Numerical investigation of optimized piled raft foundation for high-rise building in Germany

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Abstract

Piled rafts have been used as a foundation system for high-rise buildings worldwide in different soil conditions, e.g., in soft to stiff clay as well as in medium-to-dense sand. Piled raft is currently used not only to control the foundation settlement but also to minimize the required raft thickness to reach the most optimized foundation design. The purpose of this study is to investigate the behavior of piled raft as a foundation system for Frankfurt over-consolidated clay based on the well-monitored Messeturm building in Germany. The numerical tool used in analysis is Plaxis 3D finite element software with hardening soil material model. The piled raft foundation behavior will be evaluated based on the total settlement, differential settlement and the pile skin friction. Based on this study, it was found that the chosen foundation system “plied raft foundation” for Messeturm was an optimized solution for the proposed building.

Keywords Piled raft foundation · Over-consolidated clay · Finite element method · Hardening soil model

Introduction

In general, when constructing a low-rise building on a bearing layer of soil, shallow foundations can be used, but if the building is a high-rise building and contains a number of basements, raft foundation is normally chosen to support the entire structure. But in case of weak subsoil, raft on piles foundation system is used to transfer the load to deep bearing layers, and in case of a building founded on deeply extended non-bearing layer, it is a waste and an uneconomical solution to use long piles to reach the bearing layer.

In this case, the piled raft foundation system is considered to be one of the most economic foundation systems for these projects which are in the zone between the raft (relatively cheap) foundation system and raft on piles (very rigid and expansive) foundation system.

Piled raft is a composite foundation system that combines the bearing capacity of both the raft and the piles together, and its behavior depends on the complex interaction between

pile–soil, pile–raft, raft–soil and pile–pile. The piled raft foundation may be a good alternative solution; one of the most benefits of piled raft foundation is that there is no need to satisfy geotechnical bearing capacity; only the structural capacity is required as mentioned by [1].

Piled raft coefficient (α_L) is defined as the ratio of load carried by the piles to the applied total load; when this coefficient is equal to zero, it is ideal raft foundation; when it is equal to 1, it is conventional raft carried by the piles. Moreover, we can define another important coefficient (α_S), coefficient of piled raft settlement reduction factor which is equal to settlement of piled raft to settlement of traditional raft; when it is equal to 1, it is a raft foundation, while when it is equal to zero, it is the conventional raft on piles. The piled raft foundation ranges between 0.0 and 1.0 for both coefficients (α_L and α_S) as shown in Fig. 1.

Previous investigations

Kawabata [3] used the boundary element method (BEM) to investigate the piled raft foundation without considering the slipping behavior between the piles and soil. Clancy et al. [4] used the finite element method (FEM) for modeling of the piled raft. The raft was presented by a 4-node quadrilateral plate bending element, and the piles

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Fig. 1 Piled raft principles [2]

were modeled as beam elements. He discussed the effect of meshing by using the reduced integration concept to improve the numerical results. Ta and Small [5] studied piled raft in a layered soil. The piles and soil were simulated by numerical method called finite layer to represent the piles in the layered soil. The load distribution along the piles in the layered soil is affected by layers relative thickness and stiffness.

El-Mossallamy [6] studied numerically the piled raft in over-consolidated clay using two well-monitored buildings in Frankfurt: Messeturm and Westend Buildings. His method of analysis is a mixed technique where the raft is modeled using FEM, while the piles are modeled by BEM. The optimum design was achieved when the piled raft coefficient is between 0.4 and 0.6. He found that the load taken by each single pile in the piled raft system depends on pile position, raft stiffness, on the configuration of the applied structural loads and on the load level.

Russo et al. [7] classified the piled rafts to small and large piled rafts. The settlement problem is mainly associated with large piled rafts as well as the differential settlement. They considered also the nonlinearity of piled raft system in their investigations. Prakoso and Kulhawy [8] used Plaxis finite element program but as 2D plain strain model. The pile dimension-to-raft width ratio has a big effect on both settlement and differential settlement.

