

# Accurate disparity estimation in light field using ground control points

Hao Zhu<sup>1</sup>, Qing Wang<sup>1</sup> (✉)

© The Author(s) 2016. This article is published with open access at Springerlink.com

**Abstract** The recent development of light field cameras has received growing interest, as their rich angular information has potential benefits for many computer vision tasks. In this paper, we introduce a novel method to obtain a dense disparity map by use of ground control points (GCPs) in the light field. Previous work optimizes the disparity map by local estimation which includes both reliable points and unreliable points. To reduce the negative effect of the unreliable points, we predict the disparity at non-GCPs from GCPs. Our method performs more robustly in shadow areas than previous methods based on GCP work, since we combine color information and local disparity. Experiments and comparisons on a public dataset demonstrate the effectiveness of our proposed method.

**Keywords** disparity estimation; ground control points (GCPs); light field; global optimization

## 1 Introduction

With the rapid development of computational photography, many computational imaging devices have been invented, based on, e.g., coded apertures [1], focal sweep [2], and light fields [3, 4], examples of the latter being the Lytro (<https://lytro.com>) and Raytrix (<http://www.raytrix.de>) cameras. As a light field camera captures both spatial and angular information about the distribution of light rays in space, it provides a potential basis for many fundamental operations in computer vision [5–8]. In this paper, we focus on accurate disparity estimation using the light field.

Disparity estimation in stereo [9–11] is a long-standing problem in computer vision, and it plays an important role in many tasks. Given two or more images captured from different viewpoints, the fundamental problem is to find the optimal correspondence between these images. Unlike the point information captured by a traditional camera, a light field camera captures information about the light, providing a full description of the real world via a 4D function. We can obtain so-called sub-aperture images [12], and synthesize a multi-view representation of the real world. Unlike the wide baseline used in traditional multi-view stereo, the multi-view representation synthesized by the light field has a narrow baseline, which can provide more accurate sub-pixel disparity estimation.

Previous work [13, 14] has computed an optimized disparity map based on local estimation, which includes both reliable and unreliable information. Undoubtedly, reliable points will have a positive effect on the global disparity map, but the effect of unreliable points may be detrimental. To reduce the negative effects of unreliable points, we propose to obtain a dense disparity map from certain reliable estimation points in the light field called ground control points (GCPs) [15]. GCPs are sparse points which can be matched reliably in stereo, and are often obtained by stable matching or laser scanning. We determine GCPs by the reliability of the structure tensor, and construct the GCP spread function based on color similarity and local disparity similarity. By combining local disparities, the proposed method performs more robustly than the previous GCP method in shadow areas: experimental results on the LFBF dataset [16] show that our method performs more robustly than the original light field method [14] and the original

<sup>1</sup> School of Computer Science, Northwestern Polytechnic University, Xi'an 710072, China. E-mail: qwang@nwpu.edu.cn (✉).

Manuscript received: 2015-12-01; accepted: 2016-04-01

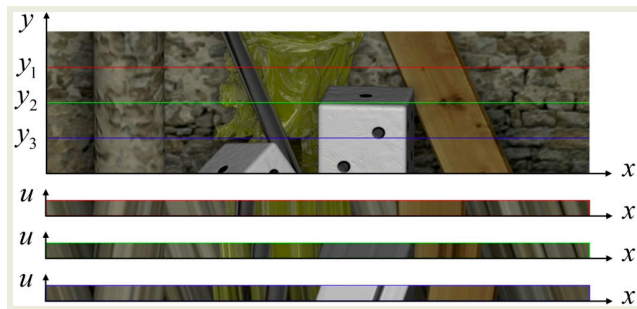
GCP method [15].

The rest of this paper is organized as follows. In Section 2, we review the background and prior work on depth estimation from a light field and the GCP method. Section 3 describes our algorithm. We give the experimental results in Section 4, and our conclusions and suggestions for future work are provided in Section 5.

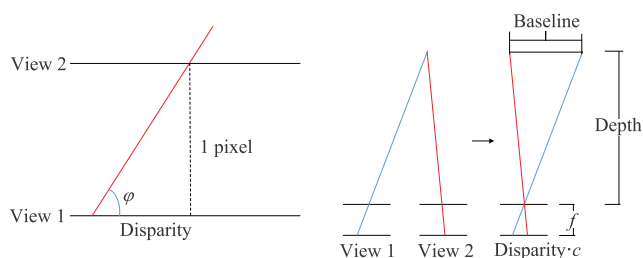
## 2 Background and related work

A light field [17] is represented by a 4D function  $f(x, y, u, v)$ , where the dimensions  $(x, y)$  describe the spatial distribution of light, and the dimensions  $(u, v)$  describe the angular distribution of light. When we fix one spatial dimension  $y^*$  and one angular dimension  $v^*$ , we get the epipolar plane image (EPI) [18] (see Fig. 1).

