Epitaxial thin-film $\text{Pd}_{1-x}\text{Fe}_x$ alloy: a tunable ferromagnet for superconducting spintronics

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ABSTRACT Thin epitaxial films of the palladium-rich $\text{Pd}_{1-x}\text{Fe}_x$ alloy were synthesized and extensively studied as a tunable ferromagnetic material for superconducting spintronics. The (001)-oriented MgO single-crystal substrate and the composition range of $x = 0.01\text{--}0.07$ were chosen to support the epitaxial growth and provide the films with magnetic properties spanning from very soft ferromagnet for memory applications to intermediately soft and moderately hard for the programmable logic and circuit biasing, respectively. Dependences of the saturation magnetization, Curie temperature and three magnetic anisotropy constants on the iron content x were obtained for the first time from the analyses of the magnetometry and ferromagnetic resonance data. The experimental results were discussed based on existing theories of dilute ferromagnetic alloys. Simulation of the hysteresis loops within the Stoner-Wohlfarth model indicates the predominant coherent magnetic moment rotation at cryogenic temperatures. The obtained results were compiled in a database of magnetic properties of a palladium-iron alloy in a single-crystal thin-film form considered as a material for superconducting spintronics.

Keywords: palladium-iron alloy, thin epitaxial films, magnetization, magnetic anisotropy, superconducting spintronics

INTRODUCTION

Conventional complementary metal–oxide–semiconductor (CMOS)-based electronics is already approaching its physical limits [1–5], so the end of conventional Moore’s law scaling [6] is really near. Approaches beyond the Moore suggest various solutions comprising new materials and devices, more efficient architectures and packaging, and new models of calcula-

tions [4,5]. One of them pushes forward heterogeneous multi-chip architectures/packages where every kind of calculations is performed by a specialized processor based on optimal device physics.

Forefront in the high-end supercomputing is associated with superconducting Josephson-junction technology [7–10], which offers up to two orders increase in the clock frequency (100 GHz and beyond) and six orders reduction in the energy dissipation per bit operation—incalculable gain against present semiconductor processors [11,12]. Requirement of the cryogenic cooling may seem complicated; however, it should not be a scare, thanks to the development of close-cycle refrigeration. The superconducting single flux quantum (SFQ) Josephson logic technology [13] was implemented in the US Cryogenic Computing Complexity (C3) Program [14,15], aiming to demonstrate a route towards the supercomputing system with the total performance of up to 1000 PFLOPS utilizing sub-ns access time Josephson magnetic random access memory (MRAM) [16–18].

Josephson junctions incorporating ferromagnetic layers were proposed not only for the superconducting spintronic memory, but also for the programmable and reconfigurable digital circuits, dissipationless and reconfigurable clock and biasing networks in SFQ circuits. To realize these applications, a ferromagnetic material which is weak in small spin-polarization of the conduction band is required [19,20], providing insensitivity to the interface roughness, and the range of the layer thickness (10–30 nm) comfortable for the deposition techniques. To restrict a number of materials involved into the production technology, a tunable ferromagnet would be desired since clocking and biasing

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networks require non-switchable, magnetically hard ferromagnetic layer, while memory and reconfigurable logic involve soft ferromagnets with low but different switching fields. Robustness of the magnetic properties is another important requirement to a material for commercial electronic devices. The $\text{Pd}_{1-x}\text{Fe}_x$ alloy with $x = 0.01\text{--}0.03$ is considered as a material for a weak and soft ferromagnet in superconducting MRAM [16,21–23]. Nevertheless, no further development towards a prototype has been demonstrated utilizing the $\text{Pd}_{1-x}\text{Fe}_x$ alloy. Instead, the Josephson magnetic memory cell controlled by a pseudo-spin-valve was demonstrated using a combination of Ni and Py (permalloy), the latter serving as a soft switchable component in the nanometer-thickness range [24].