De Sancits et al. [9] stated that the piled raft problem needs a 3D model to get an optimum design method, while 2D plain strain cannot be accurate enough. The bearing capacity block failure is accepted only when the width of pile group is the same as the raft width. Reul and Randolph et al. [10] used finite element program ABAQUS to study

the behavior of piled raft via 3 buildings: Messeturm, Westend and Torhaus. The maximum settlement by piled raft can be reduced to be 51–63% compared with the unpiled one. They found that the calculated piled raft coefficient by numerical analysis is higher than the measured values.

Mendonca et al. [11] used the mixed technique in which the interaction between piles–soil–raft is taken into account, and their results match well with the finite element method.

Reul [12] used the finite element method to model the piled raft in over-consolidated clay. He found that the reduced settlement can be achieved by using longer piles rather than using a higher number of piles. Navak et al. [13] investigated the load–settlement behavior using 3D finite element using two well-monitored buildings: Westend in Frankfurt clay and Urawa in Japan; both existed in over-consolidated clay. He compared the FEM with BEM. For the first building, the results are in good agreement. Balakumar [14] used ANSYS finite element program to study the performance of piled raft in sand. He found that the piles are fully mobilized without any failure observed. He found also that the piles load share decreases when settlement level also increases.

Oh et al. [15] used finite element (Plaxis) and finite difference (FLAC) methods to study the behavior of piled raft in sandy and clayey soil. They found that the maximum settlement depends mainly on the number of piles and the pile spacing. The differential settlement was reduced if the raft thickness increases. Sandeep et al. [16] stated that if the piled raft coefficient is initially high, then it decreases with stress increase; also, he stated that the differential settlement increases when Poisson's ratio increases.

Katzenbach et al. [17] presented a 3D finite element model to simulate piled raft in a layered soil; he stated that the load carried by the raft is increased by increasing the pile spacing. Omar El-Kadi [18] used finite element Midas GTS software to study the performance of piled raft using embedded pile concept to simulate the piles. He found that the embedded pile cannot be used to get the failure load and C-phi reduction technique cannot be used to predict the capacity of pile group as well as the piled raft precisely.

Elarabi [19] adopted the finite element program Plaxis 3D Foundation to investigate the applicability of piled raft in soft clay under undrained condition. He found that by increasing the pile spacing in case of piled raft will lead to a larger settlement. Amr [20] used DIANA finite element method to investigate the piled raft in Port Said soft clay using soil profile consisting of fill with thickness of about 1 m, followed by sand and silty sand with thickness of about 12 m underlain by a large extended Port Said soft clay; the foundation level is on the upper sand layer.

El-Wakil [21] used finite element method to simulate piled raft laboratory models; he concluded that by increasing the pile length, a better performance is obtained rather than by increasing number of the piles. S. Mil [22] used Plaxis 3D finite element program to investigate the behavior of piled raft in stiff clay. He found that by increasing the pile spacing-to-diameter ratio more than 6 will increase the settlement significantly as discussed in [23].

Verification of the numerical model

The verification of the presented numerical model will be compared via two cases; the first case is a simple single pile developed by Katzenbach [24, 25] as a conceptual verification, while the other case is Messeturm building, made by Sommer [26] and El-Mossallamy [6]. Both cases were

founded on over-consolidated Frankfurt clay, so it is important firstly to state the main properties of Frankfurt subsoil formation.

Frankfurt clay

Frankfurt subsoil consists of sand and gravel layers up to 10 m from the ground surface underlain by over-consolidated clay to a large depth, followed by limestone as shown in Fig. 2. Frankfurt clay was over-consolidated by land formation with a value of the previous vertical stresses ranging from 500 kPa to about 2500 kPa [27]. The properties of Frankfurt clay are shown in Table 1.

These results are based on different samples taken from the site of Main Tower building. For Frankfurt clay, El Mossallamy [6] reported that the difference between the short-term and long-term conditions is minor, and for a single pile, the effect is about 6.0% to 15.0%, while for piled raft case, the effect of consolidation may reach 30%.

