Metal powder bed fusion process chains: an overview of modelling techniques

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Abstract

Metal powder bed fusion (MPBF) is not a standalone process, and other manufacturing technologies, such as heat treatment and surface finishing operations, are often required to achieve a high-quality component. To optimise each individual process for a given component, its progression through the full process chain must be considered and understood, which can be achieved through the use of validated models. This article aims to provide an overview of the various modelling techniques that can be utilised in the development of a digital twin for MPBF process chains, including methods for data transfer between physical and digital entities and uncertainty evaluation. An assessment of the current maturity of modelling techniques through the use of technology readiness levels is conducted to understand their maturity. Summary remarks highlighting the advantages and disadvantages in physics-based modelling techniques used in MPBF research domains (i.e. prediction of: powder distortion; temperature; material properties; distortion; residual stresses; as well as topology optimisation), post-processing (i.e. modelling of: machining; heat treatment; and surface engineering), and digital twins (i.e. simulation of manufacturing process chains; interoperability; and computational performance) are provided. Future perspectives for the challenges in these MPBF research domains are also discussed and summarised.

Keywords Metal powder bed fusion · Manufacturing process chains · Modelling and simulation

Abbreviations

AM	Additive manufacturing
CA	Cellular automata
CA-FD	Cellular automata finite difference
CAD	Computer-aided design
CAM	Compute aided manufacturing
EBPBF	Electron beam powder bed fusion
FE	Finite element
GUM	Guide to the expression of uncertainty in measurement
HT	Heat treatment

kMC	Kinetic Monte Carlo
LPBF	Laser powder bed fusion
LSP	Laser shock peening
MO	Machining operation
MPBF	Metal powder bed fusion
PDF	Probability density function
RVE	Representative volume element
SE	Surface engineering
SP	Shot peening
TRL	Technology readiness level
XCT	X-ray computed tomography

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1 Introduction

The capability of metal powder bed fusion (MPBF) to produce complex structural components in a wide range of materials has the potential to remove traditional manufacturing constraints from product design. This can enable greater product performance to be achieved through the creation of more functional shapes, the reduction of weight,

and the consolidation of multi-part assemblies into single components.

MPBF is not without its drawbacks where key challenges such as poor surface finish, uncertainty and standardisation in part quality and certification, high processing costs, and process variability must be overcome [1]. In many cases, existing technologies can be employed to do this, such as post-processing methods for improving material properties, and digital tools for planning and optimising operations. By linking all of these physical and digital components together, it is possible to create a “digital twin”, a digital replica of a physical asset, process, or system that uses associated real data streams to communicate with and optimise its physical counterpart [2, 3].

Digital twins have become increasingly common in the industry over the last decade, with prime examples being digital twins for asset monitoring [4, 5]. It will ultimately be desirable to create a digital twin of the entire MPBF process chain, whereby data is passed from one process simulation to the next, models are updated according to machine and inspection data from physical sensors, and components and production plans are updated and optimised accordingly via data analytics and artificial intelligence. This would enable designs and processes to be optimised for a particular part with less reliance on costly and time-consuming physical trials, increasing productivity and reducing the barriers to new product introduction [3]. Work on digital twins in additive manufacturing has shown conceptual developments that can be the basis to deliver industrial impact [6–9], however, further work in the development of digital twins would help to fully realise all of the benefits of additive manufacturing in the industrial production environments while maximising productivity and cost-efficiency.

This paper reviews the state of the art for modelling the physics of manufacturing processes involved in MPBF process chains, with a view to support the realisation of future digital twins. Areas of focus are the process models themselves and methods for passing data between simulations according to the physical process chain, as well as how this affects confidence in the results of the models and the propagation of uncertainty. This allows the maturity of the various modelling methods and data transfer technologies to be assessed through the use of Technology Readiness Levels (TRLs) so that roadmaps of their predicted development can be generated in the near future.

2 Digital twin and process chain concepts in MPBF

2.1 Overview of a digital twin concept

A digital twin can be described as an organised collection of physics-based methods and advanced analytics that is used to model the present state of every asset [3, 10]. By additionally considering the data streams of these assets and communicating with them, it can be considered as a digital counterpart to physical reality. Wherever a physical tool services a need (for example moving people from one place to another, electricity provision, manufacturing a product, etc.), a virtual counterpart can be created to plan, optimise, and control it. For MBPF, a process chain digital twin would provide accurate predictions of component properties, greatly reducing the amount of trial-and-error physical experimentation that is required when developing new parts.

To describe the role of the simulation models in a digital twin, Fig. 1 shows an example of a digital twin concept for product and process development in MPBF. Alongside the digital twin is the physical environment, as well as middleware that facilitates connectivity and the transfer and storage of data, information, and knowledge. This can all be accessed by people with the necessary knowledge to act upon it, for example by deciding the next step of the product and process development. Information from the digital twin could also be used to inform other decisions, such as optimising the layout of a facility and production schedules, developing cost models, or adapting the post-processing route to help combat the variable nature of MBPF production.

The first step in the development of a product is the design work, which can include simulation and other analyses to optimise design performance. Once an initial design has been created, the product undergoes design for manufacture. This includes simulating the manufacturing process chain to determine the geometric and material changes that will arise when the material is subject to mechanical and/or thermal energy inputs. The steps shown in Fig. 1 include an additive manufacturing (AM) build process, followed by heat treatment (HT), machining operations (MO), and surface engineering (SE). The simulation of this chain can generate useful knowledge for product and process development, such as the optimal parameters for a particular process and potential regions of risk in the design geometry. Following this, the part performance analyses can be conducted again to assess the impact of any geometry and material changes that may arise during manufacture.

Once there is sufficient confidence that the design meets the requirements for functionality and performance, physical manufacturing trials can be executed. The test parts may be

Fig. 1 An example of a digital twin for product and process development

inspected for dimensional accuracy, surface quality, material characteristics, and internal defects at each stage of the manufacturing process, and this data is passed back to the simulations so that they can be updated, validated, and identify solutions to any potential problems that may arise during manufacture. The relevant experts then decide whether more improvements or iterations are needed and where such changes are required. An example problem could be an excessive distortion of the part in some locations, which could be addressed through further stiffening of the geometry in that area or by applying distortion compensation based on inspection or simulation results [11–13].

The final step is physical testing of the MPBF parts using test rigs representing in-service conditions. Further development iterations may be needed if the functionality of the parts does not meet the requirements or if further quality improvements or cost reductions can be achieved. Once the designed MPBF parts and the associated processes have been developed, inspected and tested, the designs can be prototyped and further progressed for production.

The presented example shows that physics-based modelling and simulation could potentially provide more benefits in the process and product development stage if they are integrated in a digital twin.

2.2 Overview of process chain simulation concept

Physics-based simulation is typically used in design and manufacture to reduce the need for costly experimental work, for example by examining variables in a manufacturing process or a test that the final product will undergo. These simulations typically require material properties that

are heavily dependent on temperature and strain rate, as well as they can undergo phase changes during use. For instance, physics-based simulations have been applied to manufacturing processes, such as: forming and forging [14–18], casting [19–21], welding [22–24], metal cutting [25–27], non-conventional machining [28, 29], additive manufacturing [30–33], shot-peening [34, 35] and heat treatment [36–38]. A new vision, in which micro-structural simulations, multi-scale process and material models, and manufacturing process chain simulations can be integrated into a single workflow, would enable material properties to be predicted and propagated from simulation to simulation.

Figure 2 shows a suggested manufacturing process chain simulation workflow. The vertical direction shows a multi-scale materials computational approach, the objective of which is to (i) predict the microscale mechanical fields characterising the mesoscale based on local microstructure information and (ii) derive the component-level properties from the mesoscale behaviour. Challenges in this direction include the development of efficient and accurate macroscale continuum models that implicitly simulate the influence of process-induced microstructure variations on the process, and characterisation and classification of micro-structural simulation outputs into multi-scale models representing material behaviour. This needs to be accomplished without significantly compromising accuracy and also needs to be capable of coping with numerical discontinuities, so that the multi-scale build models can be used to inform subsequent process models.