In a rectified EPI, the slope  $k$  of a line has a linear relationship with the depth  $d$  (see Fig. 2), the larger the depth, the larger the slope:  $d = fsk/c$ , where  $f$  is the focal length of the lens,  $s$  is the baseline between the two views, and  $c$  is the pixel size. Given the EPI structure, the depth estimation problem is converted into a slope detection problem. As light field cameras capture angular information, analyzing the EPI is a suitable way to estimate depth using the light field.



**Fig. 1** The epipolar plane image obtained by fixing one spatial dimension and one angular dimension.



**Fig. 2** Left: epipolar plane image. Note that the slope is the reciprocal of the disparity. Right: the inverse relationship between disparity and depth. The relationship between slope and depth is linear.

**Structure tensor (ST).** Wanner and Goldluecke [14] proposed to analyze the EPI by the structure tensor, obtaining the local disparity and the corresponding reliability at the same time. They then optimized the local disparity map by a global energy function based on variational regularization. However, as they pointed out, the sampling of viewpoints must be dense enough to guarantee that the disparity between two views is less than 2 pixels, otherwise the straight line will become a broken line in the EPI, leading to inaccurate local estimation. This issue will be discussed in Section 3.1.

**Lisad transform.** Tasic and Berkner [19] proposed the light field scale and depth transform. They initially detected the slope of the epipolar tube [20] in Lisad-2 space, and then repaired depth discontinuous areas using the slope of the epipolar strip [20] detected in Lisad-1 space.

**Multiple cues.** Tao et al. [21] proposed a method to estimate depth by combining multiple cues, including correspondence cues and defocus cues. The advantages of using different cues in different areas were exploited, and they obtained good results for real scenes.

**RPCA (robust principle component analysis) matching.** Heber and Pock [22] considered the highly redundant nature of the light field, and proposed a new global matching term based on low rank minimization. Their method achieves the best results on synthetic datasets.

**GCP method.** Ground control points are sparse points which can be matched reliably in stereo. Wang and Yang [15] proposed to predict the disparity of non-GCPs from GCPs, and optimized the initial disparity map using a Markov random field (MRF) energy function containing three terms: a data term, a smoothness term, and the GCP term. The top ranking results achieved on the Middlebury dataset prove that it is a good approach to stereo matching. However, it performs poorly in shadow (see Fig. 5) as it assumes that two points with similar colors should have similar disparities, but the colors may differ between a center point and its neighbors while their disparities are similar.

## 3 Theory and algorithm

### 3.1 Algorithm overview

Our approach is given in Algorithm 1. The input

**Algorithm 1:** Our GCP algorithm

**Input:**  
 Multi-view images  $I_1, \dots, I_N$  generated from light field  $L$ ;  
 reference view index  $r$ .  
**Output:**  
 Global optimal disparity map  $D$ .  
**Process:**  
 $(D_0, R_0) = \text{StructureTensor}(I_1, \dots, I_N);$      $\triangleright$  Section 3.2  
 $G = \text{GetGCPs}(R_0);$      $\triangleright$  Section 3.2  
 $\tilde{D} = \text{GCPSpread}(I_r, D_0, G);$      $\triangleright$  Section 3.3  
 $E = E_{\text{data}} + E_{\text{smooth}} + E_{\text{GCP}}(\tilde{D});$      $\triangleright$  Section 3.4  
 $D = \text{GraphCut}(E).$      $\triangleright$  Section 3.4

is the 4D light field  $L(x, y, u, v)$  and the reference view index  $r$ . The output is the disparity map  $D$ . The algorithm consists of five steps:

1. *Local estimation.* The local disparity map and its reliability map are obtained by using the structure tensor method (see Section 3.2).
2. *GCP detection.* The most credible points as determined by the reliability map are selected as the GCPs (see Section 3.2).
3. *GCP optimization.* The GCP spread function is built using the local disparity map and the set of GCPs. By using this function, intermediate results are obtained (see Section 3.3).
4. *Building the energy function.* The intermediate results from GCP optimization are combined with traditional stereo matching function results (see Section 3.4).
5. *Final optimization.* The energy function is found by optimization (see Section 3.4).

**3.2 Local disparity and GCPs**

We use the structure tensor to detect the slopes of lines in the EPI:

$$J = \begin{bmatrix} G_\sigma(S_x S_x) & G_\sigma(S_x S_y) \\ G_\sigma(S_x S_y) & G_\sigma(S_y S_y) \end{bmatrix} = \begin{bmatrix} J_{xx} & J_{xy} \\ J_{xy} & J_{yy} \end{bmatrix} \tag{1}$$

where  $G_\sigma$  represents a Gaussian smoothing operator, and  $S_x, S_y$  represent the gradients of the EPI in  $x$  and  $y$  directions respectively.

