the rule of PED by more than a factor of three.

The highest value for the uniformity index is gained in the observed parameter range for a flow field design, which has a large channel height and medium channel as well as land width $(w_{ch} = 3 \text{ mm}, h_{ch} = 3 \text{ mm}, d_{ch} = 22 \text{ mm})$, see Fig. 7. As this design cannot be identified due to an apparent trend of the uniformity index in dependence of the channel and land dimensions, it cannot be excluded that there exists another design within the observed parameter range, which might has a higher uniformity index value. A study with a smaller step size could insure the presented design to that circumstance. However, the available data basis does not give any hint that the dimensions of another design would be significantly different to the presented design. Indications of the flow uniformity within the electrode are deducible from the velocity distribution in a plane through the electrode centre, shown in Fig. 7. The values of the velocity magnitude are higher for this design and appear to be more even for these than for the exemplary design, compare Fig. 3. Furthermore, as the limiting current density of this design is already quite high, in Fig. 7 also the distribution of the molar concentration of V^{5+} for this plane is shown.

The maximum limiting current density is achieved by a flow field design with a low channel height and a large channel as well

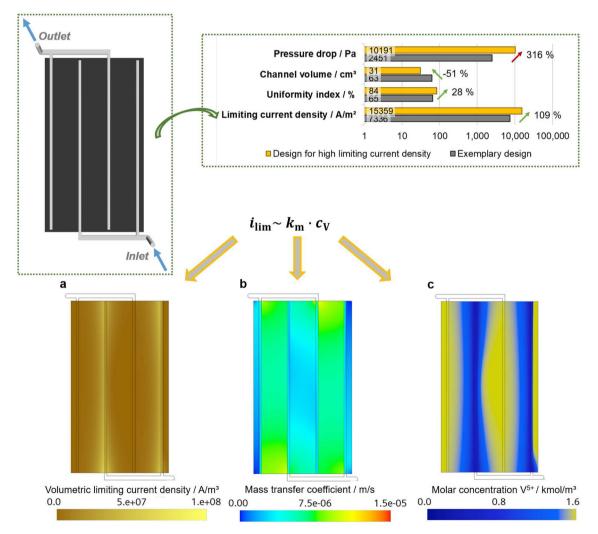


Fig. 8 Best flow field design for maximum limiting current density with the distribution in a plane through the electrode centre for volumetric limiting current density (a), mass transfer coefficient (b) and resulting molar concentration of V^{5+} (c)

as land width. For this design, the distribution of the limiting current density, which results from the mass transfer coefficient and the vanadium concentration, are illustrated for a plane through the electrode centre in Fig. 8. The volumetric limiting current density decreases between the channels, although the mass transfer coefficient does not strongly change, compare Figs. 8a and 8b. As explained before, the reason for this is the molar concentration of V⁵⁺, which reaches after a short distance in the electrode the maximum molar concentration and therefore a SoC of almost 100%, see Fig. 8c.

In summary, it is evident for the four analysed system parameters, that with regard to the varied input parameters, neither the 473

channel width or height nor the land width turn out to be similar for all presented flow field designs. Therefore, the total costs of a whole VFB system are introduced as a uniting target value. This target value allows the consideration of the four demands simultaneously, while searching for a compromise.

Cost model results

In order to be able to calculate the total costs of the VFB system, the previously considered system parameters are converted into the pump power density, the DoD and the nominal power density, see methods section.

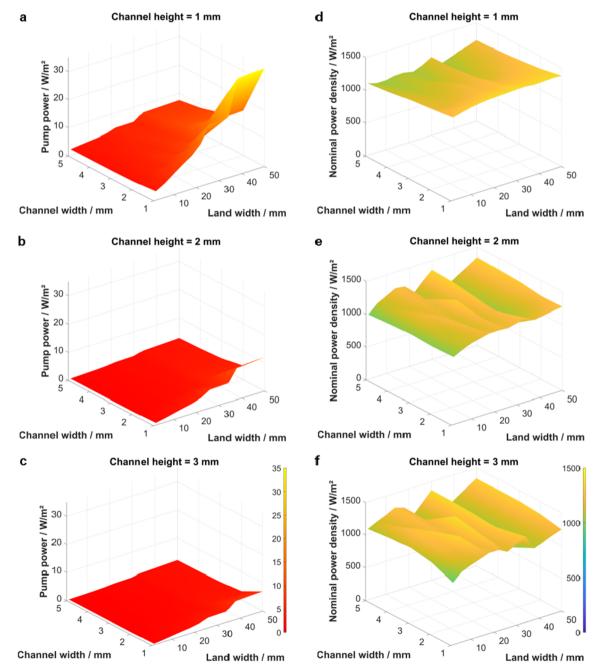


Fig. 9 Nominal power density (a-c) and pump power density (d-f) in dependence of the channel and land width