The challenges in the horizontal direction regard data transfer between different micro-structural simulations, material models, and process simulations. This must be

Fig. 2 MPBF process chain simulation concept

accomplished to predict the micro-structural defects, residual stresses, geometric distortion, fatigue life, and mechanical properties of parts passing through the process chain.

The simulation workflow shown in Fig. 2 aims to reduce the amount of physical testing required to obtain the material properties that are necessary for manufacturing process simulations. Although doing so would not completely replace the need for obtaining physical material property data, building on the results of process-specific micro-scale models should enable more effective simulation of emerging materials and applications.

3 Laser powder bed fusion (LPBF)

The multiscale nature of the LPBF process means that behaviour over a range of length and time scales needs to be addressed if an entire process chain is to be realised. At the lowest level, interactions between the heat source and the powder particles are fundamental in the development of the melt-pool and resulting thermal fields. The solidified microstructures are composed of grains (of the order of tens of microns), fine precipitates (of a few nanometres) and voids (ranging from nanometres to microns in size). These factors will then influence the mechanical response of the material at the mesoscale, characterised as length scales of $\sim 100 \mu\text{m}$. In general, the resulting micromechanical fields will be non-uniform at these length scales.

3.1 Micro and meso scale models

Physical modelling of the powder melting process is extremely challenging. To arrive at accurate results, a representative statistical distribution of the powder particles within the layer of interest must first be obtained. Powder size distribution impacts the packing density of the powder bed which has been linked with the formation of

Fig. 3 Packing density (f) reaches a maximum (f^*) when the particle size distribution includes a mixture of small (s) and large (L) particles. Image sourced from [40]

lack-of-fusion voids [39]. The relationship between the powder size distribution and the packing density is shown in Fig. 3.

One method used for generating a powder bed is the rain model [41], whereby a falling particle searches for a local minimum in potential energy. The falling particle rotates as necessary when coming into contact with another particle, ultimately either settling in place at the local minimum or falling until reaching the global minimum. Variations of this method have been employed by a range of authors [42–44] to generate distinct powder packing characteristics based on experimentally measured particle size distributions. An alternate technique is the use of the discrete element method to simulate the raking of powder particles into position on the bed [45–48]. In this approach, the motion of the individual particles and their effects on one another are computed by considering the various forces that act on each particle, such as friction and gravity. Most of these approaches currently consider spherical particles.

In addition to the powder bed, the laser beam power, point distance, and scan speed all have significant impacts on the melt-pool dynamics, spatter pattern, and sublimation of particles, and therefore the resulting porosity and surface roughness of the part [49]. The heat source can be described using a variety of techniques, such as Gaussian expressions [50, 51] or ray tracing that describes the absorption and reflection of the laser by the powder and substrate [52].

One of the main purposes of meso-scale modelling is to predict porosity and the cooling rates that dictate microstructural evolution, and thus component properties. The meso-scale describes phase transitions during laser melting, capturing the molten pool dynamics as a function of the powder, process parameters, and material [43].

The melting and solidification are achieved by scanning a laser beam over a randomly distributed powder bed, which in turn is situated over a preplaced powder layer or previously solidified powder layer in a multilayer scanning strategy. The development of porosity has been correlated experimentally with both top sample surface structures and the melt pool and flow behaviour [53], and this behaviour has been further explained through numerical modelling [54]. Recent experimental analysis into the transient dynamics of powder spattering in LPBF has provided information on the various powder melting stages that dictate local flow dynamics as well as the effect of environmental pressure on spatter [55].

Given the stochastic nature of the process being simulated, confidence in the output of powder melting models may be improved through running multiple simulations with different powder bed morphologies. Doing so enables the construction of probabilistic functions, for example of porosity against energy density, layer thickness, and beam scanning speeds. The output of these meso-scale models is a thermal history that can be used for the calculation of microstructure evolution and the prediction of effective material properties. In particular, homogenisation of microscale fields defined within a representative volume element (RVE) or unit cell provides a method for calculating the mechanical and thermal properties of an additively manufactured material [56]. The advantage of such simulations is that details of the process-induced microstructure are explicitly accounted for. Such methods also enable the exploration of the sensitivity of the effective properties to the presence of voids and unmelted particulates [57], ensuring that the effects of variable build quality can be considered at component level. For an additively manufactured material, it is likely properties would be orthotropic or anisotropic [58, 59] since build direction will potentially have an effect on properties. For a material with some random factors in its microstructure, such as porosity or grain orientation, many randomly generated RVEs should be analysed to capture the statistical variability correctly, leading to a corresponding statistical description of the component level properties.

Many parts have elaborated internal geometry with cellular, lattice or beam structures providing high performance to weight ratio, and homogenisation methods can evaluate the effective properties of these substructures to simplify simulations at component level [60, 61]. Homogenization methods have also been used in conjunction with topology optimisation methods to define effective properties for topological designs created using density-based methods [62]. Some software vendors are already building RVE-type tools into their engineering simulation packages to facilitate the use of these approaches. Other homogenisation methods are limited to regular or nearly periodic geometries, but they can be useful for porous materials with medium to low porosity levels and widely separated pores. The simplest of these is Maxwell's method [63] which can be used to calculate effective mechanical and thermal properties for materials with spheroidal pores and inclusions.

Microstructural evolution models can be grouped into interface tracking methods (such as phase field and level-set) [64–67], cellular automata (CA) [68, 69] and kinetic Monte Carlo (kMC) [70]. The interface tracking methods have shown a realistic modelling of dendritic structures while accounting for the solute segregation, however the higher computational requirements often limit the application over a large number of grain-aggregates. On the other side, kMC based on the Potts model captures the general characteristics of solidification of grains over a large number of grain aggregates, however, it cannot predict the range of solidification structures observed during LPBF such as cellular and dendritic domains. The CA methods based on finite element or finite difference schemes provide a half-way solution between interface tracking and kMC methods. They can deal with a range of computational domain sizes and are able to simulate cellular, dendritic and large-scale grain structures. The CA-FD (cellular automata finite difference) approach has recently been extended by Panwisawas et al. [43] to take into account local curvature effects as well as strain energy contributions and mass transport.

Despite these advances, it is still a challenge to numerically model the complexity of the LPBF over multiple scales. This challenge is increased by statistical variation and a lack of material data in the literature. The accurate prediction of surface roughness, mechanical and physical properties, fatigue life, melt-pool dynamics, and porosity remains a distant goal.

3.2 Component scale models

At present, macro-scale models tend to be based on empirical data (commonly using an eigenstrain formulation) and as such are relatively computationally efficient and have been demonstrated to be effective in simulating trends for the development of residual stresses and topological

deformations accompanying the LPBF process [71]. However, such models do not explicitly consider the powder particles and their interactions with the heat source, and neglect the important meso-micro scale fluid dynamics [72]. The biggest challenge in modelling the build of an entire component at the micro and meso scales is excessive computational time, which arises due to the large number of finite elements needed to represent the additive layers. To reduce computational time, some researchers have adopted the “classical welding” approach for modelling the melt pool and assume that the powder can be modelled as a continuous solid. Although this is a significant simplification, such models can produce representative results after calibration against measured data [73]. Even with this assumption, the classical welding approach still requires large computational times unless additional approaches are utilised. For example, dynamic adaptive meshing techniques to maintain mesh refinement around the heat source while coarsening it elsewhere have been used [74, 75]. This technique requires temperature data to be mapped between dissimilar meshes, introducing further computational effort and sources of error.

Analytical formulations have been used to predict the thermal history of a moving laser [76]. Similar approaches have been used in modelling the welding process [77]. The method is extremely fast and can deliver quick solutions, meaning it has the potential to be used at the component scale. The disadvantages are that it cannot consider temperature-dependent thermal properties and lacks the ability to incorporate realistic boundary conditions. Since the heat source beam is very small compared to the component and surrounding powder, the analytical thermal model is similar to conduction in an infinite body. Terry et al. [78] demonstrated that the use of an analytical thermal model to predict temperature evolution in an industrial impeller is feasible for both single and multiple laser systems. Figure 4

is sourced from this work, and it shows the predicted temperature at the top three layers of an impeller made of In718. The computational time required to provide this prediction was reported to be less than a minute. Terry et al. [78] also demonstrated the integration of a machine toolpath generated by a Computer-Aided Manufacturing (CAM) system into their model.