Tunability of magnetism in the palladium-rich $\text{Pd}_{1-x}\text{Fe}_x$ alloy was extensively studied for the bulk [25]. Much less information is available on the properties of the palladium-iron films. In particular, the polycrystalline films with low iron content ($x \sim 0.01$) have been investigated [26–30]. We could find only a few reports on studies of thin Pd-rich alloy films grown with molecular beam epitaxy (MBE) technique, but no evidence of the epitaxial film growth had been given there [31–34]. The principal characteristics that determine an applicability of $\text{Pd}_{1-x}\text{Fe}_x$ alloys for thin-layer superconductor/ferromagnet/superconductor (S/F/S) type Josephson structures are the saturation magnetization (controls the conduction band exchange splitting) and magnetic anisotropy (determines coercivity and, hence, the switching fields). In this paper we present a systematic study on the magnetic properties

varying with the composition of palladium-rich $\text{Pd}_{1-x}\text{Fe}_x$ ($x = 0.01\text{--}0.07$) alloy thin films epitaxially grown on the single-crystal $\text{MgO}(001)$ substrate, targeting at a low-temperature weak and tunable ferromagnet suitable for superconducting spintronics.

EXPERIMENTAL SECTION

Epitaxial films of $\text{Pd}_{1-x}\text{Fe}_x$ ($x = 0.011\text{--}0.07$) alloy with the thickness of 20 nm were grown on epi-polished (100)-oriented MgO substrates (MTI Corp., USA) utilizing MBE technique in the ultra-high vacuum (UHV) chamber (SPECS GmbH, Germany). The pressure during the depositions was in the range of $(3\text{--}5) \times 10^{-10}$ mbar. The metallic Fe and Pd pellets were simultaneously co-evaporated from pre-calibrated high-temperature effusion cells (CreaTec Fischer & Co., Germany). A three-step deposition procedure [35] was applied to obtain 20-nm-thick, smooth and compositionally homogeneous epitaxial films of $\text{Pd}_{1-x}\text{Fe}_x$ ($x < 0.10$) alloy [36]. The representative transmission electron microscopy (TEM) image, and the selected-area electron diffraction pattern (SAED) from the $\text{MgO}/\text{Pd}_{1-x}\text{Fe}_x$ interface (Fig. 1) confirm epitaxial “cube-on-cube” growth mode of the palladium-iron alloy film on the single-crystalline $\text{MgO}(100)$ substrate. More details of the sample preparation and characterization can be found in Ref. [36].

Magnetic properties of the synthesized samples, which are of primary importance for the superconducting spintronic applications, were studied with the vibrating sample magnetometry (VSM, Quantum Design PPMS-9 system) and ferromagnetic resonance (FMR, Bruker

Figure 1 (a) TEM image of the sample cross-section; (b) magnified area of the $\text{Pd}_{0.988}\text{Fe}_{0.012}/\text{MgO}(001)$ interface where ten interplanar distances were marked for both materials. The inset shows the SAED pattern taken from the interface. High quality of the contrast, reflecting the cubic symmetry of the lattice, is an indication of the single-crystal character of the interface area. Two sets of the superimposed diffraction spots correspond to the MgO lattice (smaller pitch size is due to the larger lattice parameter $a_{\text{MgO}} = 421.6$ pm) and $\text{Pd}_{0.989}\text{Fe}_{0.011}$ lattice (larger pitch size, $a_{\text{Pd}} = 389.1$ pm).

ESP300 cw X-band spectrometer) techniques. The temperature dependence of the magnetic moment $M(T)$ was measured on sample warming from 5 K to 300 K at a rate of 3 K min^{-1} in the saturating magnetic field of 30 Oe applied in the film plane (“in-plane” geometry) along the film easy axis. Magnetic hysteresis loops were recorded with the sweep rate of 2.3 Oe s^{-1} . The measured magnetic moment was reduced to the number of Bohr magnetons (μ_B) per iron atom as well as to the volume magnetization of the film (emu cm^{-3}). The diamagnetic and paramagnetic contributions of the MgO substrate were subtracted from the collected VSM data. The FMR measurement geometries and interpretation are described in Ref. [37].

RESULTS

Fig. 2a shows the temperature dependence of the saturation magnetization for a composition series of $\text{Pd}_{1-x}\text{Fe}_x$ films. In Fig. 2b, the same set of the dependencies is presented in the reduced $M_s/M_s(0)$ vs. T/T_C coordinates. Clearly, these temperature dependencies have practically identical shape for all studied concentrations of iron, though this common dependence is significantly different from that for the pure iron (also shown in Fig. 2b). We will address this observation in the following section.