Parameters at system level

The pump and nominal power density are shown in dependence of the channel dimensions and land width in Fig. 9. The pump power density decreases analogously to the pressure difference between cell in- and outlet with declining channel width and height and growing land width, see Fig. 9a-c and compare with the pressure difference of Fig. 4a-c. The nominal power density increases analogously to the limiting current density with growing land width. The influence of the uniformity index on the nominal power density becomes evident, as the results for the limiting current and nominal power density

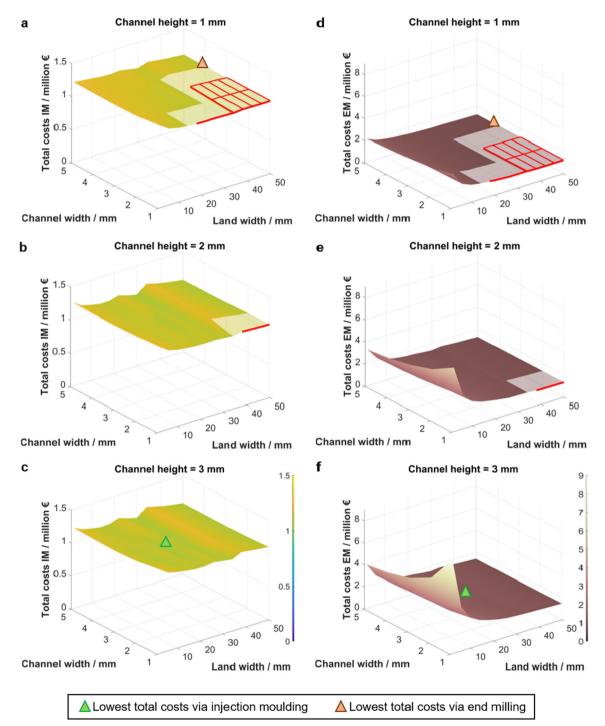


Fig. 10 For a production via injection moulding (**a-c**) and for a production via end milling (**d-f**), the total costs for VFB with a flow field production in dependence of the channel and land width. Red lines mark the designs, which have a pressure drop above 0.5 bar

considerably differ, see Fig. 9d-f and compare with Fig. 5. The power demand resulting from the pump power density is significantly lower than the nominal power density.

Total costs of VFB system

The total system costs of the VFB system consist of the electrolyte, component and production costs. For the electrolyte costs, the additional capacity, which is needed to raise the pump power, is obtained by the quotient of the pump power to the nominal power, see methods section Eq. (23). The additional capacity is very low under the selected boundary conditions, due to the comparatively low pump power. Therefore, the electrolyte costs result primarily from the set nominal capacity, which is independent from the channel dimensions of the IFF design. Moreover, the costs of the electrolyte depend on the DoD, which varies between 73% and 91%. The DoD has comparatively lower values for a small land width, which in return leads to increased electrolyte costs for these dimensions. In total, the geometric dimensions of the IFF design only affect the electrolyte costs to a minor extent.

The component costs directly depend on the total area of all cells of the system. These result from the ratio of the given nominal power and the needed pump power to the nominal power density. Starting from the constant nominal power, a small nominal power density leads to a large total area and vice versa, as the effect of the low pump power on the total area is rather small. Accordingly, small component costs result from a large nominal power density and the other way round, whereby the component costs are particularly large for small land width.

The total costs of the VFB, which are shown in Fig. 10a-c, are the sum of the electrolyte and component costs. This is due to the fact that it is assumed that no further flow field dependent production costs arise for the production via IM. As already outlined, the component costs and consequently the total costs depend on the total area of all cells. Therefore, for a low land width, the total costs are the largest. Moreover, for a high nominal power density, the total costs are low and vice versa, compare Figs. 10a-c and 9d-f.