Another challenge in modelling the melt pool at the component scale is the selection of an appropriate heat source model (surface or volumetric heat source). It is well known in welding modelling that volumetric heat source models more realistically represent the melt pool generated by laser melting. Surface heat sources, such as a 2D Gaussian heat source, lack the ability to quickly transfer energy into the material, which results in shallower melt pools. A common technique used in welding is to calibrate the heat source model to match the melt pool dimensions [79]. This suggests that a calibration step is essential to gain confidence in LPBF models thermal models.

At the component scale, temperature predictions are vital for simulating the thermal expansion and the generation of thermal stresses and distortion. Due to the aforementioned challenges in calculating temperature, predicting the residual stresses and distortion using conventional coupled thermo-mechanical approaches has proven to be challenging. This has led to the development of different techniques for predicting mechanical behaviour. For example, researchers have assumed that a number of layers can be lumped together and assigned a given temperature, before being allowed to cool [80]. Other researchers applied a heat flux based on the energy equilibrium, rather than an initial temperature [81]. In both approaches, the prescribed temperature field does not represent the actual temperature during the process. Analytical temperature fields have also been used to induce thermal strains and stresses [11, 82]. This methodology has been validated using a radially and vertically varying temperature

Fig. 4 Prediction of thermal history of IN718 impeller using a multi-layer analytical thermal model integrated with a gCode reader [78]

Fig. 5 Comparison of calculated surface deviations obtained using various fast predictive methods and experimentally measured data, all aligned to the nominal geometry using the same alignment method [83]. Units in mm

field [82, 83]. Other researchers have adopted the inherent strain approach [83–85], which treats the residual strains in the material as a source for calculating the residual stresses with Hooke’s law. In the finite element model, the plastic strains represent the residual strains. Some researchers have therefore solved the thermo-mechanical problem at the micro scale to predict the plastic strains, before imposing them in a component scale model. It is typically assumed that the strains are uniformly distributed in a single layer. While the inherent strain method is usually based on the theory of elasticity, some researchers have found that considering plasticity improves distortion predictions [83].

Figure 5 shows a comparison of fast methods for predicting distortion in LPBF [83]. It can be seen that the accuracy depends on the selected method. The inherent strain method using elastic plastic material properties shows the most accurate prediction of distortion distribution and magnitude of an impeller made of In718. The difference of the maximum predicted and measured surface deviation in the buckled blade was approximately 11%. Such predictions can be used to assess the likelihood of build failures due to recoater collision or support failures, and can also help with selecting appropriate support strategies. Distortion predictions can also be inverted and used to pre-distort the initial geometry, so that the built part distorts into the correct shape, rather than out of it. This concept has been demonstrated to be feasible and implementable on industrial parts [11, 86]. The main challenge is the requirement for an accurate initial distortion prediction; however, it has been demonstrated that pre-distorting the geometry using experimentally measured data from a test component can deliver distortion compensation of approximately 75% using one

Fig. 6 The effect of compensation on the distortion of two otherwise identical experimental In718 Impellers [12]. The surface deviation vs. nominal geometry is plotted and was measured using a structured light scanner. Dimensions in mm

iteration for an impeller and a blade [12], and a manifold [13]. Figure 6 shows an example of a distortion compensation of an impeller where the distortion was reduced from approximately $\pm 300 \mu\text{m}$ to approximately $\pm 65 \mu\text{m}$.

Modelling residual stress at the component scale is another challenge. Most of the validations of LPBF models are based on distortion comparisons, although there are a number of studies comparing predicted and experimentally measured residual stresses. For example, Yaghi et al. [83] compared residual stresses obtained with fast finite element predictive methods against experimentally measured stresses obtained by the neutron diffraction method for a component made of In718 as shown in Fig. 7. The fast-predictive methods were: (i) inherent strain method with elastics material model; (ii) inherent strain method with elastic–plastic material model; and (iii) analytical thermal field using temperature dependant elastic–plastic material properties [11]. It can be seen that the three methods capture the overall behaviour of the residual stress distribution (tensile at the surface and compressive inside). The analytical temperature field method predicted the residual stresses most closely to the experimentally measured results where the difference of predicted and measured peak compressive stress was approximately 9.5%. Also, Yaghi et al. [87] compared predicted stainless steel 316 residual stresses against data that was obtained using the contour and hole drilling methods. A comparison between the contour and finite element methods are shown

Fig. 7 Comparison of FE and experimentally predicted stresses for In718 [83]

Fig. 8 Comparison of FE and experimentally predicted residual stresses for stainless steel 316 [87]

in Fig. 8. It was reported that the FE predicted and experimentally measured residual stresses demonstrate reasonable agreement except at the bottom right corner, where the predicted stresses are lower. This could be due to the fact that the predicted residuals stresses from the process models are based on a 3D geometrically circumferential model of the impeller, whereas the calculated stresses in the contour method are based on distortion measurement of a cross section applied into a plane strain FE model to calculate the residual stresses using the Hooke's law [87].

4 Electron beam powder bed fusion (EBPBF)

Similar approaches to modelling LPBF are often used in the modelling of EBPBF, with considerations given to the different physics of the two process. In EBPBF, the primary energy source for powder melting is the kinetic energy of electrons travelling at around 0.1–0.4 times the

speed of light [88]. Upon collision with a powder particle, some of this kinetic energy is converted to heat. With a sufficient number of collisions, the heat generated is easily capable of melting the metal.

A recent review of EBPBF modelling techniques highlighted three main approaches for modelling the EBPBF process [88]:

- Uncoupled thermal models, which simplify the physics and reduce the computational resources required by only considering the main heat transfer phenomena. These consist of conduction between the powder particles, conduction between the powder bed and substrate, and radiation from the powder into the chamber. Heat dissipated by viscous forces and convection in the melt pool are ignored [89, 90].
- Thermal-fluid models, which include the effects of flow convection on the temperature distributions and melt pool geometry [91, 92].

- Thermomechanical models, which incorporate mechanical properties to predict the residual stresses induced in the material by the EBPBF process. This results in more informative models at the cost of longer run times [93].

Models can also be split according to how they treat the powder; some consider individual powder particles, while others treat the powder as a continuum. Examples of thermal-fluid models include using a lattice Boltzmann approach to model the melting of a randomly generated powder bed with an electron beam [94]. Different approaches are used in the modelling of the heat source as well, for example simulating the impact of electrons on the powder bed using a Monte Carlo method to predict the heat flux distribution across the beam diameter [90].

At the component scale, EBPBF models also need to consider the effect of the semi-sintered powder on the stress and distortion of the part, as this can affect the heat transfer from a component as well as the mechanical loads on it. A compact model of the EBPBF processes to predict shrinkage was developed in [95]. The model assumes that the thermal stresses can be neglected because they are low due to the elevated temperature in the build machine, and that the creep rates at temperatures above 1000 °C are significant, leading to quick stress relief of the parts. Considering this assumption, the EBPBF process model can be simplified by assuming an initial temperature of the part equivalent to the temperature in the build machine and allowing it to cool down to room temperature using natural convection. Figure 9 shows a comparison between experimental and predicted distortion for Ti64 part produced on the Arcam Q20 [96]. The results show a very similar distribution between predicted and measured distortion by comparing the surface deviations. It was reported that the maximum surface deviations were less than 8% between predicted and measured

surface deviations. It needs to be noted that creep deformations due to gravity loads have not been modelled. However, the proposed model showed that it can predict the overall distortion and it can be used for distortion compensation instead of using global or Cartesian scaling factors.