As expected, both the film saturation magnetization M_s and the Curie temperature T_C raise monotonically with the increase of the iron content x (see Table 1). Maximum magnetic moment per iron atom of $M_{\text{Fe}} \approx 7.5 \mu_B/\text{Fe}$ was found for the $x = 0.017$ sample. This is in a good agree-

ment with the results for the bulk $\text{Pd}_{1-x}\text{Fe}_x$, where the values of $\approx 10 \mu_B/\text{Fe}$ for $x = 0.01$ and $\approx 5.5 \mu_B/\text{Fe}$ for $x = 0.1$ have been reported [39]. However, the obtained result is considerably larger than $\sim 3.7 \mu_B/\text{Fe}$ for a non-epitaxial $\text{Pd}_{0.99}\text{Fe}_{0.01}$ film [29].

Magnetic anisotropy of the films was characterized utilizing the FMR technique. The FMR spectra were recorded at $T = 10 \text{ K}$ for the samples with $x = 0.011\text{--}0.019$ ($T_C < 100 \text{ K}$), and at $T = 20 \text{ K}$ for the samples with higher iron contents. Fig. 3a shows representative angular dependences of the FMR resonance field for the in-plane geometry of the measurements (external magnetic field was rotated in the film plane). The samples reveal the four-fold in-plane magnetic anisotropy with the easy directions along the $\langle 110 \rangle$ axes, which is typical for single-crystalline materials. For instance, Bagguley *et al.* [40] reported that the bulk single-crystalline $\text{Pd}_{0.983}\text{Fe}_{0.017}$ alloy revealed the cubic anisotropy with the hard directions along the $\langle 100 \rangle$ axes. The four-fold anisotropy with the easy $\langle 110 \rangle$ axes in the film plane was also found for nominally epitaxial $\text{Pd}_{1-x}\text{Fe}_x$ ($x \approx 0.04$ and 0.10) films by Garifulin *et al.* [32].

Fig. 3b shows the hysteresis loops for three representative $\text{Pd}_{1-x}\text{Fe}_x$ films with different iron contents. It is clear from the shape of the loops, as well as the FMR angular dependences, that the anisotropy becomes stronger with an increase of the iron content x (see Fig. 3a, b). Coercivity H_c also depends on the iron content and varies from 5.5 to 23 Oe (Table 1). The observed coercive field values are consistent with those reported for polycrystalline films, compared with $H_c \approx 5 \text{ Oe}$ for $x =$

Figure 2 Temperature dependence of the saturation magnetization for a series of 20-nm-thick epitaxial $\text{Pd}_{1-x}\text{Fe}_x$ films on MgO(001), in the absolute (a) and the reduced (b) coordinates. Normalized $M_s(T/T_C)/M_s(0)$ dependence for pure iron is given for a comparison (orange symbols, adopted from Ref. [38]).

Table 1 Experimental parameters of epitaxial Pd_{1-x}Fe_x alloy films with different iron content

x , from XPS	T_C (K)	M_s (emu cm ⁻³)	M_{Fe} (μ _B) ^a	H_c (Oe) ^b		g -factor ^c
				Easy	Hard	
0.011±0.001	36±2	52±4	6.8±0.9	8.8±1.0	7.0±1.0	2.19
0.014±0.001	49±2	63±4	7.1±0.9	7.5±1.0	5.5±1.0	2.20
0.017±0.001	72±3	83±5	7.5±0.8	16.7±1.0	14.7±1.0	2.18
0.019±0.002	73±3	85±5	6.5±0.8	10.1±1.0	7.8±1.0	2.15
0.038±0.002	120±4	119±6	5.3±0.6	8.5±1.0	9.0±1.0	2.15
0.062±0.002	177±5	211±11	5.6±0.5	17.0±1.0	18.5±1.0	2.17
0.070±0.002	200±5	216±11	4.3±0.3	23.0±1.0	15.0±1.0	2.13

a) Magnetic moment per iron atom; b) coercive field measured at 5 K along easy or hard axes of the film; c) for the g -factor, experimental uncertainties are less than 0.004 for all samples.

Figure 3 (a) Angular dependences of the FMR resonance field for the in-plane measurements of Pd_{1-x}Fe_x films with different iron contents (symbols—experimental data; lines—fitting results); the measurement temperature $T = 10$ K for $x = 0.014$ sample and $T = 20$ K for $x = 0.038$ and $x = 0.070$; (b) in-plane magnetic hysteresis loops of Pd_{1-x}Fe_x alloy films measured at 5 K with the field applied along the hard $\langle 100 \rangle$ axis of the film. Right-bottom inset is the same along the easy $\langle 110 \rangle$ axis. Left-top and left-bottom insets demonstrate the long-term stability of the hysteretic and magnetization properties after six months at ambient conditions.