Then, the direction of the line is

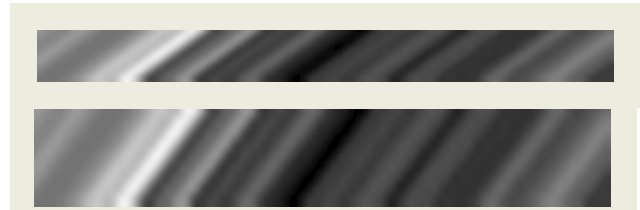
$$\phi = \frac{1}{2} \arctan\left(\frac{J_{yy} - J_{xx}}{2J_{xy}}\right) \tag{2}$$

and its reliability is measured by the coherence of the structure tensor:

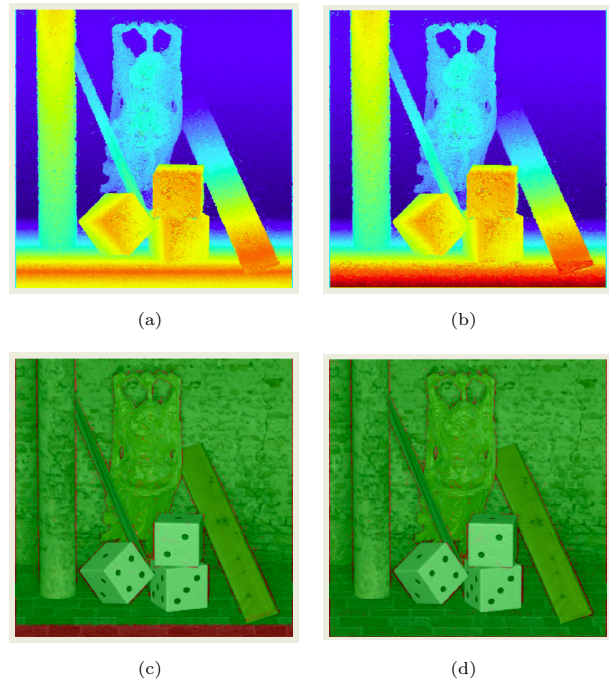
$$r = \frac{(J_{yy} - J_{xx})^2 + 4J_{xy}^2}{(J_{xx} + J_{yy})^2} \tag{3}$$

It is worth noting that the structure tensor performs poorly in the near field (see Fig. 4), which corresponds to the low-slope area in the EPI; in other words, the disparity between two views is larger than 2 pixels in these areas. We adopt the easiest method to solve this issue—by scaling up the EPI along the  $y$  axis in these areas to convert the low-slope area into a high-slope area. We use bicubic interpolation to scale up the EPI. After calculating the slope of the scaled EPI, we can recover the slope of the original EPI by dividing by the scaling factor. An original EPI and the scaled up EPI can be seen in Fig. 3. The improvement of our method can be seen in Fig. 4.

Having obtained the coarse disparity map  $D_0$  and its reliability map  $R_0$  from the structure tensor,



**Fig. 3** Top: an original EPI. Bottom: the scaled up EPI. Clearly, the slopes of the lines are greater in the latter.



**Fig. 4** Disparity and error map obtained by the basic structure tensor method and our method for the Buddha dataset. (a) Disparity map obtained by the basic structure tensor method. (b) Disparity map obtained by our improved method. The basic structure tensor method performs poorly at close range. (c) and (d) Relative depth error maps for the above two methods. Relative depth errors of more than 1% are indicated in red. The error rates of these two methods are 7.87% and 3.97%, respectively.

it is unnecessary to do stable matching or laser scanning to obtaining GCPs; to do so would be time-consuming and laborious. We obtain the set of GCPs  $G$  from the reliability map  $R_0$ .

### 3.3 GCP spread function

The inputs to our GCP spread function are the reference view image  $I_r$ , the local disparity map  $D_0$ , and the set of GCPs  $G$ .

Unlike Wang and Yang’s method [15], which constrains similar colors to have similar disparities, we use the constraint that two neighboring pixels  $p$  and  $q$  should have similar disparities if not only their colors are similar but also their local disparities are similar. This constraint can be described by minimizing the difference between the disparity of  $p$  and a weighted combination of its neighbors’ disparities. The global cost function is given by

$$J(\tilde{D}) = \left( \tilde{D}_p - \frac{\sum_{q \in N_8(p)} \omega_{pq} \tilde{D}_q}{\sum_{q \in N_8(p)} \omega_{pq}} \right)^2 \tag{4}$$

where  $\tilde{D}$  is the optimal disparity map found by minimizing this global cost function.  $N_8(p)$  comprises  $p$ ’s 8-connected neighbors;  $\omega_{pq}$  are weights based on a color term and a disparity term:

$$\omega_{pq} = \max \left( \exp \left( \frac{-\Delta C_{pq}}{\gamma_c} + \frac{-\Delta D_{0,pq}}{\gamma_d} \right), \epsilon \right) \tag{5}$$