5 Topology optimisation models

The topology optimisation can be tracked back to over a hundred years ago where criteria for least-weighted layout of trusses was developed. In the seventies, analytical solutions were developed for grid-type structures. With the emergence of the finite element method, the topology optimisation started its rapid development along with the development of computational capabilities. The following methods emerged since then, including in chronological order: density-based methods, evolutionary procedures, bubble method, topological derivative, level-set methods and phase field methods [97, 98]. Those methods have been incorporated in commercial finite element solvers to tackle structural topology optimisations, particularly light weighting of structures. Choe et al. [99] benchmarked commercially available software and the results showed that the topology optimisation methods subject to mechanical loads are mature enough to be applied to industrial designs. Dbouk [100] reviewed the research work conducted in the last 20 years in the topology optimisation of heat transfer and fluid flow systems. They concluded that despite the advanced developments and advanced work in the field, the topology optimisation is not a robust numerical design technique for finding optimal designs of thermal systems. Therefore, further work is required to mature and validated the numerical techniques before they are adopted in industry. Topology optimisation methods have been applied in electro-magnetisms, but those

Fig. 9 Comparison of experimental data with FE predictions for EBPBF shrinkage of a Ti64 component [95]

methods have not been widely adopted in industry despite the promising results published in the literature [101]. Computation fluid dynamics methods using gradient-based algorithms, stochastic algorithms and metamodeling have been applied to aerodynamics shape optimisation applications [102].

Topology optimisation algorithms that consider manufacturing constraints have been developed for minimum member size, minimum hole size, symmetry, pattern repetition, casting, milling, turning, forging, extrusion and rolling [103]. The inclusion of manufacturing constraints modifies the solution resulting in greater material volume/mass for the design. In additive manufacturing, particularly powder bed technologies, supports are used for build angles lower than 45° . The implementation of overhang-free topological designs has been demonstrated for different topology optimisation methods [104]. For additive manufacturing design application, where the use of supports is unavoidable for some geometries, topology optimisation methods can be used to generate the supports. For example, a validated process model for a build simulation was used to predict the forces acting at the overhang structures in [95] based on the model presented in [11] where the support structures are modelled with spring elements to represent the stiffness of the support structures in the three directions of the Cartesian coordinate system. The predicted forces were then applied to a topology optimisation model to obtain the support structures (see Fig. 10). It was found that the topology optimised supports were 50% lighter than conventionally generated supports using commercially available tools [95].

Additive manufacturing induces material anisotropy which is unavoidable despite the efforts made to be reduced. The material anisotropy constraint has been implemented by the implemented anisotropic constitutive material model in

the finite element solution or by changing the plasticity criteria [104]. Furthermore, topology optimisation techniques for multi-materials, microstructure control and lattices have been reviewed and presented as future development opportunities towards their maturation [104, 105].

In additive manufacturing process chains, post-processing steps (heat treatment, surface finishing, surface hardening, and inspection techniques) can be required to deliver the functional requirements of designs. Therefore, considering topology optimisation for additive manufacturing process chains can introduce further complexity due to an increased number of manufacturing constraints. To the best knowledge of the authors, the inclusion of manufacturing constraints considering the full additive manufacturing process chain has not been addressed by the research community which presents an opportunity for future research.

6 Post-processing operations

6.1 Heat treatment

Heat treatment is an important step for most MPBF components, and it can deliver improved performance through aging and residual stress relief. The latter is typically conducted for a relatively short period of time (i.e. a couple of hours, depending on the material and thermal mass of the part). Depending on the material performance that needs to be achieved (for example large grains for better creep performance or fine grains for better fatigue performance), the aging time can be significantly greater.

Modelling both processes requires the prediction of the thermal history in the furnace. Many furnaces operate under a vacuum, meaning heat is primarily transferred from the heating elements to the parts through radiation. Reflection at the part needs to be considered when modelling this radiation, which can be accomplished using view factor calculations [38]. These models can accurately predict the thermal history of the parts, and can therefore provide practical benefits. These include optimising the power in the heating elements to control thermal gradients, or identifying how to position the parts in the furnace to avoid shading and cold spots [106]. The predicted thermal history can also be used to calculate the evolution of the microstructure and support the development of the most appropriate thermal cycle [36]. One of the challenges in this type of modelling is determining the surface emissivity, which depends on the surface oxidation and surface roughness. The emissivity can vary over a wide range, suggesting that validation using experimentally measured temperatures should be used to gain confidence in the values used [107].

Post-build stress relief modelling requires the thermal history from the heat treatment process and residual

Fig. 10 Topology optimised supports based on predicted forces from a process model [95]

stresses in the component from the MBPF build process. Stress relief or relaxation is typically simulated with a creep model, which is generally empirical and describes the material response to temperature and stress as a time-dependent process. Creep models are based on material data gathered from tests conducted at either constant load/stress or constant elongation/strain. The strain rates for each of the creep tests at constant stress are obtained at the secondary creep region.

There is limited creep data for materials manufactured using powder bed fusion in the literature. What is available is often for different temperatures than those of the stress relief thermal cycle used for additive manufacturing. For example, Read et al. [108] conducted creep tests at constant stress for AlSi10Mg at 180 °C, while the typical stress relief thermal cycle for AlSi10Mg is heating up to 300 °C, holding for 2 h and cooling down to room temperature.

The Norton creep law is commonly used to simulate stress relaxation. O'Brien et al. [109] conducted a study where the Norton creep constants for In718 at 980 °C were obtained using a reverse engineering approach. The manufacture of a cantilever beam specimen that was built on a Renishaw AM250 and heat treated (by heating to 980 °C, holding for 2.5 h at 980 °C, and cooling down to room temperature) was simulated using a validated LPBF build model and the Norton creep law approach. Figure 11 compares measurements from the physical parts with simulated distortion predictions for both the as-built and stress relieved parts, demonstrating the validity of the Norton creep law approach for simulating stress relief. O'Brien et al. [109] reported that the maximum measured and predicted vertical distortions after cutting

the double cantilever beam from the baseplate after LPBF were between 0.84 mm and 0.87 mm respectively, which is less than 4% difference. They also reported that the vertical displacements were less than 0.04 mm for both the predicted and measured vertical displacements after the stress relief step.

6.2 Machining operations

A disadvantage of powder bed fusion technologies is an inability to produce quality surface finishes without further processing, particularly on overhanging structures [110]. The typical average surface roughness (Ra) for LPBF is in the vicinity of 20 µm, depending on the material, laser system, powder characteristics, and build angle [110, 111]. Yaghi et al. [87] conducted milling on an LPBF manufactured stainless steel 316 impeller to demonstrate the improved surface finish that can be achieved. Milling can also induce compressive residual stresses at the surface, which can be beneficial for fatigue life [112]. Grinding is another process that can be employed for improving the surface finish and surface integrity [113].

The modelling of conventional material removal processes is typically done by deactivating elements of the finite element stiffness matrix [27, 114]. The element deactivation technique does not take into account the effect of the tool-workpiece interaction on the surface stresses, meaning potential contributions to residual stress, distortion, and component fatigue life are neglected. Yaghi et al. [87] consider the surface stresses in their work by combining the bulk material removal process and the tool-workpiece interaction. This was achieved by imposing surface stresses obtained from experimental measurements, although

Fig. 11 Results from a study comparing measured and predicted vertical distortion for an as-built and stress relieved cantilever beam for In718 [109]

simulation-based surfaces stresses could also be imposed if desired.

Conventional machining processes can only be conducted once a build is complete, and it can therefore only be applied to external surfaces and any internal features that can be accessed by the machine tools. Given the complex geometries powder bed fusion permits, conventional machining processes may not be capable of providing a quality surface finish on all surfaces of an AM part. Hybrid LPBF combined with micro-milling can overcome this limitation by machining the internal and external surfaces as the layers are built up. Little research has been conducted into modelling hybrid LPBF and micro-milling. Afazov et al. [115] used the inherent strain approach for modelling LPBF and further developed the inclusion of the micro-milling process. The material removal process was modelled by deactivating elements from the stiffness matrix, in a similar fashion to the modelling of conventional machining. A comparison of predicted and experimental distortion for a hybrid LPBF component is shown in Fig. 12 where it can be seen that the predicted and experimentally measured distortion have similar overall distribution. In addition, the peak distortion deviations have the same location and pattern. The authors used the model to optimise a nozzle design by incorporating two additional applied stiffeners at the outlet where the distortion was alleviated by approximately 60% at the bottom of

the nozzle, with the entire nozzle being within the application specified tolerance of ± 0.2 mm.