0.01 [30] and $H_c \simeq 25$ Oe for $x = 0.072$ [34].

ANALYSIS AND DISCUSSION

To analyze the temperature dependence of the magnetic moment and the concentration dependence of the ferromagnetic transition temperature T_C , several theoretical models can be applied. These models utilize different approaches in their theoretical frameworks and provide physical parameters suitable for a comparative analysis.

Temperature dependence of the magnetic moment (identification of the magnetism type)

Spin-fluctuation model

The magnetic moment per iron atom in Pd_{1-x}Fe_x series (Table 1) varies from 4.3 μ_B to 7.5 μ_B at saturation, while that in the metallic iron is about 2.2 μ_B [41,42]. This suggests the dominance of the palladium contribution to the total magnetic moment of Pd_{1-x}Fe_x ($x = 0.011$ – 0.070) alloy (or almost equivalent contributions from the iron

and the palladium in the case of the highest iron content, $x = 0.070$, with 4.3 μ_B per iron atom). The universal temperature dependence of the magnetic moment (Fig. 2b) for different concentrations of iron in the studied range makes it reasonable to fit the $M_s(T)$ data within the most general approach, which takes the itineracy of electrons carrying magnetism into account. The approach is based on the Landau-type expansion in a power series in magnetization up to higher orders to account for spin fluctuations [41,43–46]. In the latest analysis by Kuz'min [46], an equation for the reduced magnetization $\sigma(T) = M_s(T)/M_s(0)$ is given, which can be used to fit the experimental $M_s(T)$ from Fig. 2b:

$$\sigma^2(\tau) = \frac{\sqrt{\kappa^2 + 4(1-\kappa)(1-\tau^3)/(1+p\tau^{3/2})} - \kappa}{2(1-\kappa)}. \quad (1)$$

Here, $\tau = T/T_C$, and κ is a dimensionless ratio of the Landau expansion coefficients (of the fourth order to the second order), which depends on the relationship of nonlinear and linear susceptibilities balanced by the sa-

turation magnetization extrapolated to zero temperature [46]. The parameter p provides a correct low-temperature behavior of the magnetic moment $M_s(T)$ (for example, providing compliance with the Bloch- $T^{3/2}$ law for fixed-spin Heisenberg model with spin-wave excitations). The fit of the experimental data (Fig. 4a) has given $p = -0.02 \pm 0.05$ and $\kappa = 2.1 \pm 0.1$. This parameter set is in a drastic contrast with that of $p = 0.95 \pm 0.12$, and $\kappa = 0.86 \pm 0.07$, obtained for gadolinium, which is the localized-spin $S = 7/2$ ferromagnet [47]. Similar data for nickel, which is the iron-group ferromagnetic metal with much higher degree of delocalization of its d-electrons compared with f-electrons of gadolinium, have given $p = 0.28$ and $\kappa = 0.47$ which lie somewhere in between of $\text{Pd}_{1-x}\text{Fe}_x$ and gadolinium [46]. This observation provides a further evidence of a dominant itinerant carriers contribution to the spontaneous magnetization of $\text{Pd}_{1-x}\text{Fe}_x$ alloys in the range of $x = 0.01$ – 0.07 .

Handrich-Kobe model

Nanoscale composition inhomogeneity is a distinctive feature of alloys with respect to elementary metals or stoichiometric compounds. This also affects the shape of the magnetization dependence on temperature. Handrich-Kobe model uses a modified Brillouin function with the distribution of the exchange coupling strength in the positionally disordered environment [48,49]. The reduced magnetization is expressed as:

$$\sigma(\tau) = \frac{1}{2} \{ B_S[(1+\delta)y] + B_S[(1-\delta)y] \}, \quad (2)$$

where $y = [3S/(S+1)]\sigma(\tau)/\tau$, B_S is the conventional (spin-only) Brillouin function and S is the magnetic atom spin value. The exchange fluctuation parameter is defined as $\delta = \sqrt{\langle \Delta J^2 \rangle / \langle J \rangle^2}$, where J is the exchange integral.