Table 1 Average properties of Frankfurt clay and limestone [24, 25]

Properties	Units	Frankfurt clay	Frankfurt limestone
Angle of friction	Degrees	20	32.5
Cohesion	kPa	20	15
Uniaxial strength	MPa	0.28	84
Young's modulus	MPa	50	20,000
Coefficient of earth	–	0.6	0.5
<i>Pressure at rest</i>			
Unit weight of soil	kN/m ³	18.5	20
Buoyant unit weight	kN/m ³	y	10
Natural water content	%	34	–
Liquid limit	%	74	–
Consistency index	–	0.82	–

Fig. 2 Soil profile in Frankfurt City [24, 25]

Fig. 3 Single pile and raft dimensions [24]

Single pile

First numerical task has been done as a conceptual verification based on Katzenbach finite element work [24]. He studied a single pile embedded in Frankfurt clay numerically and compared the effect of the raft on the pile performance. The modeled pile was a bored pile of 30 m long with diameter 1.50 m. The dimension of circular raft was 12 m in diameter and has 1 m thickness (Fig. 3).

The computations were carried out using the finite element program Plaxis. A 2D-axisymmetric model with triangular (15 nodes) is used to examine the behavior of a free-standing pile and pile raft in clay soil under vertical axial loading conditions. An exemplary finite element mesh is shown in Fig. 4.

Close to the pile, a very fine discretization is used to ensure accurate results. The model dimensions of a width equal to 20 times the pile diameter or equal to 5 times the raft width and a depth equal to 2.5 times the pile length were chosen to ensure that the numerical results are not affected by the boundary conditions.

For the numerical modeling, a linear elastic material behavior for concrete was assumed with the parameters

Fig. 4 Finite element mesh for single pile and piled raft model

$E = 3.0 \cdot 10^4 \text{ MN/m}^2$ (Young's modulus) and $\nu = 0.25$ (Poisson's ratio).

To account for the nonlinear soil behavior, elasto-plastic material behavior was considered for the soil elements. A hardening soil material model was adopted for the numerical modeling.

This material model is considered as an advanced model for soil simulation, where the elastic deformation is represented by three input values instead of one value as in the case of the Mohr–Coulomb Model. The input moduli are the triaxial loading modulus (E_{50}) [Eq. (1)], the triaxial unloading modulus (E_{ur}) (Eq. (2)) and the oedometer modulus (E_{oed}). The difference between the input soil moduli is shown in Fig. 5.

$$E_{50} = E_{50}^{\text{ref}} \left(\frac{C' \cot \varphi' + \sigma'_3}{C' \cot \varphi' + p^{\text{ref}}} \right)^m \quad (1)$$

$$E_{ur} = E_{ur}^{\text{ref}} \left(\frac{C' \cot \varphi' + \sigma'_3}{C' \cot \varphi' + p^{\text{ref}}} \right)^m \quad (2)$$

where E_{50} =reference stiffness modulus at confining pressure (p^{ref}) 100 kPa; E_{ur} =reference unloading stiffness modulus at confining pressure (p^{ref}) 100 kPa; C' and φ' =effective shear parameters; m =factor which represents the stress level dependency of the stiffness; its value ranges between 0.4 and 1.0 according to the type of the soil.

The soil stiffness in this model depends on the stress level and on the stress path; moreover, it takes the unloading and reloading behavior of the soil into consideration. The yield surface is not fixed, but it can be expanded due to straining; moreover, the dilatancy can be cut off and the failure criterion is adapted according to the Mohr–Coulomb failure criterion.

Fig. 5 Relation between deformations moduli of hardening soil model and stress–strain relationship [30]

The model takes into account both shear and compression hardening [28, 29] (sometimes it is called a double hardening model); shear hardening occurs due to primary deviatoric loading, while compression hardening occurs due to isotropic loading and primary compression.

The hardening soil parameters used in analysis are listed in Table 2.

The numerical calculation is divided into several steps. In the first step, the initial stress state is generated by consideration of soil elements only. Afterward, the soil elements located at the pile position are removed and replaced by pile elements (wished in place), and the pile/raft own weight and contact conditions are activated. Finally, the prescribed settlements are applied on the top of pile or to the raft.

In Katzenbach study [24], each case was investigated under three different settlements. For the free-standing pile case, the three displacement values were 0.005D (7.5 mm), 0.01D (15 mm) and 0.1 D (150 mm), and the corresponding axial forces were 5.0, 8.0 and 13.0 MN, respectively. In the other case by connecting the raft to the same pile under the same settlement values, the values of loads transferred to the piles were 4.0, 6.0 and 12.0 MN, respectively.