6.3 Surface engineering

Treating the surface of LPBF parts is essential for improving the surface finish and/or surface integrity. A high-quality surface finish (with low surface roughness) improves the fatigue life [116], while surface treatment can also be used to improve surface functionality by creating an appropriate surface texture [117]. The most widely used technologies for improving the surface quality of LPBF parts are sand blasting, laser polishing, finishing and mass finishing. Fatigue life improvements can also be achieved by applying surface hardening processes, such as shot-peening and laser shock peening.

The numerical modelling of some of the surface engineering processes can be challenging, and it may require the use of alternative analytical solutions. For example, the modelling of sand blasting can be very computationally expensive, since there is a need to calculate multiple particle impacts over large surfaces. Developing a material model capable of accurately capturing the abrasive phenomena involved in sand blasting is another challenge [118]. Finishing and mass finishing processes present similar challenges, and so analytical and empirical solutions are often utilised for prediction and optimisation purposes [119].

Laser polishing can be numerically modelled by applying a volumetric heat source that produces the required melt pool shape [120]. This type of model can predict temperature distribution and residual stresses, however, the prediction of surface roughness after melting can be very challenging. The surface roughness is therefore typically predicted using empirical equations, which can be developed using techniques such as regression or artificial neural networks [118]. Regression functions have also been utilised in mass finishing for the prediction of surface roughness [121].

Shot-peening has been modelled at the micro scale, including the impact of a number of shots on a small surface. This type of modelling can give an understanding of the effect of ball diameter, momentum, impact angle, and surface coverage on the induced residual stresses. The main challenge in modelling shot-peening is developing a material model to account for the cyclic hardening caused by multiple shot impacts. Previous reviews of these models have shown that the combined use of kinematic and isotropic hardening can produce good predictions [35]. Unfortunately, micro scale modelling cannot be applied at the component scale due to the large computational requirements that would arise. To overcome this, micro-to-macro mathematical models have been developed to map residual stress profiles to the component level [122]. The mapping techniques have been successfully applied to aerospace components [123].

Fig. 12 Modelling of hybrid LPBF for a stainless steel 316 component. The figure shows a comparison of experimentally measured surface deviation from the nominal geometry and that predicted numerically [115]. Units in mm

In a similar fashion to modelling shot-peening, laser shock peening modelling is conducted at the micro scale. The laser shockwave is represented by a moving pressure distribution that follows the toolpath of the laser. The pressure distribution is calculated from the laser pulse and the laser power using empirical methods. Laser shock peening is very quick, with the laser pulse for a single shock usually less than 100 ns. This requires the use of strain rate-dependent models such as the Johnson–Cook model and an explicit dynamic finite element solver [124]. The challenge in laser shock peening is obtaining the residual stresses after the explicit dynamic simulation. The stresses oscillate after each shock and cannot reach equilibrium, despite the use of infinite elements that have been used in the modelling of shot-peening to minimise the dilatational and shear wave energy reflected back into the finite element mesh. The use of the inherent strain approach has proven that the modelling of laser shock peening is possible [125]. This approach consists of a dynamic model predicting the plastic strains induced by the laser shockwaves. The plastic strains are then used as inherent strains in an implicit finite element solver to predict the residual stresses. Figure 13 shows a comparison between predicted and measured residual stresses for In718, which can then be mapped to the component level using a micro-to-macro scale mathematical model using the formulations from [122]. The results show that the model can predict peaks of the residual stresses while the experimentally measured residual stresses represent an average representation of the area. Therefore, it is difficult to quantify the accuracy of the model.

6.4 Inspection

Inspection is discussed briefly as this is the means by which experimental data is obtained for use in and validation of models. Inspection here relates to integrity assessment of parts (typically by non-destructive testing means), dimensional conformance analysis (deviations from nominal, etc.) and surface topology measurement. Such inspection may be conducted at multiple stages in the LPBF process chain, including during the build itself, and may be applied to feedstock, test coupons, full components or sectioned regions (destructive cut-ups). From the perspective of inspection providing an input/target output for a model of part of the LPBF process chain, it is important to be aware of the limitations of inspection techniques (both in terms of what cannot be inspected, and what the likely uncertainty is) and the format of inspection output (given data transfer challenges).

The three groups of techniques most relevant to metal powder bed part inspection are structured light and laser line scanning, optical surface topography methods such as focus variation, and X-ray Computed Tomography (XCT). The first group relates to optical means of capturing a component's dimensions, which means that it requires line of sight access to the sample surface, and is affected by surface reflectivity. The output format is a point cloud, which may be converted to a (generally non-watertight) surface mesh. Optical surface topography methods are similarly limited by line of sight access constraints and affected by surface reflectivity. The output generally is a surface height map, which can then be processed to obtain surface roughness metrics. XCT is a radiographic method for obtaining a volumetric model of a sample by acquiring many X-ray transmission images. Whilst this technique provides a fully volumetric inspection that can be used for integrity, dimensional

Fig. 13 Prediction of residual stresses using eigenstrain modelling and experimental data for In718 [126]

and topology inspections, it has numerous other limitations, including on the size/density of components that can be inspected [127]. The inspection output is a volume (of greyscale voxels, equivalent to 3D pixels), which can then be processed to obtain a surface mesh. For all these techniques estimating inspection uncertainty is challenging and an active area of research.

Additionally, it is worth noting that modelling techniques may be applied to the inspection process itself, as a means of technique development, inspection planning and optimisation, uncertainty estimation and improving data analysis [128–130]. Such modelling could potentially also be linked into the product manufacturing process chain digital twin, for example with predictions on likely regions of porosity being fed into inspection planning models, to enable optimal inspections [131]. The relevant modelling techniques here are raycasting, for computing optical wavelength inspection coverage as well as the primary (simply absorbed) radiation in X-ray transmission images, and Monte Carlo photon propagation, for modelling more complex matter interactions [132]. Whilst these models are well established, the latter type is generally slow, and producing high fidelity predictions of sensor outputs following photon interaction with real surfaces remains a subject of research [133].

7 Data acquisition and transfer in manufacturing process chain simulation

In the digital twin and the manufacturing process chain, data needs to be transferred between different models that may have been created in different software packages. Physical data will also be required for boundary conditions, material properties, and geometric information, either as inputs or for validation. In general, one model will require more than one set of data, and a single set of data may be used more than once, either because the data is common across multiple parts (e.g. the material powder used is all from the same batch), or because the model that uses the data is being used for multiple predictive scenarios.

7.1 Data acquisition

In order for the data to be used correctly, context about how the data was gathered must be stored with it. This contextual information is called metadata, and it could include all information that would enable users to be sure that the use of the data is appropriate. Metadata could include time and date, sensor type, last date of calibration, operator name (if not automated), identification of the object or material being measured, and measurement uncertainty, amongst other

categories. Collection and transfer of metadata are particularly important for data reuse.

Many of the models in the process chains are transient, and so much of the data gathered will be a time series. If multiple time-dependent data sets are being used in the same model, it is important to ensure that the sensors are synchronised. This is particularly important for data that are gathered often where the quantities being measured change rapidly. Calibration of sensors is vital to the digital twin approach: if the data are gathered from an uncalibrated sensor the results cannot be relied upon. This aspect is particularly important in an industrial environment because the sensors are generally being used in an uncontrolled environment, meaning factors like thermal drift, humidity, and vibration are more likely to affect sensor performance. Similarly (as is discussed in more detail in Sect. 8) uncertainties associated with measurement data affect the reliability of the decisions made based on the digital twin, and a good understanding of the uncertainty associated with the data is required for reliable decision-making.

It is also important to draw a distinction between data to be used for input into models, data to be used for parameter-fitting for models, and data to be used for validation of models. The validation data cannot be used for inputs or for parameter determination, otherwise the model will effectively become a self-fulfilling prophecy. This requirement is necessary even if the data has been used in a sub-model of the model being validated. For instance, if a phase change in a material has been observed, a micro-scale model of that phase change has been developed based on the observations, and the micro-scale model has been fed into a macro-scale model of the process that produced the phase change, then observation of the phase change in the macro scale model cannot be regarded as validation.