where  $\Delta C_{pq}$  and  $\Delta D_{0,pq}$  are respectively the Euclidean distances between pixels in RGB color space and local disparity ( $D_0$ ) space. Parameters  $\gamma_c$ ,  $\gamma_d$ , and  $\epsilon$  control sharpness of the function. To ensure that the disparity term and the color term have the same order of magnitude, the parameter  $\gamma_d$  is not independent, and is calculated from the following equation:

$$\gamma_d = s_{\gamma_d} \frac{\gamma_c (d_{\max} - d_{\min})}{(C_{\max} - C_{\min}) \sqrt{N_C}} \tag{6}$$

where  $C_{\max}$  and  $C_{\min}$  are the maximum and minimum values in color space, 255 and 0 respectively.  $N_C$  is the number of color channels, here 3. Parameters  $d_{\max}$  and  $d_{\min}$  are the maximum and minimum values in hypothetical disparity space, respectively.  $s_{\gamma_d}$  is a weight to control the strength of the disparity term. We suggest that the disparity term should be larger than the color term, so  $s_{\gamma_d} < 1$ .

Equation (4) is a quadratic function. After taking its derivative to find the extremum, we find that the disparity of the center point  $p$  has a linear

relationship with the disparities of its neighbors:

$$\begin{aligned} \tilde{D}_p &= \frac{\sum_{q \in N_8(p)} \omega_{pq} \tilde{D}_q}{\sum_{q \in N_8(p)} \omega_{pq}} \\ &= \sum_{q \in N_8(p)} \alpha_{pq} \tilde{D}_q \end{aligned} \tag{7}$$

$$\alpha_{pq} = \frac{\omega_{pq}}{\sum_{q \in N_8(p)} \omega_{pq}} \tag{8}$$

Given the linear relationship above, we can derive the disparity of non-GCPs from GCPs by solving a system of sparse linear equations  $(\mathbf{I} - \mathbf{A})\mathbf{x} = \mathbf{b}$ , where  $\mathbf{I}$  is an identity matrix, and  $\mathbf{A}$  is an  $N \times N$  matrix ( $N$  is the number of points in the image). In each row of  $\mathbf{A}$ , if the corresponding pixel  $p$  belongs to the GCPs, all elements are zero, otherwise only the 8-connected neighbor points  $q$  have non-zero values, equal to their weights  $\alpha_{pq}$ . Similarly, for the elements in vector  $\mathbf{b}$ , only the pixels belonging to GCPs have non-zero values, and are equal to their initial disparities.  $\mathbf{x}$  is the optimal disparity map that we hope to obtain.

### 3.4 Energy functions with the GCPs

Our energy function contains three terms: a data term, a smoothness term, and the GCP term.

As the length of the baseline between two views in the light field camera is narrow, we combine the basic sum of squared differences (SSD) and sum of squared gradient differences (SSGD) as our data term to ensure good matching:

$$E_{\text{data}}(D) = E_{\text{basic}}(p, D(p)) + E_{\text{grad}}(p, D(p)) \tag{9}$$

where

$$\begin{aligned} E_{\text{basic}}(p, D(p)) &= \sum_{i \in V} \sum_{q \in N(p)} \{I_i(q) - I_r[q + D(p)(i - r)]\}^2 \end{aligned} \tag{10}$$

and

$$\begin{aligned} E_{\text{grad}}(p, D(p)) &= (1 - \alpha) \cdot \sum_{i \in V} \sum_{q \in N(p)} \{I_{i,gx}(q) - I_{r,gx}[q + D(p)(i - r)]\}^2 \\ &\quad + \alpha \cdot \sum_{i \in V} \sum_{q \in N(p)} \{I_{i,gy}(q) - I_{r,gy}[q + D(p)(i - r)]\}^2 \end{aligned} \tag{11}$$

Here,  $D$  is the global optimal disparity map,  $D(p)$  is the disparity value of point  $p$ ,  $V$  is the number of views in the light field,  $N(p)$  is an image patch centered at pixel  $p$ ,  $I_r$  is the reference view in the light field, and  $I_{i,gx}$  and  $I_{i,gy}$  are the gradients of the  $i$ -th view image in  $x$  and  $y$  directions, respectively.



We select the widely used linear model based on a 4-connected neighborhood system as our smoothness term, which is expressed as

$$E_{\text{smooth}}(D) = \lambda_s \sum_{p \in I_r} \sum_{q \in N_4(p)} \omega_{pq} \Delta D_{pq} \quad (12)$$

where  $\Delta D_{pq}$  is the difference in disparity between pixels  $p$  and  $q$ ,  $\lambda_s$  is a smoothness coefficient to control the strength smoothing, and  $\omega_{pq}$  is a weight based on the distance between  $p$  and  $q$  in RGB color space:

$$\omega_{pq} = \max \left( \exp \left( \frac{-\Delta C_{pq}}{\gamma_c} \right), \epsilon \right) \quad (13)$$

Given the optimal disparity  $\tilde{D}_p$  obtained by the GCP spread function in Eq. (7), we can now employ the robust penalty function [15]:

$$\begin{aligned} E_{\text{GCP}}(D) &= \lambda_r \sum_{p \in I_r} \varphi(D_p, \tilde{D}_p) \\ &= -\lambda_r \sum_{p \in I_r} \ln \left( (1 - \eta) \exp \left( \frac{-|D_p - \tilde{D}_p|}{\gamma_d} \right) + \eta \right) \end{aligned} \quad (14)$$

where  $\lambda_r$  is a regularization coefficient that controls the strength of the GCP energy;  $\gamma_d$  and  $\eta$  control the sharpness and upper-bound of the penalty function.