Taking $S = 3/2$, which follows the closest proximity from the above to provide the magnetic moment value per atom $\mu(\text{Fe}) = 2.2 \mu_B$ in metallic iron, we obtain $\delta = 0.48$ from the fit of our experimental data (see Fig. 4a). The sensitivity of the theory to the spin value appears to be weak: δ -value varies in the range of 0.45–0.53 when the spin S is varied from 5/2 to 1. The fluctuations of the exchange integral flatten the $M_s(T)$ -dependence against the ideal compositional order ($\delta = 0$ for pure iron) (see Fig. 4a). The value of $\delta \sim 0.48$ is close to that for amorphous iron-containing ferromagnet, for instance, $\delta = 0.5$ for $\text{Fe}_{80}\text{B}_{12}\text{Nb}_8$ [47] and $\delta = 0.55$ for $\text{Fe}_{88}\text{Zr}_7\text{B}_4\text{Cu}_1$ [50]. Exchange fluctuation parameter δ originates from the compositional (structural) disorder and the corresponding distribution of distances to the nearest magnetic neighbors. In this respect, the $\text{Pd}_{1-x}\text{Fe}_x$ alloy with random arrangement of iron atoms is just another nonzero- δ case. Hence, the application of the Handrich-Kobe approach seems to be adequate, despite completely ignoring the contribution of the palladium constituent to the net moment of the alloy.

Korenblit-Shender-Shklovsky model

A commonly accepted physical picture supposes that an iron atom embedded into paramagnetic palladium magnetizes electrons of the host matrix around it because of the d-electron hybridization [41]. Thus, it creates a local “bubble” of magnetized palladium atoms around. Upon cooling, the bubbles of spin-polarized palladium electrons grow in size, and at a temperature when they overlap, the long-range ferromagnetic order sets in. The onset of ferromagnetism thereby occurs through a percolation process involving these spin-polarized bubbles [51]. Korenblit, Shender and Shklovsky [52] elaborated a model of magnetic ordering for Pd-Fe like alloys with low

Figure 4 (a) Normalized saturation magnetization σ dependence on the reduced temperature τ of the $\text{Pd}_{0.989}\text{Fe}_{0.011}$ film (solid symbol) and its fits with three theoretical models (lines), see the legend and main text; (b) Curie temperature dependence on the iron content x (solid symbols) in $\text{Pd}_{1-x}\text{Fe}_x$ alloy films. Solid blue line is a fit with the Mohn-Schwarz model; and dashed red line is a fit with the Korenblit-Shender-Shklovsky model. Green symbols represent experimental $M_s(x)$.

concentration of ferromagnetism-inducing dopant based on a percolation of magnetically-polarized bubbles. The proposed potential of an indirect exchange interaction between two magnetic atoms has a form:

$$V(r) = V_0(R/r)e^{-r/R}. \quad (3)$$

Here V_0 determines the interaction energy scale, r is a distance between the magnetic atoms, $R = a/\sqrt{1+I} \gg a$ is an interaction range (a is the interatomic distance), and $(1+I)^{-1}$ is the static susceptibility enhancement factor of the host [52].

The reduced magnetization σ at a certain temperature T equals to a probability of a magnetic ion occurrence inside the “infinite” magnetic cluster uninterruptedly extending over the entire sample. The resulting $\sigma(T)$ dependence may take the shape of a flattened convex curve for $(4/3)\pi nR^3 \sim 10^{-2} - 10^{-3}$ or even a concave curve for $(4/3)\pi nR^3 < 10^{-4}$ with the threshold depending on the magnetic dopant concentration and the actual range of the interaction provided by the host (n is a number of the dopant atoms per unit volume). The “tail” above T_C cannot be described by this “mean-distance” theory because it does not account for the short-range order effects of the nearest or close neighbors.

The experimental $M_s(T)$ data fitted with the Korenblit-Shender-Shklovsky theory is presented in Fig. 4a for the sample of $\text{Pd}_{1-x}\text{Fe}_x$ alloy with $x = 0.011$ (recalls that the reduced $\sigma(\tau)$ curves have identical shape for $x = 0.011 - 0.070$). The best-fit parameter R varies from ≈ 130 pm to ≈ 70 pm for iron contents within the range from 0.011 to 0.070. These values are unexpectedly small and concentration-dependent, and the latter has not been inherent to the original theory [52].