7.2 Data transfer

All data transfer within the digital twin may require conversion from one data format to another, as well as the interpolation of data between different models and meshes. For example, an MPBF process model will likely require a large mesh to capture the layers of the build, which may not be appropriate for simulating heat treatment if the furnace and the associated thermal cycles are modelled in detail. This is because modelling the vacuum furnace requires considerable memory to solve the radiation problem. For this type of analysis, the large number of surface elements required is still a limitation. Less refined meshes at the surfaces are therefore desirable for complex geometries, especially when multiple components are placed in the furnace. Further down the chain, different meshes may be needed. For example, surface engineering processes that affect the surface and sub-surface integrity of the component require very fine meshes at the

surface. As a result, interpolation of simulation data from the previous meshes will be needed.

There are several tools available that can transfer and interpolate finite element data between different meshes and solvers, but it must be stated that errors can accumulate during interpolation [134, 135]. The interpolation methods themselves will induce some errors, while the type of data that needs to be interpolated may also have an effect. Values computed at the nodal points of the mesh (such as displacement and temperature) will introduce less error during interpolation because they can be mapped directly. Data that is calculated at integration/Gaussian points (e.g. strains and stresses) will likely generate more errors during data transfer, due to averaging that occurs as they are mapped from a refined mesh to a coarse one.

For example, if data needs to be transferred from an MPBF build process model into a heat treatment model, the predicted strains and stresses of the build model will need to be mapped to the integration nodes of the heat treatment model to be used as an initial condition. If the element shape function is used for the interpolation, the stress and strain values of the additive model will need to be at the nodal points, requiring extrapolation from the integration points. This is done by averaging and smoothing the data, which can introduce errors. If the mesh of the MPBF build process model is more refined than the heat treatment model, and the peak stresses are at the surface, then the integration points of the heat treatment model might be too far from the peak stresses of the build model to accurately capture them. Mapping between processes further down the chain would involve similar steps, and it could therefore generate more errors [123]. Another source of error is the potential use of different material properties for the different models, which could cause rebalancing of the mapped stresses at the beginning of the numerical analyses when computational stress equilibrium is first obtained.

Mapping stress and strain tensors from very refined to very coarse meshes should therefore be avoided. For the case of a heat treatment model where a coarser mesh may be required, it could be good practice to use a coarse mesh for the thermal analyses and a more refined mesh for the mechanical analyses. This would require mapping of temperature data from the nodal points of the coarse mesh into the nodal points of the refined mesh, which should introduce a lower level of error. Errors due to the use of different material properties can be mitigated using the multi-scale approach discussed in Sect. 3. This would prevent the use of material data from test specimens that do not adequately represent the actual material behaviour of the component, such as tensile data from a forged specimen being used to represent the properties of an MPBF part.

Apart from developing accurate process and material models, and data transfer strategies in the manufacturing

process chains, attention should be paid to data storage, traceability, and reuse. This could be achieved by using an open, non-proprietary file format that permits data visualisation [123]. Such a file format would allow data to be passed more readily between different commercial software tools, be easily visualised and analysed when desired, and ensure long-term access to data. This is particularly important for manufacturing areas with strict data retention requirements, such as aerospace.

Figure 14 shows the simulation of two additive manufacturing process chains using data transfer and mapping techniques detailed in [109]. The first manufacturing process chain consists of AM (or LPBF) followed by HT (or stress relief) and shot-peening (SP). The second processes chain applies laser shock peening (LSP) after the stress relief operation instead of SP. The residual stress distribution from both manufacturing routes has been used for the selection of manufacturing routes in the development of new additive manufacturing components and processes. Similar approach for LPBF manufacturing process chain of an aero-casing was used and demonstrated in [134]. In both research works [109, 136], validated process models have been applied to demonstrate the simulation of a manufacturing process chain, but the validation on the process chain has been highlighted as a future research.

8 Uncertainties in modelling, validation and data transfer

8.1 General overview

The evaluation of the uncertainties associated with model results provides increased confidence in those results and supports reliable decision-making. Uncertainty evaluation, and an understanding of associated sensitivity coefficients, can also drive process improvements by identifying the parameters that need to be most tightly controlled to improve product quality. These aspects are particularly important for techniques such as additive manufacturing where a complex process is used to create load-bearing, and potentially safety critical, structural parts.

Uncertainty quantification is also key to model validation: if model results are to be compared to measured values, the uncertainties should be included in the comparison to make the agreement quantitative and meaningful. For instance, if the uncertainties associated with the model results are 100 times bigger than those associated with the measurements, it is highly debatable whether the model is telling you anything useful even if its predictions agree exactly with the measurements.

A lot of the work on uncertainty evaluation in AM processes to date has focussed on assessing process variability

Fig. 14 Predicted principal residual stresses in the LPBF process chain of an impeller [109]. Units in MPa

by measuring the finished product and considering this as uncertainty [137–139]. Whilst this approach does not generally return enough information or understanding to know how to improve a process, it can provide information of the sort needed to validate models in a statistically meaningful way.

Uncertainty evaluation for model results has three main stages [140]:

- Identification of uncertain input quantities and quantification via appropriate probability density functions (PDFs);
- Propagation of the PDFs through the model;
- Summarising the results statistically.

A further step that is useful in many cases is sensitivity analysis, which quantifies the effects of the model inputs on the model outputs and can therefore enable prioritisation. The identification and propagation steps will be discussed in more detail with reference to LPBF and EBPBF below.

The approach above considers only the uncertainties associated with the model inputs (i.e. the parameters and numerical values used to define a specific instance of the model). An additional source of uncertainty that is more difficult to quantify is model uncertainty. This source includes

not only errors associated with discretisation and time stepping, which can usually be reduced if more computational resources are available, but also the effects of the various assumptions made in the model development. The effects of the assumptions are generally very difficult to quantify for a physically derived model and are usually reduced as far as possible through validation and improvement.

The main circumstances where model uncertainty should be considered in more detail are when a simplified model is used for reasons of computational cost. This approach is particularly common in MPBF simulations, where complex multi-physics multi-scale processes need to be simplified in order to be made solvable. Here the information used to validate the simplified model can be used to estimate the model uncertainty, which can then be treated as an additional source of uncertainty in the propagation step, using a statistical model of the error based on the results of the validation. This approach has been used in AM applications to evaluate uncertainty associated with the use of a multiscale model [141, 142].

Hu and Mahadevan [143] provide a thorough overview of the current state of the art regarding uncertainty evaluation for AM, including identifying the uncertain and poorly-known aspects of each stage of the manufacturing process.

The same authors [144] also provided a similar analysis of the various approaches associated with material property prediction.

8.2 Input parameters and assigning distributions

The problem of turning knowledge about a quantity into a suitable probability density function is one of the more difficult aspects of uncertainty evaluation. Generally, the available knowledge will be some combination of measured values, experience and expertise, and results of smaller-scale simulations.

MPBF techniques have a very wide range of inherently variable input parameters. The powder will have an associated size distribution, which may change as a powder gets recycled, and the powder material properties (thermophysical and optical) are likely to vary from sample to sample, from particle to particle, and as recycling occurs. The laser power may be known as an average value, but the laser spot size and the spatial distribution of the power across the spot are likely to be more difficult to obtain.

Jacob et al. [145] have begun to assess the uncertainty associated with measurements of some of these quantities. Others researchers have used smaller-scale models to calculate effective properties and associated uncertainties for input to bulk-scale models [146, 147]. Obtaining appropriate uncertainties for these variations is likely to be one of the key challenges of reliable uncertainty evaluation and hence reliable process control for MPBF.

Most MPBF models have more than one input quantity. The existence of multiple-input quantities raises the question of whether there is correlation between the quantities. Some uncertainty evaluation methods require independence of input quantities, so it is important to identify, and if possible eliminate, any correlations. If it is possible to express two input quantities in terms of a set of independent quantities about which information can be gathered, this is often preferable to the use of correlated quantities.

Some quantities exhibit random behaviour that cannot be described using a single PDF. An example is a material property such as porosity that typically varies randomly in space and has a correlation length associated with its

variation. A commonly accepted approach to describe such quantities is the use of random fields [148]. This approach captures the randomness and the correlation in a way that can be used within a sampling method or another method for the solution of stochastic equations.