For a flow field production by EM, the production costs are included in the total costs as well, see Fig. 10d-f. The specific production costs for EM are high for IFF designs with many deep channels. The lowest total costs arise for the IFF design with a small channel width and height as well as a quite large land width ($w_{ch} = 1 \text{ mm}$, $h_{ch} = 1 \text{ mm}$, $d_{ch} = 46 \text{ mm}$). This design is very similar to the one for the lowest channel volume, although the land width is a little bit lower. This is due to the fact, that for the small channel dimensions, the nominal power density is slightly lower for the maximum land width. This leads to some extent to higher component costs and

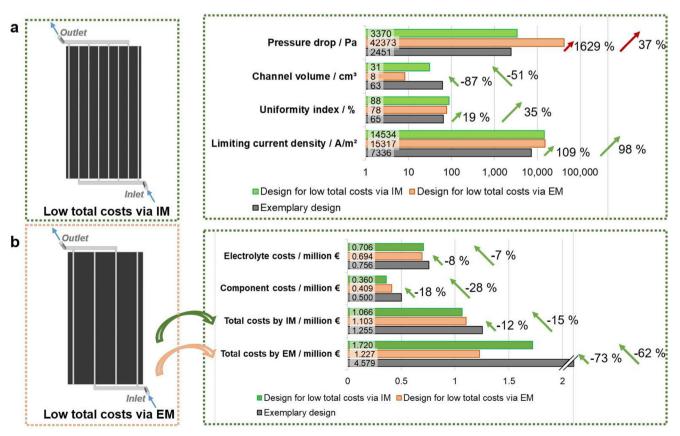


Fig. 11 Comparison of best flow field designs for minimum total costs by the flow field production via injection moulding (a) and via end milling (b)

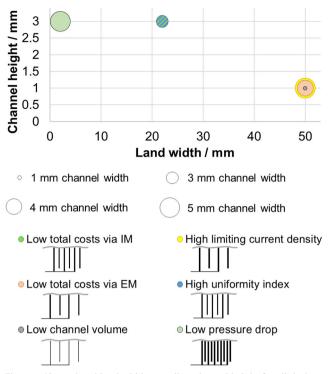


Fig. 12 Channel and land width as well as channel height for all designs reaching best each system parameters or minimum total costs with a rough geometry sketch of the flow field for each design

accordingly higher total costs. Yet, for this design, the pressure drop is larger than 0.5 bar and thereby exceeds the upper limit of the allowed pressure by PED restrictions. Excluding all designs with a pressure drop above 0.5 bar leads within the observed parameter range to a design, which has a large land and medium channel width and a low channel height ($w_{ch} =$ 4 mm, $h_{ch} = 1$ mm, $d_{ch} = 50$ mm), see Fig. 11b. Consequently, the selection of the flow field design with the minimum total costs for a production by EM strongly depends on the upper limit of the allowed pressure drop. Therefore, for instance changing the permeability of the electrode or even the electrode material or the volume flow rate might result in a different best design. In Fig. 10 all designs are marked by a red line, which have a pressure difference between cell in- and outlet above 0.5 bar. Furthermore, such areas are marked by a transparent colour, which represent the transition zones between those designs having a pressure drop above or bellow 0.5 bar.

The design, which achieves the minimum total costs for the production via IM, has a large channel width and height as well as a medium land width ($w_{ch} = 3 \text{ mm}$, $h_{ch} = 3 \text{ mm}$, $d_{ch} = 22 \text{ mm}$). The geometry of this design is shown in Fig. 11a. It leads to a lower pressure drop and higher uniformity index in comparison to the flow field design with the lowest production costs via EM.

There are just minor differences in the electrolyte and component costs for the two designs with the minimal total costs. The electrolyte costs are slightly larger for the IFF design by IM, as its achievable DoD is smaller. Yet, due to its higher nominal power density, its component costs are lower than those of the design by EM. Yet, for both designs the electrolyte and component costs are lower than these of the exemplary design of Fig. 3, as this design has a lower nominal power density and a lower DoD. Assuming that the two designs with the minimal total costs are manufactured by IM leads to quite similar costs. As expected, the total costs are lower for the design, which has the lowest total costs via IM. For the production method EM, the production costs have an impact on the total costs. The costs for the flow field design, which is best for IM, are higher for the production technique EM than the costs are for the design with the minimal total costs by EM. Although, the total costs are significantly larger for the exemplary design, which is mainly due to its high number of flow field channels.