Fig. 4a presents the fits with the three models mentioned above to the experimental $M_s(T)$ data for the $\text{Pd}_{1-x}\text{Fe}_x$ alloy film with the iron content $x = 0.011$. All the three models fit the data fairly well; however, a model selection based solely on the best-fit criterion would be misleading because of very different assumptions behind these theories. Additional arguments could be obtained from the concentration dependence of the transition temperature $T_C(x)$.

Concentration dependence of the ferromagnetic transition temperature

Mohn-Schwartz model

The spin-fluctuation model of itinerant electron paramagnets doped with magnetic impurities was developed by Mohn and Schwartz to calculate the temperature of the

ferromagnetic transition in alloys of palladium with elements of the iron group [41,53]. The transition temperature T_C is determined by the divergence point of the magnetic susceptibility, which, in turn, is given by the balance of the inverse susceptibilities of the host and magnetic impurity contributions. The concentration-dependent T_C can be found then as a real-valued solution of the cubic equation,

$$A + 5Bak_B T_C + 35C(\alpha k_B T_C)^2 = \frac{(g-1)^2}{\mu_B^2 n} I^2 \frac{2S(S+1)}{3k_B T_C}, \quad (4)$$

where A , B and C are the expansion coefficients of the Landau theory, α is the proportionality coefficient between the mean square of the fluctuating magnetic moment of the host and temperature [53], g and S are the spectroscopic g -factor and spin of magnetic impurity (iron in our case), and I is the constant of coupling between the localized impurity moment and the itinerant electron spin. Left-hand side of Equation (4) is nothing but the inverse magnetic susceptibility of palladium, the fitting of which to a pure palladium susceptibility data fixes parameters $B\alpha/A$ and $C\alpha^2/A$. Namely, $5Bak_B/A = 172(35C(\alpha k_B)^2/A) \text{ K}^{-1}$ from the maximum of Pd susceptibility at $T_{\max} \sim 86 \text{ K}$ [25], and $35C(\alpha k_B)^2/A = 1.4 \times 10^{-5} \text{ K}^2$ from $\chi(T_{\max})/\chi(T=0) \sim 1.115$. All poorly determined quantities in the numerator of the right hand side (r.h.s.) (Equation (4)) can be absorbed into a single parameter subject to the fitting procedure: $(T_C \text{ r.h.s.}/A) = 2920 \text{ K}$. The fitted curve is shown in Fig. 4b by the blue solid line. The resulting concentration dependence of the T_C is found non-linear because of the non-monotonous temperature dependence of the palladium magnetic susceptibility with the maximum at $T_{\max} \sim 86 \text{ K}$. Due to this, the concentration dependence $T_C(x)$ gradually switches from higher increment at low iron content x to the reduced increment once the T_C surpasses $\sim 86 \text{ K}$. The dopant content threshold is within 0.03–0.045 of iron in palladium (see Fig. 4b).

Korenblit-Shender-Shklovsky model

Korenblit, Shender and Shklovsky [52] suggested an expression for the T_C dependence on x within their model of dilute alloy. The Curie temperature corresponds to a percolation of spin-polarized bubbles and occurrence of the “infinite” magnetic cluster:

$$T_C = V_C \frac{Rn^{1/3}}{0.87} \exp\left(-\frac{0.87}{Rn^{1/3}}\right), \quad (5)$$

where $V_C \sim V_0 S^2$, and the numerical factor comes from the percolation theory. The direct fitting of Equation (5)

to the experimental data (Fig. 4b) allows to determine the pre-factor V_C in Equation (5) as $V_C = 650 \pm 120$ K, and the R of 470 ± 40 pm. The $T_C(x)$ dependence is non-linear convex, and this non-linearity is ascribed in Ref. [52] to spatial fluctuations of molecular fields, especially at the lower side of concentrations. The fitting quite matches; however, the mismatch between $R \sim 100$ pm and $R \sim 470$ pm, determined from the fitting to $M_s(T)$ and $T_C(x)$ data, respectively, looks confusing with no explanation at the moment.