From Fig. 6, the skin friction under small displacement is not fully mobilized and remains almost constant (37 kN/m² under 5 MN) along the depth; then, it increases gradually until it reaches its final mobilized value (linear distribution) under 13 MN.

For the second case, Fig. 7 shows the distribution of skin friction along the pile length. Under smaller loads (up to 6 MN), the skin friction increases linearly with the depth. Under the higher loads (12 MN), the peak of skin friction will be localized directly under the raft (up to 97 kN/m²) due to the high applied pressure.

Figures 8 and 9 show the verification of the numerical model done by the authors and the numerical study done by Katzenbach [24]. Figure 8 shows the comparison regarding the skin friction along the pile shaft for the free-standing

Table 2 Material parameters in the analysis [31]

Parameter	Name	Frankfurt clay	Unit
Type of material	Type	Drained	–
Soil unit weight above GWT	γ_{unsat}	20	kN/m ³
Soil unit weight below GWT	γ_{sat}	20	kN/m ³
Secant stiffness	E_{50}^{ref}	4.5×10^4	kN/m ²
Oedometer stiffness	$E_{\text{oed}}^{\text{ref}}$	4.5×10^4	kN/m ²
Unloading–reloading stiffness	E_{ur}^{ref}	9.0×10^4	kN/m ²
Poisson ratio	ν	0.3	–
Power	m	0.5	–
Cohesion	C	20	kN/m ²
Internal friction angle	φ	20	°
Lateral earth pressure coefficient	K_0	0.8	–

Fig. 6 Load–settlement curve; skin friction along pile shaft; free-standing pile [24, 25]

Fig. 7 Load–settlement curve; skin friction along the pile shaft; pile connected with raft [24, 25]

pile, while Fig. 9 shows the skin friction distribution for the piled raft case.

From Fig. 8, it is obvious that at the low-stress level (up to 7.50 mm), the skin friction is almost constant along the pile length. By increasing the prescribed settlement from 7.5 mm to 15 mm, the mobilized skin friction increases and reaches its maximum value at the pile tip. In the last stage, by increasing the pile settlement from 15 mm to 150 mm, a sufficient relative displacement between the pile and the soil will mobilize both cohesion and friction to its maximum value.

The effect of connecting raft to the pile is presented in Fig. 9. Under the prescribed settlement, the settlement caused by the raft reduces the relative displacement between the pile and the surrounding soil, especially in the upper domain near the raft application. For higher prescribed settlement, an additional deformation has been produced, and its value depends on the used constitutive laws, which is the reason for the massive skin friction in the upper part. In the lower part, the relative displacement decreases with depth.

There is a very good agreement between our results and the previous numerical results reported by Katzenbach, under small displacement up to 15 mm. But a relatively small deviation is observed especially for 150-mm settlement for the second case due to the higher contact stress under the raft compared with the same settlement in the free-standing pile due to raft contribution. Based on these results, the numerical model has been verified and can be adopted for further investigation cases.

Case study (Messturm)

Description

A building with 256 m height with two basements with the total area of 58.80 m × 58.80 m, has central core shaft in the middle with dimensions 41.0 m × 41.0 m and with height 210 m. The proposed foundation system is piled raft system with a thickness of 6 m in the middle which decreases linearly to 3 m at the edges. The raft is carried by 64 large

Fig. 8 Skin friction with depth in case of free-standing pile

Fig. 9 Skin friction with depth for a single pile connected with raft

diameter bored piles with 1.3 m diameter, and the pile lengths differ according to its position in the raft.

The bored piles are distributed in three rings; in the inner ring, the piles length is 34.90 m; in outer ring, the piles length is 26.90 m, and in the middle ring, the piles length is 30.90 m. The pile spacing varies from $3.5 \cdot D$ up to $6 \cdot D$ according to their position in the raft. The piles are concentrated mainly under the central core of the Messeturm to be near the heavy loads coming from the core to reduce the straining action in the raft and also to control the differential settlement.