The aim of assigning a PDF to a quantity is to encapsulate all available information about the quantity without imposing further constraints on the quantity. The two most useful tools in the assignment process are Bayes' theorem and the principle of maximum entropy, but other approaches can be used if their use can be justified. For instance, a quantity may have been measured so many times that construction of a reliable PDF directly from the measured values is possible, although care should be taken to check the values for drift or other dependencies.

Bayes' theorem is a law of conditional probability that also applies to continuous random variables described by PDFs. The significance here is that it enables a PDF that encapsulates existing information about a quantity to be updated in the light of new information, and in particular it allows a PDF to be assigned based on measurements or other evaluations of the quantity, under certain fairly widely applicable assumptions. The book “Bayesian Data Analysis” by Gelman et al. [149] provided a comprehensive introduction to the use of Bayes' theorem for practical analysis.

The principle of maximum entropy is useful for assigning distributions when information that can be expressed as a statement about the PDF is available. Examples include knowledge of the mean value or other percentiles, knowledge of the standard deviation, and knowledge (including inexact knowledge) of limits on the value of the quantity. Application of the principle of maximum entropy can be mathematically challenging, but it has already been carried out for many commonly available types of information. An extensive list of cases for which solutions have been found is available in Section 6.4 of the first supplement to the Guide to the expression of Uncertainty in Measurement (GUM) [140], including a description of how to sample from each PDF, but some of the most common cases are listed in Table 1 below.

Table 1 Assignment of distributions for different types of information derived using the principle of maximum entropy

Information available	PDF derived using the principle of maximum entropy
Lower and upper limits a and b	Rectangular: $R(a, b)$
Inexact upper and lower limits $a \pm d, b \pm d$	Curvilinear trapezoid: $CTrap(a, b, d)$
Sinusoidal cycling between lower and upper limits a, b	Arc sine (U-shaped): $U(a, b)$
Best estimate x and associated standard uncertainty $u(x)$	Gaussian: $N(x, u^2(x))$
Best estimate x of a non-negative quantity	Exponential: $Exp(1/x)$

See also Table 1 in Section 6.4 of [140]

8.3 Uncertainty propagation and sensitivity

Different methods of uncertainty propagation are suitable for different models. For models that are linear in their uncertain quantities, and if the uncertainties are not dominated by the contribution of one input that does not have a Gaussian distribution, the method described in the GUM is likely to give a reliable value quickly and easily [150]. This approach expands the model function as a Taylor series about its mean value, truncates the series after the linear terms, and uses the results to derive an analytical expression for the uncertainty associated with the model output.

Many models are not linear in their uncertain input quantities, meaning this simple approach is not suitable. Further, the approach requires the user to be able to obtain the partial derivative of the model result with respect to the input quantity (called the sensitivity coefficient). For many models, this information is not available, either because the model has been constructed using “black box” software such as a finite element solver, or because the equations linking the inputs and the outputs are too complicated for this derivative to be obtained.

For nonlinear and “black box” models, sampling methods are preferable. These methods take samples from the PDFs of the uncertain inputs, evaluate the model at the resulting values, and construct a PDF for the output quantities from the evaluated results. The simplest sampling method is random, or Monte Carlo sampling [140]. This method can be analysed to calculate how many samples, M , and hence how many model evaluations, are required for a given level of accuracy in the uncertainty estimate. A value of $M = 10^6$ can often be expected to deliver a 95% coverage interval for the output quantity such that this length of this interval is correct to one or two significant decimal digits.

This number of samples is manageable if the model takes a fraction of a second to run (a million seconds is about 11.5 days), and has been applied to simple models of laser powder bed fusion processes [151]. Most complex models of thermal processes take significantly longer than this to solve. There has been much research into uncertainty evaluation using fewer samples. The available methods can broadly be split into smart sampling methods and surrogate models.

Smart sampling methods use non-random methods of selecting sampling points from the PDFs of the input quantities to obtain improved accuracy for a small number of samples. Latin hypercube sampling [152] is widely used and comparatively simple to implement: the approach subdivides the input PDF into regions of equal probability and samples once within each region, thus ensuring that the sample spans the full range of each input quantity. Approaches such as importance sampling [153] use knowledge of the model to ensure that the sample focusses on the region of the input quantities that causes the greatest variability in the output

quantity. Space-filling sequences can be created by adding random small perturbations to low discrepancy sequences, which are structured sequences that have similar distribution properties to uniformly distributed random variables.

Surrogate models, also known as metamodels, similarly take samples from the inputs and evaluate the model, but they then use various approaches to create a model that is quick to solve, accurately reproduces the results at the points where the full model has been evaluated, and is expected to be a good approximation to the full model in regions where the full model has not been solved [154]. These models can vary in complexity from simple polynomial expressions to more mathematically challenging approaches such as Gaussian processes (often known as kriging) and polynomial chaos.

Gaussian process surrogate models [155] approximate the model output as a weighted sum of random functions, parameterised by a variance and a set of correlation lengths, are chosen so that the values of a function at two points are more strongly correlated the closer they are together. The surrogate model is generally a smooth interpolant of the known model results, and the use of random functions means that an estimate of the interpolation error at intermediate points is immediately available, so that areas where the error is large can easily be identified and further model runs can be carried out to reduce the error. Kriging approaches have been applied to AM models by several authors [156–158], who have provided guidance on methods for the selection of input values to build a reliable surrogate model.

Polynomial chaos uses the link between different families of orthogonal polynomials and specific PDFs, identified by Wiener [159], to construct an approximation to the model as a polynomial of the random variables representing the model input quantities. In many models with only a few inputs, an accurate surrogate can be constructed using a small number of model evaluations. Careful choice of input points is key to efficient implementation for models with a lot of inputs. Polynomial chaos has been applied to AM models for a small number of input parameters [146], focussing on the laser beam diameter and the material emissivity as these quantities are generally poorly known and difficult to control.

An alternative method of reducing the computational complexity of an uncertainty evaluation problem is to reduce the number of uncertain inputs. This can be achieved by focussing only on those inputs whose uncertainties have the most effect on the uncertainty associated with the output quantities. The identification of the most important inputs is effectively a process of sensitivity analysis. Another approach is to reduce problem dimensionality through principal component analysis, which identifies linear combinations of inputs that have the most effect on the output. Assigning a distribution to these combinations would need

to be done numerically, but the problem complexity would be reduced.

The simplest approach to sensitivity analysis is to evaluate, either analytically or numerically, the partial derivative of the model output with respect to the model input, as suggested by the GUM [140]. In general, this gives a single point value, which is only informative if the model is linear. Other approaches use a set of local numerical estimates of the partial derivative to calculate indices that rate not only the sensitivity of the model to each input variable, but also the sensitivity of the model results to combinations of more than one input variable. Sobol indices [160], which give a large amount of information about the input quantities but require multiple model evaluations, have been applied to AM models using a Gaussian process surrogate model [156].

8.4 Uncertainties in data transfer

Transferring data from one model to another is effectively altering the data through a “transfer model”. In some cases, this transfer model is as simple as extracting a single value from one model to use as an input in another model, for instance if a detailed model of a multi-phase material has been used to calculate the effective properties of that material. In such cases, the results of the first model should be treated as an uncertain input to the second model, and the methods discussed above should be used.

In other cases, the transformation of the results of one model are more complicated and so need more careful consideration. One of the most common processes is transferring the results of one type of finite element model to the inputs of another type of finite element model. This task generally includes several potential sources of uncertainty and error:

- change of formats between different software packages;
- change of physics;
- change of geometry or spatial distribution;
- change of time distribution;

The change of format is described in Sect. 7.2. Beyond the challenge of transferring between data formats, common sources of error include consistency of units and coordinate systems (local and global); consistency of tensor notation, particularly when considering stresses and strains; and consistency of definition of signs on stresses and effective stress measures.

Changing physics often generates problems associated with geometry. Models that are constructed to simulate different physics on the same object are likely to have different levels of detail, for instance the key heat flow paths in an object are not necessarily the key load-bearing paths. Further, some objects that are insignificant and hence neglected in one physics model may be crucial to another. An example is the use of plastic supports for some AM geometries: the plastic is an insulator so can be neglected in thermal analysis, which is a key part of stress analyses. These kinds of transfer problems can be reduced via care when planning the analysis and ensuring good communication between different domain experts.