## 4 Experimental results

### 4.1 Parameters and dataset

In our experiments, we have found that the structure tensor method performs poorly for lines in the EPI with slope larger than 0.65. So, we first analyze the EPI by structure tensor, and then if the slope of 50% of points is larger than 0.65, we scale this EPI from 9 to 17 pixels in the  $y$  direction, and reanalyze the EPI.

We set two thresholds to select GCPs, using absolute reliability and relative reliability. The absolute reliability is set to 0.99 in our implementation. If the reliability of a point is larger than 0.99, it is classified as a GCP. If only this criterion is used, GCPs may be too sparse in some datasets to reliably determine the disparity map calculated from the GCPs. We thus also consider relative reliability. If the fraction of GCPs obtained by considering absolute reliability is smaller than a set percentage (20%), we select the 20% most reliable points as GCPs.

For the disparity map obtained from GCPs, the parameters  $\gamma_c$  and  $\epsilon$  are set to 30 and 0, respectively.

The weight parameter  $s_{\gamma_d}$  is set to 0.25. Note that if  $\gamma_c$  or  $\gamma_d$  is unsuitable, the sparse linear system may be singular.

In the data term, the parameter  $\alpha$  is set to 0.5, and the size of image patches is  $7 \times 7$ . The parameters  $\gamma_c$  and  $\epsilon$  in the smoothness term are set to 3.6 and 0.3, respectively. And the parameters  $\eta$  and  $\gamma_d$  are set to 0.005 and 2 according to Wang and Yang [15], respectively. In the final energy function, the smoothness coefficient  $\lambda_s$  and the GCP scaling coefficient  $\lambda_r$  are set to 1.67 and 4.67, respectively. We divide the disparity into 120 levels, and use linear interpolation to get floating point values for use in the data term. We use GCO-v3 [23–25] to optimize our energy function.

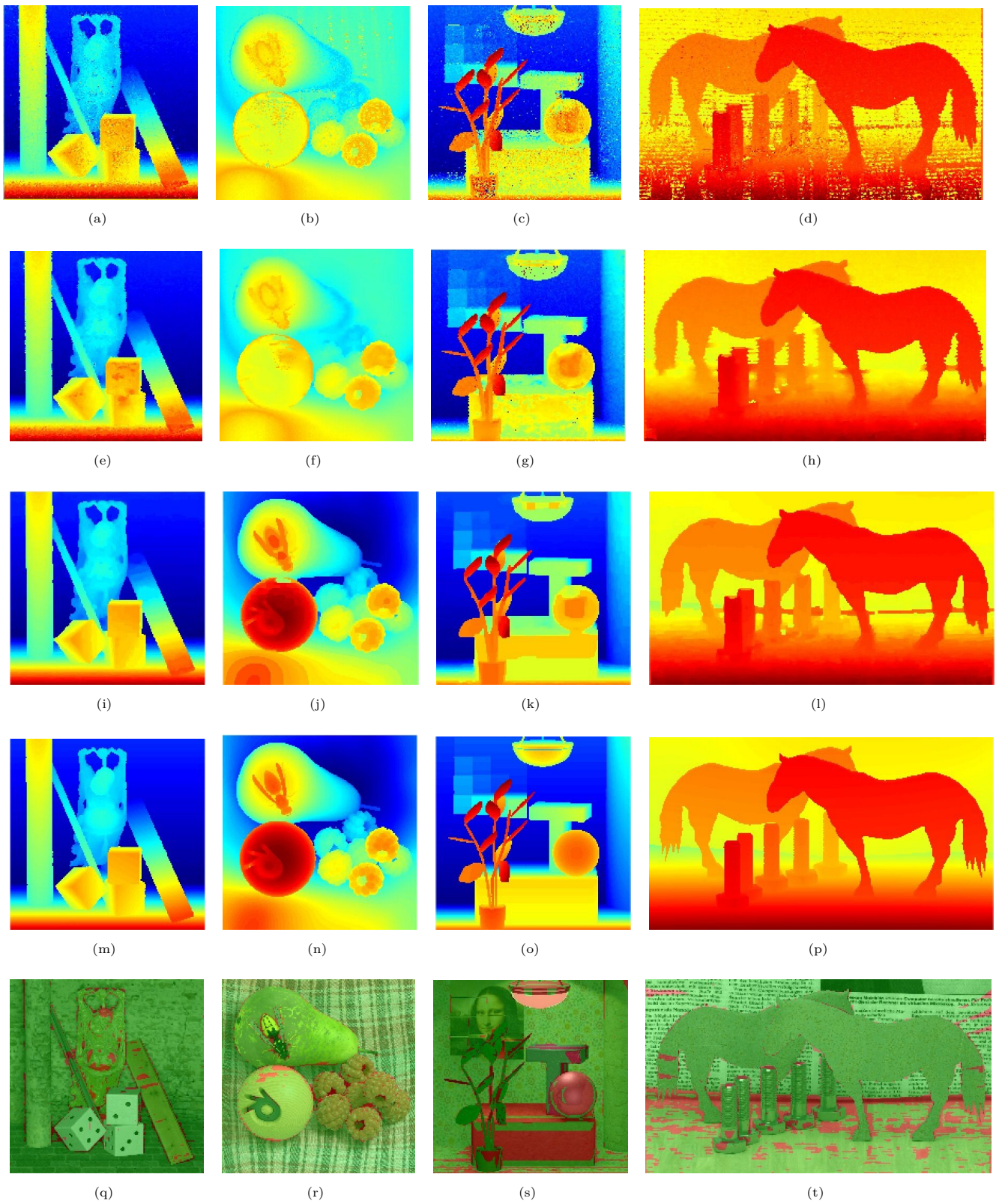
We tested our method using HCI LFBD [16], which contains synthetically generated light fields, each of which is represented by  $9 \times 9$  sub-aperture images. The dataset was rendered by Blender (<http://www.blender.org>), and contains the ground truth.