It was shown, that the best IFF design strongly depends on the observed goal parameter. The precise choice of dimensions for the IFF design allows to reduce the costs of a VFB system. In comparison with the exemplary design, minor saving opportunities of less than 10% result for the electrolyte costs and medium saving opportunities with less than 30% for the component costs, see Fig. 11. Large saving of more than 60% are achievable for the total costs concerning the production technique EM.

Parameter	Name	Value	Unit
N _{fine}	Cell number for fine mesh	21,968,680	_
N _{middle}	Cell number for middle mesh	10,389,090	-
$p_{\rm fine}$	Pressure drop for fine mesh	2490.71	Ра
$p_{\rm middle}$	Pressure drop for middle mesh	2446.29	Ра
ψ_{fine}	Volume uniformity for fine mesh	65.144	%
ψ_{middle}	Volume uniformity for middle mesh	65.188	%
iL _{fine}	Limiting current density for fine mesh	7321.736	A/m ²
<i>iL</i> _{middle}	Limiting current density for middle mesh	7329.194	A/m ²

Table 5Mesh data andsimulation results of theexemplary flow field design forthe medium and fine mesh

Table 6 Extrapolated values forthe mesh evaluation of theexemplary flow field design

Parameter	Name	Value	Unit
p_{∞}	Pressure drop for zero mesh size	2530.56	Ра
ψ_{∞}	Volume uniformity for zero mesh size	65.105	%
iL_{∞}	Limiting current density for zero mesh size	7315.045	A/m ²
ERE_p	Extrapolated relative error for pressure drop	3.4	%
ERE_{ψ}	Extrapolated relative error for uniformity index	0.1	%
ERE _{iL}	Extrapolated relative error for limiting current density	0.2	%

Result combination

The channel width and height as well as land width for the observed best designs are summarized in Fig. 12. Additionally, a sketch of each design is shown in the figure's legend to further illustrate their dimensions. The channel and land dimensions can be contrary depending on the aspired goal parameter, which is the case for instance for a low pressure drop and a low channel volume. For the design of the lowest total costs by the production via EM, the flow field dimensions are very similar to those of the minimum channel volume. Yet, this design is not applicable due to the PED restrictions. Therefore, a larger channel and land width has to be applied. This design has quite similar dimensions to the one of the highest limiting current density. For the total costs by the production via IM the resulting IFF turns out to have channel and land dimensions, which are equal to those of the design with the highest uniformity index. Its dimensions are in the middle of the beforehand four observed system parameters. In dependence of the boundary conditions, the definition of the total costs allows to find a compromise for the different requests.

Conclusion

For a large number of different flow field channel and land dimensions, the four system parameters, pressure drop, volume of the flow field channels, uniformity index of the velocity and limiting current density, were systematically evaluated. Based on the CFD model of an exemplary IFF, the designs which allow to achieve the desired value of each of the system parameters were presented. As no single flow field design was optimal for all system parameters, the total costs of the VFB system in dependence of the flow field characteristics were introduced. Their definition allows the identification of a superior flow field design for the VFB, which takes the different system parameters simultaneously into account. For this evaluation of the entire VFB system, also the pump and nominal power density as well as the DoD in dependence of the flow field's channel and land dimensions were considered. They were used to estimate the costs for the electrolyte, the flow field production and the component, which together give the total costs of the VFB system. Finally, flow field designs were achieved, which cause less than half of the total costs for a production by EM in comparison to an initial exemplary design. Accordingly, the identified flow field designs lead to desired low total costs of a VFB system.

In this study, it was shown that many relations exist between the flow field dimensions, the boundary conditions, the system parameters and the VFB costs. Thereby, the analysis of the uniformity index might be enhanced in the future, as it strongly influences the resulting nominal power density. In prospective studies, the described approach can be applied for other cell sizes as well as for further flow field geometries and designs. Moreover, this method is applicable for other electrode materials and types of RFB.

Appendix

The ERE is calculated in dependence of the field variable δ by Eqs. (44), Eq. (45) and Eq. (46), which are taken from [24] for the mesh evaluation of particle packings. The fine mesh has a base size of 0.5 mm.

$$\delta_{\infty} = \delta_{\text{fine}} + \frac{\delta_{\text{fine}} - \delta_{\text{middle}}}{r_{\text{g}}^2 - 1} \tag{44}$$

$$r_{\rm g} = \sqrt{\frac{N_{\rm fine}}{N_{\rm middle}}} \tag{45}$$

$$\text{ERE} = \left| \frac{\delta_{\infty} - \delta_{\text{middle}}}{\delta_{\infty}} \right| \tag{46}$$

The values of the observed pressure drop, velocity uniformity and limiting current density for a fine and a medium size mesh with the number of mesh cells N are listed in Table 5. It is noticeable, that the values of Table 6 for the exemplary flow field design differ to a slight extend in comparison with the values for this design given in the Results and Discussion section. This is due small deviations in the starting conditions of the simulations, which result from the requirements of the parameter study. The calculated results are presented in Table 6.