Change of geometry is probably the most common problem when transferring data between models, and it has been discussed in Sect. 7. Change of time step causes similar interpolation issues, with the added complication of stability limitations. In many cases, an error bound for interpolations in time and space can be estimated, either as a constant over the entire model or as a map over the model geometry. The error could then be treated as an additional source of uncertainty uniformly distributed over the interval $[-C, +C]$ where C is the error bound.

Fig. 15 Methodology for determining the TRL rating of different simulations

9 Maturation of MPBF modelling technologies

Technology Readiness Levels (TRLs) have proven to be an effective tool to communicate, design, and launch new products and technologies, adopt new processes, assess internal and external capabilities, and define technology road maps [161–163]. For this work, the TRL scale has been used to determine the maturity of MPBF modelling domains. First, a methodology with 5 questions (as shown in Fig. 15) was developed to determine the TRL of different simulation domains. The aim of the methodology was to provide representative guidance for identifying where different modelling domains are positioned on the TRL scale.

A workshop was conducted to determine the TRL of various MPBF simulation domains by following the proposed methodology. These domains were considered individually, i.e. without concerns about data transfer from one to another. The investigated domains were:

- Mechanical properties: prediction of properties that govern the mechanical behaviour of the part, such as the Young's modulus.
- Physical properties: prediction of properties that govern the non-mechanical behaviour of the part, for example thermal, electrical conductivity or density.
- Micro-cracks: the ability to predict small cracks that form and propagate at the micro and meso scales.
- Surface roughness/texture: the surface finish quality of an MPBF component following a build.
- Micro-structure: the microscopic structure of the material, including grains and precipitates, that evolves as it cools and solidifies.
- Porosity: the ability to predict the amount of non-material space in the part, such as gas pores or other voids.
- Powder distribution/raking: the morphology and distribution of metal powder as it is spread over the build chamber bed.
- Melt pool temperature: the variation in the temperature of the molten material in the melt pool with time.
- Lack of fusion: areas of the part where the powder has failed to fully melt.
- Overheating: the temperature of a component and the risk of it becoming too high during a build.
- Geometric distortion: the deviation of the part geometry from that which is intended due to stresses and strains that arise during the build process.

Fig. 16 Summary of results from TRL mapping workshop. Note that the numbers 0–9 indicate the TRL in the spider diagram. The zero indicates that no work has been done in that domain. Applications—Strengths and Weaknesses

- Recoater collision: the risk of the powder recoating blade within the machine hitting the part due to geometric distortion.
- Residual stresses: stresses remaining in the part following manufacture that arose as a result of the manufacturing process.

The results from this exercise are summarised by Fig. 16, which shows that component scale predictions of geometric distortion, recoater collision, and component scale residual stresses are currently amongst the more developed aspects of MPBF simulation. A variety of commercial tools provide capability in this area, and results around component scale distortion are relatively easy to validate. On the other hand, simulations of micro and meso-scale phenomena, such as the micro-structure, porosity, and physical and mechanical properties, were found to be at the lower end of the TRL scale. There is promising early-stage research in these areas, however, significant investment, research, and development is needed in these domains if the full potential of simulating MPBF is to be realised.

10 Conclusions

An overview of modelling techniques for powder bed fusion process chain has been presented, with a view to identifying the work required to realise future digital twins. This has been achieved through a review of the various computational modelling techniques from micro-scale simulations of powder behaviour to simulations of subsequent process steps such as heat treatment and surface finishing. In addition, methods for transferring data between different models have been discussed, alongside uncertainties involved in modelling

Table 2 Summary of concluding remarks and future perspectives

Technology	Domain	Concluding remarks & future perspectives
Metal powder bed fusion (MPBF)	Modelling of powder	Rain models and models based on the discrete element method have been used to simulate powder raking and distribution of powder. Models should be advanced by incorporating non-spherical shapes. The benefits of the models are that they could support the design of the recoater blade and its operation. Another research challenge is to predict potential defects based on the powder distribution. This challenge would require further research effort by incorporating uncertainty models to describe the input randomness of the initial powder distribution.
	Prediction of temperature	Models for the prediction of the melt pool temperature are available, but the validation of the predicted melt pool temperature history remains a challenge. Prediction of the thermal history at component scale is a challenging due to high computational demands. Analytical models have been developed, as well as method to lumps layers together, but there are still no strong validation procedures, which could be a focus of research.
	Prediction of material properties	Prediction of material properties is heavily dependent on the accuracy of the predicted temperature field which is used for the prediction of the microstructural evolution. There are existing theories based on multi-scale approaches to predict the mechanical properties in MPBF. However, their application at component scale is still a challenge due to the challenges in predicting the thermal history. It is expected that more research emerges in this field in the near future.
	Prediction of distortion	Despite the fact that distortion is depended on the thermal history, macro-scale approaches (e.g. inherent strain method) have been successfully applied to predict distortion at a component level. Sufficient accuracy has been demonstrated and commercial software tools are available. However, for distortion compensation where high accuracy is required, the macro-scale predictive methods for distortion might show weaknesses for some geometries and materials which would require to understand the limitation of those modelling techniques.
	Prediction of residual stresses	Bulk residual stresses have been predicted with macro-scale approaches. There are evidences that the prediction of residual stress field can be reliable. However, the predictions of residual stress distribution need to be further understood at micro-scale and how it affects the development of micro-structure and defects.
	Topology optimisation	Topology optimisation tools for mechanical loads have been widely used in light-weighting applications against proof and fatigue performances. Manufacturing constraints have been also researched and incorporated in the topology optimisation algorithms for MPBF. Embedding manufacturing constraints from post-processes into topology optimised algorithms is an area where further research can be conducted. Optimisation of surfaces for fluid flow and electro-magnetisms is also an area where further research is needed.
Post-processing	Heat treatment	Modelling of temperature history in a furnace is possible. Stress relief models have been also validated and applied to MPBF. Validation of furnace models for prediction of the thermal history in the part could be enhanced. Rapid micro-structural changes in a stress field during the heating could be further research to avoid cracks due to brittleness effects.
	Machining operations	Modelling of machining on additively manufactured parts has been researched, including modelling of bulk material removal and the tool-workpiece interaction. Prediction of microstructural changes and material properties at the surface is an area where further research can be dedicated.
	Surface engineering	Physics-based modelling of surface finishing with conventional and non-conventional technologies remains a challenge due to computational demands. Empirical-based modelling techniques have been primarily used. Surface hardening with shot-peening and laser shock peening have been modelled to predict the residual stress effect. Residual stresses profiles have been superimposed on surfaces using mathematical models.

Table 2 (continued)

Technology	Domain	Concluding remarks & future perspectives
Digital twins	Manufacturing process chains	Research on modelling and simulation of manufacturing process chains has been demonstrated where distortion and residual stresses have been transferred from the LPBF to other post-processes (e.g. heat treatment, machining and surface hardening). However, there is a lack of validation of the predicted residual stresses and distortion for the entire manufacturing process chain. There is also a gap in estimation of errors and uncertainty quantification due to data transfer between models. Modelling the evolution of micro-structured and the non-homogeneous nature of the material has not been studied in the context of manufacturing process chains. There is also a lack of modelling capabilities to predict defect and their evolution in the manufacturing process chain. The integration of process models into manufacturing process chains requires further development and validation to enable the emergence of simulation-based process chain digital twins in the near future.
	Interoperability	The data transfer between models in the process chain has been addressed to some extent. However, there is no standardised data transfer formats to enable the wider usability within the research community. Also, links between inspection data and predictive models should be developed. Development of architectures for enabling seamless interoperability should be addressed in the development of future digital twins.
	Computational performance	The computational power is still a demand in modelling the physics in LPBF and post-processes. The development of surrogate models by using simulation data generated with validated physics-based predictive models is an area where long computational efforts can be overcome in applications requiring real-time calculations (e.g. deep machine learning techniques). Future research for the development of hardware and fast software algorithms is needed.

the process chain. Finally, a discussion on the current maturity of powder bed fusion-specific modelling domains, such as the prediction of residual stresses, has been presented. Table 2 summarises the key conclusions and it provides future perspectives.

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