The foundation level of the building is located 14 m below the ground surface; the total weight of the building is 1880.0 MN with average stress on the raft of 544.0 kPa, while the uplift force is about 276.0 MN. A simplified calculation approach was used for a preliminary design of the foundation system to calculate the raft size and pile distribution. The total pile loads were assumed to depend on the mobilized skin friction and carry 55% of the total load. The behavior of the foundation was monitored during the construction period and for more than 7 years after the finishing of construction by means of geodetic and geotechnical measurements using 12 instrumented piles, 13 contact pressure cells, one pore pressure cell and three multi-point borehole extensometers as shown in Fig. 10.

The results of the field measurements indicate that the load-bearing behavior of the Messeturm piled raft foundation has been optimized. However, the design concept assumed that the piles would reach their ultimate bearing capacity by the settlements caused by the structural load; thereafter, transferring any additional load increments to the raft could not be proved by field observations. The measured pile loads show that much higher skin friction has been mobilized than that determined for a single isolated bored pile.

Numerical model

The computations were carried out using the finite element program Plaxis 3D. A 3D-numerical model with 10-noded elements is developed to investigate the behavior of a piled raft foundation for Messeturm founded on Frankfurt clay and compared with numerical results developed by Sommer [26] and El-Mossallamy [6].

The finite element mesh is shown in Fig. 11. Close to the piles, a very fine discretization is used to ensure accurate results. The chosen model dimensions in x , y and z are 300.0, 300.0 and 90.0 m, respectively. These dimensions have been chosen to be large enough to minimize the effect of the model boundaries on the numerical results (see Fig. 11). Also, the model depth was taken the maximum of 2.5 times the length of piles or the depth were the increase in stresses of the building becomes smaller than 20% of the overburden pressure.

The boundary conditions were applied as follows:

1. The ground surface is free in all directions.
2. Vertical model boundaries with their normal in x -direction are fixed in x -direction and free in y - and z -direction.
3. Vertical model boundaries with their normal in y -direction are fixed in y -direction and free in x - and z -direction.
4. The model bottom boundary is fixed in all directions.

Fig. 10 Applied measurements on the foundation system of Messeturm [6]

Fig. 11 Finite element mesh

Due to Frankfurt clay nature as mentioned before, the clay was overloaded by heavy loads with average stress ranging between 500.0 and 2500.0 kPa, so the Over Consolidation Ratio (OCR) ranged over specific values and it was difficult to find out the exact value of OCR without performing a consolidation test.

There are many correlations, which relate OCR with several parameters, for example $K_{Ooc} = K_{onc}(OCR)^m$ reported by Meyerhof 1976 [32] where $m=0.5$, and the OCR for Frankfurt clay, in this case, is 1.50. For the presented study, several values of OCR will be investigated using values above and below 1.50 (see Table 3). Another technique for defining the over-consolidation pressure is adopted in the hardening soil model which is the pre-overburden pressure (POP) technique instead. The difference between both of them is illustrated in Fig. 12.

Table 3 The settlement and α_L (%) for different OCR values as well as POP

	OCR				POP
	1.25	1.50	1.75	2	700 kPa
Settlement (cm)	13.211	12.276	11.825	11.639	11.342
α_L (%)	57.1	56	55.2	54.4	54.6

For the raft, a linear elastic material model was adopted, and the model assumes a linear relationship between the stress and the strain. This material model needs two parameters: the modulus of elasticity (E) and Poisson ratio (ν). For the raft, $E=30,000$ MPa, $\nu=0.167$, while for piles, $E=22,000$ MPa, $\nu=0.20$.

The piles were modeled as “embedded elements.” In this case, the piles do not have a “real” volume or a “real” interface. However, a virtual elastic zone is created by assigning an equivalent pile diameter within the material data set of the embedded pile. This virtual elastic zone disregards the plastic behavior of the soil within the zone and approaches the actual volume pile behavior. On the other hand, due to the “virtual” volume and interface, evaluation of the effect of strength reduction factor (R_{inter}) cannot be realized. R_{inter} is taken as rigid (1.0) with the assumption that the interface does not have a reduced strength with respect to the strength in the surrounding soil.