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Authors' contributions Not applicable.

Availability of data and material Not applicable.

Availability of data and material Not applicable.		ot		i diodiciti Sciiniat fidilloci	
		au	_	Tortuosity	
Code availability Not applicable. Symbols used			ψ	_	Uniformity index
			Sub- and Superscripts		
			0	—	Initial
Symbols	Unit	Meaning	с	_	Compressed
•	m^{-1}	Specific surface area	с	-	Cell
а	mol m ^{-3}	Molar concentration	CE	_	Coulombic efficiency
С	mol m € m ⁻²		ch	_	Channel
c C		Specific costs	ch.	-	Charge
C	€	Costs	comp	_	Component
d	m	Diameter	dis.	_	Discharge
$d_{\rm ch}$	m 2 –1	Land width	EE	_	Energy efficiency
D	$m^2 s^{-1}$	Diffusion coefficient	EM	-	End milling
DoD	-	Depth of discharge	f	_	Fibre
F	$\rm C \ mol^{-1}$	Faraday's constant	F	_	Forchheimer
$h_{\rm ch}$	m	Channel height	fine	_	Fine mesh
i	$A m^{-2}$	Current density	IM	_	Injection moulding
i _{vol}	$A m^{-3}$	Volumetric current density	i	_	Inertial
Κ	m^2	Electrode permeability	iL	_	Limiting current density
k _m	${ m m~s}^{-1}$	Mass transfer coefficient	in	_	Inlet
l	m	Length	lim	_	Limiting
η	_	Efficiency	m	_	Mass
n	_	Number	max		Maximum
р	Pa	Pressure	middle	_	Middle mesh
Р	W	Power	min	—	Minimum
Pi	kg m ^{-4}	Inertial resistance tensor		—	
P _v	$kg m^{-3} s^{-1}$	Viscous resistance tensor	mix	-	Mixture
Q	Ws	Capacity	N	—	Nominal
2 R	$J K^{-1} mol^{-1}$	Universal gas constant	OCV	-	Open circuit voltage
R_0	$\Omega \text{ cm}^2$	Specific cell resistance	p	-	Pressure drop
Re	_	Reynolds number	PE	-	Positive electrolyte
S	mol $m^{-3} s^{-1}$	Source term	prod	_	Production
S Sc	_	Schmidt number	S	-	Superficial
Sh	_	Sherwood number	t	_	Turbulent
SoC		State of charge	uni	-	Uniformity
50C	_	Time	V	-	Viscous
ι Τ	S V		ν	_	Velocity
T T	K kg m ⁻¹ s ⁻²	Temperature	V	-	Vanadium
	kg m s V	Stress tensor	VE	_	Voltage efficiency
U	$v m s^{-1}$	Voltage	V4+	_	Vanadium 4+
V		Velocity	wear	_	Cutter wear
V	m ³	Volume	Y_i	_	For mass fraction of species i
Wch	m	Channel width	ψ	_	Uniformity index
					,

Molecular weight of species i

Mass fraction of species i Electron stoichiometry

Forchheimer constant

Field variable

Dynamic viscosity

Turbulent Schmidt number

Porosity

Density

 $\mathrm{kg} \ \mathrm{mol}^{-1}$

 $m^{-1} \\$

Pa s

_

 $kg \ m^{-3}$

_

 W_i

 Y_i

z

 $\beta_{\rm F}$

 δ

ε

μ

ρ

 $\sigma_{\rm t}$

Greek symbols

∞	-	Zero mesh size
Abbreviations		
CFD	-	Computational fluid dynamics
DoD	-	Depth of discharge
EM	-	End milling
ERE		Extrapolated relative error
IFF	-	Interdigitated flow field
IM	-	Injection moulding
PE	-	Positive electrolyte
PED	-	Pressure equipment directive
SoC	_	State of charge
VFB	_	Vanadium redox-flow batteries

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Declarations

Conflict of interest The authors have no relevant conflicts of interest to declare.

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