Our algorithm was implemented in MATLAB, on MacOS X 10.11.1 with 8 GB RAM and a 2.7 GHz processor. The running time for a  $9 \times 9 \times 768 \times 768 \times 3$  light field is 60 minutes. Most of the cost is to build two large sparse matrices for the smoothness term and the GCP term, and could be greatly reduced by reimplementation in C.

### 4.2 Comparison with previous works

We compare our GCP propagation method with the basic structure tensor method and Wang and Yang's method [15] in Fig. 5. Our method performs more robustly than Wang and Yang's in shadows and in color discontinuous areas.

We also compare our results with Wanner and Goldluecke's [14] and Wang and Yang's [15] results, as shown in Fig. 6. Note that there is much noise in the initial map; there is reduced noise after the GCPs' spread. A quantitative comparison can be seen in Table 1. We select the relative depth error as our criterion (we used 0.2% here). Our method performs better than Wanner and Goldluecke's on 4 datasets, but worse on 3 datasets. On analyzing these 7 datasets we find that there are few transparent materials in the Buddha, StillLife, Horses, and Medieval datasets, but more transparent materials and shadows, lamps, and mirrors in the Buddha2, Mona, and Papillon

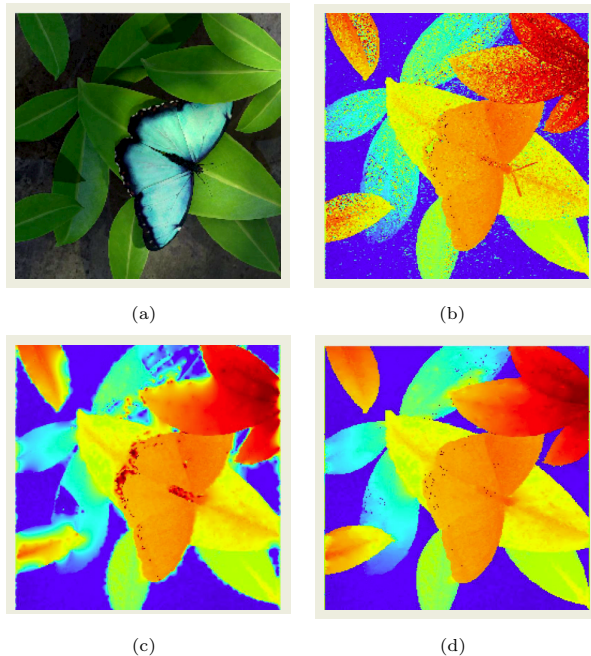


**Fig. 6** Results of our method on Buddha, StillLife, Mona, and Horses datasets from LFBD. Top: initial disparity map  $D_0$ . 2nd row: results  $\tilde{D}$  from the GCP spread function. 3rd row: final results of our method. 4th row: ground truth. Bottom: error map. Relative depth errors of more than 0.2% are shown in red.