The steps of the numerical model are summarized as follows:

Fig. 12 Difference between OCR and POP

1. Firstly, in-situ stress state or it is also called primary stress conditions is applied. In the step, only the own weight of the soil domain will be activated.
2. Then, the soil excavation up to a depth of 8 m below GL will be done. This was modeled by deactivation of the soil element from ground surface up to 8.0 m. Keep in mind that the excavation sides were kept in equilibrium by supporting them horizontally in x- or in y-direction.
3. In the third step, the installation of piles as embedded elements was done by activating the beam elements and the contact conditions along them in the three different rings (inner, middle and outer).
4. Consequently, a further excavation up to 14 m below ground level was done. This step is necessary in order to construct the concrete piled raft. Then, the own weight of the raft and the interface elements between the raft and subsoil have been activated taken into consideration the uplift water pressure. This means the own weight will be reduced by almost 60 kN/m^2 .
5. Finally, the vertical loading representing the own weight of the high-rise building is out on the upper surface of the raft.

Numerical results

Figure 13 shows the verification of the hardening soil model results with four different OCR values 1.25, 1.5, 1.75 and 2.0. The numerical results show that the curve with OCR value equal to 1.50 is nearest to the measured one, as the total settlement is about 12.27 cm compared with 12.0 cm measured value under the same vertical loading, but it is also shown that the effect of OCR value on the behavior is minor.

Fig. 13 Vertical stress–settlement curves for different OCR values

Table 3 summarizes the results of hardening soil model using the previous OCR values. When the OCR slightly increases, this will reduce the pile share (α_L) due to the increase in soil stiffness, which will increase the soil share, and consequently, the pile load coefficient (α_L) will be reduced from 57% to 54%.

In the case of using pre-overburden pressure (POP) of 700.0 kPa, the reached settlement in this case was 113 mm, which is near to the obtained value by OCR that is equal to 1.50.

Figure 14 shows the differential settlement between the center of raft and its edge as a function of the applied vertical stress on the raft. It can be noticed that for the three presented results (numerical molding of the authors, measured values and the results reported by El-Mosallamy [6]), the differential settlement increases with the applied vertical stress. Our numerical results show a good agreement, but it is slightly less than observed values;

Fig. 14 Vertical stress–differential settlement curves

this means that the numerical model for the piled raft has more stiffness than the reality.

Figure 15 shows the settlement contour after application of the total vertical load. Under the own weight of raft, the vertical settlement was almost constant with a maximum value of 2.4 cm, by applying the total vertical load on the raft, a higher increase in the vertical settlement of the piled raft system up to 12.0 cm (OCR = 1.50).

Figure 16 shows the skin friction distribution for a selective pile in the middle ring. The embedded pile element in Plaxis 3D gives directly the skin friction as force/unit length, and then, it can be transformed manually to skin friction along the pile length. The results in Fig. 16 show a good agreement with the previous results obtained by El-Mossallamy [6]; both of them show comparable distribution up to a depth of 20.0 m. The maximum skin friction was almost 130 kN/m^2 , which is comparable with the measured value of 140.0 kN/m^2 . This confirms the applicability of the numerical model to predict the behavior of piled raft in over-consolidated clay.

Conclusions

This article presents the results of numerical analysis of the piled raft foundation for over-consolidated clay using 3-D finite element analysis. Firstly, the numerical model has been verified by comparing our results with a previous numerical study reported by Katzenbach for free-standing pile and for

Fig. 16 Skin friction distribution along a pile in the middle ring ($L = 30.90 \text{ m}$)

a pile connected to circular raft. The comparison shows a very good agreement between the results under small loading conditions. But a relatively small deviation was observed for a higher vertical loading.

Then, a finite element model of Messeturm piled raft foundation was developed. The hardening soil material model is used to simulate the over-consolidated Frankfurt

Fig. 15 Settlement contour in cross section under total vertical load

clay; moreover, the embedded beam element concept was adopted for the piles as it is a quick tool to simulate piles under service load but not to predict precisely the ultimate pile load capacity. The numerical results show a good agreement with measurement made for the foundation for the “Messeturm” regarding the raft settlement and skin friction distribution along the piles.

Finally, this study indicates that piled raft foundation concept has significant advantages in comparison with conventional foundation systems and can be considered as optimized solution for high-rise building founded on over-consolidated clay.

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