Both models describe the concentration dependence of the magnetic transition temperature quite well. However, the Korenblit-Shender-Shklovsky model requires the effective range of the interaction between the impurity atoms $R \gg a$, where a is interatomic distance (Equation (3)), whereas fitting to our experimental data gives for the R parameter the maximal value of 470 pm which is about two interatomic distances. Moreover, the Korenblit-Shender-Shklovsky model predicts gradual change of the shape of $M_s(T)$ -dependence from convex on the high impurity concentration side towards the concave upon dilution. No indication of this trend is visible in our experimental data on $M_s(T)$ (Fig. 4a). On the other hand, the Mohn-Schwarz spin-fluctuation model does not imply the $M_s(T)$ shape to change until the host susceptibility dominates in the net magnetic response of the alloy. For our $\text{Pd}_{1-x}\text{Fe}_x$ samples with $x = 0.011$ – 0.062 , the palladium host magnetism dominates over the iron one (Table 1). So, from our analysis of the particular palladium-rich $\text{Pd}_{1-x}\text{Fe}_x$ alloy we opt for the spin-fluctuation model, albeit not at the evidence level.

In the spin-fluctuation model, the conduction band exchange splitting, which determines the coherence length of Cooper pairs in the $\text{Pd}_{1-x}\text{Fe}_x$ [19,20], scales with the concentration dependence of the magnetic moment $M_s(x)$ (Fig. 2a and Table 1). Once the coherence length is determined for a certain iron content x from the critical current *versus* the alloy thickness dependence [18,21,23], it can be re-calculated for desired iron content x with the use of $M_s(x)$ (Table 1 and Fig. 4b).

FMR quantification of magnetic anisotropies

The angular dependence of the FMR field for resonance (Fig. 3a) was analyzed using the free energy density expansion [54,55] assuming the cubic symmetry of the film lattice with small tetragonal distortion [37]:

$$E = -MH + 2\pi M_s^2 \alpha_3^2 - K_p \alpha_3^2 - \frac{1}{2} K_1 (\alpha_1^4 + \alpha_2^4 + \alpha_3^4) - \frac{1}{2} K_2 \alpha_3^4, \quad (6)$$

where the first term is the Zeeman energy in an external magnetic field; the second term describes the demagnetization energy arising from the thin-film shape of the sample; the third term accumulates the “perpendicular” anisotropy induced by interfaces and a leading term due to the tetragonal lattice distortion; the last two terms are the cubic and second-order tetragonal anisotropy contributions. The indexed α_i ’s represent the directional cosines of the magnetization vector $\mathbf{M}$ with respect to the crystallographic axes ([100], [010], [001]) of the MgO (001) substrate [54,55], and M_s is a saturation magnetization at a given temperature. The anisotropy constants K_i and spectroscopic g -factor are determined by simultaneous fitting of the in-plane (Fig. 3a) and out-of-plane (not shown here) angular dependencies of the resonance field. Resonance field values were obtained by simultaneous solution of the system of Suhl and equilibrium equations [54,55] and for the particular case of $\text{Pd}_{0.92}\text{Fe}_{0.08}$ in Ref. [37]. Upon fitting the FMR data, the saturation magnetization M_s measured by VSM was used to provide the stable convergence of the fitting procedure with the minimal scatter of the freely varied parameters.

Concentration dependences of the anisotropy constants and the spectroscopic g -factor are presented in Fig. 5. The figure shows that the magnitudes of the cubic, K_1 , and the second-order tetragonal, K_2 , anisotropy constants change gradually with an increase of the iron content (con-

Figure 5 Dependences of the anisotropy constants K_1 (a), K_2 (b) and K_p (c) and of the g -factor (d) are shown by solid circles. Dashed line in (d) presents the fit (see text). Results from other studies are presented: for thin film—▲ [32], for bulk single crystal—■ [40], for bulk polycrystal—◆ [56,57], for a thick polycrystalline film—▼ [59].

centration). The cumulative perpendicular and the first-order tetragonal anisotropy, K_p , first, keeps its positive magnitude nearly independent on the iron content, then it changes sign at $x \sim 0.04$ and increases in accelerating manner in the negative value domain. To distinguish the evolution of the intrinsic anisotropies of $\text{Pd}_{1-x}\text{Fe}_x$ alloy from that associated with the thin film morphology, we compare our FMR results with data found in the literature for the bulk sample and for various films. Indeed, FMR studies on the bulk and thick-film $\text{Pd}_{1-x}\text{Fe}_x$ reported on only cubic anisotropy, the energy scale of which, K_1 , is in good agreement with ours (see Fig. 5).