**Table 1** Percentage of pixels with depth error more than 0.2% for LFBD [16]. The results of Wanner and Goldluecke's method were obtained by running their public source code. The results of Wang and Yang's method were obtained by our implementation (Unit: %)

	Buddha	Buddha2	Mona	Papillon	StillLife	Horses	Medieval
Wanner and Goldluecke's [14]	7.28	26.55	15.08	16.64	4.50	16.44	24.33
Wang and Yang's [15]	5.50	35.31	25.80	18.39	4.55	14.25	24.75
Our method	5.50	34.81	25.86	17.56	3.61	13.29	23.24

**Fig. 5** Comparison. (a) Input dataset; there are two colors in the butterfly and a shadow on the leaves to the left of the butterfly. (b) Basic structure tensor result, showing many points with wrong values. (c) Wang and Yang's propagation strategy assigns wrong disparities to shadow areas and divides the butterfly into 2 parts along the color boundary in its tail. (d) Result of our GCP propagation method, with few wrong values and good performance in shadow areas.

datasets. Stereo matching outperforms the structure tensor method in a Lambertian environment, whilst the structure tensor performs better in non-Lambertian environments.

Our method performs better than Wang and Yang's method, especially for the Papillon, StillLife, and Horses datasets. Note that there exist some shadows in these datasets; the disparities of shadow areas ought to be the same as those of their neighborhoods. As local disparity information is combined in our GCP spread function, our method outperforms Wang and Yang's.

## 5 Conclusions and future work

In this paper, we have proposed the idea to determine GCPs by using the reliability of the structure tensor.

We also give a more robust GCP spread function than Wang and Yang's [15] to propagate disparity from GCPs to non-GCPs. Experimental results on LFBD show that our method performs more robustly than Wanner and Goldluecke's and Wang and Yang's methods. However, our method performs less well in strong light and complicated shadow areas; this is a problem for most stereo methods. In the future, we will continue to investigate stereo in light fields, and take the advantages of more features of light field to solve these problems.

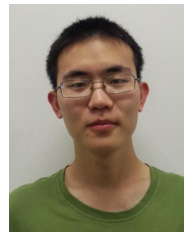
## Acknowledgements

The work was supported by National Natural Science Foundation of China (Nos. 61272287, 61531014) and a research grant from the State Key Laboratory of Virtual Reality Technology and Systems (No. BUAA-VR-15KF-10).

## References

- [1] Levin, A. Analyzing depth from coded aperture sets. In: *Lecture Notes in Computer Science, Vol. 6311*. Daniilidis, K.; Maragos, P.; Paragios, N. Eds. Springer Berlin Heidelberg, 214–227, 2010.
- [2] Zhou, C.; Miao, D.; Nayar, S. K. Focal sweep camera for space-time refocusing. Columbia University Academic Commons, 2012. Available at <http://hdl.handle.net/10022/AC:P:15386>.
- [3] Lumsdaine, A.; Georgiev, T. The focused plenoptic camera. In: *Proceedings of IEEE International Conference on Computational Photography*, 1–8, 2009.
- [4] Ng, R.; Levoy, M.; Brédif, M.; Duval, G.; Horowitz, M.; Hanrahan, P. Light field photography with a handheld plenoptic camera. Stanford Tech Report CTSR, 2005.
- [5] Birkbauer, C.; Bimber, O. Panorama light-field imaging. *Computer Graphics Forum* Vol. 33, No. 2, 43–52, 2014.
- [6] Dansereau, D. G.; Pizarro, O.; Williams, S. B. Linear volumetric focus for light field cameras. *ACM Transactions on Graphics* Vol. 34, No. 2, Article No. 15, 2015.
- [7] Li, N.; Ye, J.; Ji, Y.; Ling, H.; Yu, J. Saliency detection on light field. In: *Proceedings of IEEE Conference on*

- Computer Vision and Pattern Recognition, 2806–2813, 2014.
- [8] Raghavendra, R.; Raja, K. B.; Busch, C. Presentation attack detection for face recognition using light field camera. *IEEE Transactions on Image Processing* Vol. 24, No. 3, 1060–1075, 2015.
- [9] Scharstein, D.; Szeliski, R. A taxonomy and evaluation of dense two-frame stereo correspondence algorithms. *International Journal of Computer Vision* Vol. 47, No. 1, 7–42, 2002.
- [10] Du, S.-P.; Masia, B.; Hu, S.-M.; Gutierrez, D. A metric of visual comfort for stereoscopic motion. *ACM Transactions on Graphics* Vol. 32, No. 6, Article No. 222, 2013.
- [11] Wang, M.; Zhang, X.-J.; Liang, J.-B.; Zhang, S.-H.; Martin, R. R. Comfort-driven disparity adjustment for stereoscopic video. *Computational Visual Media* Vol. 2, No. 1, 3–17, 2016.
- [12] Wanner, S.; Fehr, J.; Jähne, B. Generating EPI representations of 4D light fields with a single lens focused plenoptic camera. In: *Lecture Notes in Computer Science, Vol. 6938*. Bebis, G.; Boyle, R.; Parvin, B. et al. Eds. Springer Berlin Heidelberg, 90–101, 2011.
- [13] Wanner, S.; Goldluecke, B. Globally consistent depth labeling of 4D light fields. In: Proceedings of IEEE Conference on Computer Vision and Pattern Recognition, 41–48, 2012.
- [14] Wanner, S.; Goldluecke, B. Variational light field analysis for disparity estimation and super-resolution. *IEEE Transactions on Pattern Analysis and Machine Intelligence* Vol. 36, No. 3, 606–619, 2014.
- [15] Wang, L.; Yang, R. Global stereo matching leveraged by sparse ground control points. In: Proceedings of IEEE Conference on Computer Vision and Pattern Recognition, 3033–3040, 2011.
- [16] Wanner, S.; Meister, S.; Goldluecke, B. Datasets and benchmarks for densely sampled 4D light fields. In: Proceedings of Annual Workshop on Vision, Modeling and Visualization, 225–226, 2013.
- [17] Levoy, M.; Hanrahan, P. Light field rendering. In: Proceedings of the 23rd Annual Conference on Computer Graphics and Interactive Techniques, 31–42, 1996.
- [18] Bolles, R. C.; Baker, H. H.; Marimont, D. H. Epipolar-plane image analysis: An approach to determining structure from motion. *International Journal of Computer Vision* Vol. 1, No. 1, 7–55, 1987.
- [19] Tomic, I.; Berkner, K. Light field scale-depth space transform for dense depth estimation. In: Proceedings of IEEE Conference on Computer Vision and Pattern Recognition Workshops, 441–448, 2014.
- [20] Criminisi, A.; Kang, S. B.; Swaminathan, R.; Szeliski, R.; Anandan, P. Extracting layers and analyzing their specular properties using epipolar-plane-image analysis. *Computer Vision and Image Understanding* Vol. 97, No. 1, 51–85, 2005.
- [21] Tao, M. W.; Hadap, S.; Malik, J.; Ramamoorthi, R. Depth from combining defocus and correspondence using light-field cameras. In: Proceedings of IEEE International Conference on Computer Vision, 673–680, 2013.
- [22] Heber, S.; Pock, T. Shape from light field meets robust PCA. In: *Lecture Notes in Computer Science, Vol. 8694*. Fleet, D.; Pajdla, T.; Schiele, B.; Tuytelaars, T. Eds. Springer International Publishing, 751–767, 2014.
- [23] Boykov, Y.; Kolmogorov, V. An experimental comparison of min-cut/max-flow algorithms for energy minimization in vision. In: *Lecture Notes in Computer Science, Vol. 2134*. Figueiredo, M.; Zerubia, J.; Jain, A. K. Eds. Springer Berlin Heidelberg, 359–374, 2001.
- [24] Boykov, Y.; Veksler, O.; Zabih, R. Fast approximate energy minimization via graph cuts. *IEEE Transactions on Pattern Analysis and Machine Intelligence* Vol. 23, No. 11, 1222–1239, 2001.
- [25] Kolmogorov, V.; Zabih, R. What energy functions can be minimized via graph cuts? *IEEE Transactions on Pattern Analysis and Machine Intelligence* Vol. 26, No. 2, 147–159, 2004.



computer vision.



**Hao Zhu** received his B.E. degree from the School of Computer Science, Northwestern Polytechnic University, in 2014. He is now a Ph.D. candidate in the School of Computer Science, Northwestern Polytechnic University. His research interests include computational photography and

**Qing Wang** is a professor and Ph.D. tutor in the School of Computer Science, Northwestern Polytechnic University. He graduated from the Department of Mathematics, Peking University, in 1991. He then joined Northwestern Polytechnic University as a lecturer. In 1997 and 2000 he obtained his master and Ph.D. degrees from the Department of Computer Science and Engineering, Northwestern Polytechnic University, respectively. In 2006, he was recognized by the Outstanding Talent of the New Century Program by the Ministry of Education, China. He is a member of IEEE and ACM. He is also a senior member of the China Computer Federation (CCF).

He worked as a research assistant and research scientist in the Department of Electronic and Information Engineering, Hong Kong Polytechnic University, from 1999 to 2002. He also worked as a visiting scholar in the School of Information Engineering, University of Sydney, in 2003 and 2004. In 2009 and 2012, he visited the Human Computer Interaction Institute, Carnegie Mellon University, for six months, and the Department of Computer Science, University of Delaware, for one month, respectively.



Prof. Wang's research interests include computer vision and computational photography, including 3D structure and shape reconstruction, object detection, tracking and recognition in dynamic environments, and light field imaging and processing. He has published more than 100 papers in international journals and conferences.

**Open Access** The articles published in this journal are distributed under the terms of the Creative Commons Attribution 4.0 International License (<http://creativecommons.org/licenses/by/4.0/>), which permits

unrestricted use, distribution, and reproduction in any medium, provided you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons license, and indicate if changes were made.

Other papers from this open access journal are available free of charge from <http://www.springer.com/journal/41095>. To submit a manuscript, please go to <https://www.editorialmanager.com/cvmj>.