The g -factor for our films lies in the range of 2.13–2.2 (Fig. 5d). It is a typical value for this material, for example, $g = 2.09$ – 2.17 ($x = 0.025$ – 0.06) [32,40,56–59]. The dependence of the g -factor on the iron content x was fit following the prescription of Ref. [40]. The result is shown by the dashed line in Fig. 5d. The values of the g -factors obtained from the fit are $g_{\text{Pd}} = 2.28$ and $g_{\text{Fe}} = 2.0$. These quantities are important in the modeling of the magnetic moment switching by spin-polarized current or magnetic field pulses [60].

Hysteresis loops analysis

The FMR fields for resonance in all studied films have values larger than 1000 Oe, which significantly exceed both coercive fields (maximum 23 Oe, Table 1) and saturation fields (a few hundred Oe, Fig. 3b). Therefore, films under resonance conditions are inevitably in a saturated (single-domain) state. However, among the desired properties of $\text{Pd}_{1-x}\text{Fe}_x$ thin films, mapped on their application in superconducting spintronics, we can find magnetic uniformity and a possibility of a coherent rotation of the magnetization in the film plane by weak magnetic fields. Such information can be obtained from an analysis of the shape of the hysteresis loops. Our epitaxial films were characterized by a pronounced anisotropy in the film plane (Fig. 3a), which is a prerequisite for a coherent (over the film volume) magnetization reversal. The most informative is the shape of the hysteresis loops in the field applied along the hard in-plane direction; representative loops are shown in Fig. 3b. It is seen that the shape of the loops is qualitatively identical for the three compositions presented. In addition, left-top and left-bottom insets of Fig. 3b demonstrate the robustness of the hysteretic and magnetization properties after six months at ambient conditions without any protection.

To model the hysteresis loops we applied a model of the uniform magnetization rotation (Stoner-Wohlfarth mode). Equilibrium orientation of the magnetic moment

φ_M was determined by finding a minimum of the free energy, Equation (6), with the magnetic field of a given magnitude applied at a given angle φ_H in the film plane. The anisotropy constant K_1 obtained from the above analysis of the FMR data was used to model the hysteresis loops. The measured magnetization of the film corresponds to the projection of the equilibrium magnetization on the direction of the applied field [61].

Calculated loops in Fig. 3b reproduce well the experimental ones. Successful simulation of the hysteresis loops of thin epitaxial $\text{Pd}_{1-x}\text{Fe}_x$ films with $x \leq 0.07$ within the Stoner-Wohlfarth model allows us to conclude on predominantly coherent magnetic moment rotation at low temperatures. This, in turn, confirms the promise of these materials for the use as a ferromagnetic layer in the components of superconducting spintronics.

CONCLUSION

Epitaxial $\text{Pd}_{1-x}\text{Fe}_x$ ($0.011 \leq x \leq 0.07$) films were grown on the single-crystal MgO (001) substrates, and magnetic properties of the films, being of the key importance for superconducting spintronics, were extensively studied with the combination of the VSM magnetometry and FMR spectroscopy. All fundamental magnetic parameters, such as the Curie temperature and saturation magnetization, as well as the magnetic anisotropy constants were determined, and their dependences on the iron content x were obtained for the first time. The shape of the magnetization dependence on temperature was found universal in the studied iron content range. It is extensively discussed in the framework of several models of dilute magnetic alloys, and it is concluded that the spin-fluctuation model has the least controversies with our experimental data. The in-plane magnetic hysteresis loops were successfully reproduced utilizing the FMR data for the magnetic anisotropies and the Stoner-Wohlfarth model of the magnetic moment reversal. This allows us to conclude on the predominantly coherent magnetic moment switching upon remagnetization at low temperatures. The presented experimental data cover the range of $0.011 \leq x \leq 0.070$ for the iron content in $\text{Pd}_{1-x}\text{Fe}_x$ alloy suitable for different components of cryogenic spintronic and quantum computing circuits based on Josephson π -junctions.

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designed and engineered the samples; Yanilkin IV and Vakhitov IR performed the magnetic measurements, while Gabbasov BF and Yusupov RV carried out the FMR measurements; Tatarsky DA prepared the sample for TEM imaging; Yanilkin IV, Yusupov RV and Tagirov LR processed the data and wrote the manuscript. All authors contributed to the general discussion and finalization of the manuscript.

Conflict of interest The authors declare no conflict of interest.

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