

LCL-resonance damping strategies for grid-connected inverters with LCL filters: a comprehensive review

Jinming XU¹, Shaojun XIE¹



Abstract Grid-connected LCL-filtered inverters are commonly used for distributed power generators. The LCL resonance should be treated properly. Recently, many strategies have been used to damp the resonance, but the relationships between different damping strategies have not been thoroughly investigated. Thus, this study analyses the essential mechanisms of LCL-resonance damping and reviews state-of-the-art resonance damping strategies. Existing resonance damping strategies are classified into those with single-state and multi-state feedback. Single-state feedback strategies damp the LCL resonance using feedback of a voltage or current state at the resonance frequency. Multi-state feedback strategies are summarized as zero-placement and pole-placement strategies, where the zero-placement strategy configures the zeros of a novel state combined by multi-state feedback, while the pole-placement strategy aims to assign the closed-loop poles freely. Based on these mechanisms, an investigation of single-state and multi-state feedback is presented, including detailed comparisons of the existing strategies. Finally, some future research directions that can improve LCL-filtered inverter performance and minimize their implementation costs are summarized.

Keywords LCL filter, Grid-connected inverter, Resonance damping, State feedback, Investigation

1 Introduction

A voltage source inverter is widely used in renewable energy power generation systems and micro-grids in order to ensure a high-quality grid current [1–3]. However, the pulse width modulation (PWM) of the inverter produces many switching harmonics in the grid current. Thus, to limit these current harmonics according to standards such as IEEE Std 929-2000, an L or LCL filter is needed [4–6]. Compared with the L filter, the LCL filter with or without a harmonic trap in [5, 6] can provide much higher attenuation of switching harmonics with reduced volume and weight so that the power density is increased. Unfortunately, the LCL inherent resonance complicates its control. The passive damping (PD) method with an extra resistor is simple, but it causes power losses [7–10]. Alternatively, active damping (AD) with extra control algorithms has been widely studied.

Existing AD strategies include filter-based AD, feedback-based AD with the feedback of extra voltage and current states, and weighted average control of the two inductor currents. Filter-based AD improves stability by adding a digital filter next to the current controller [11–16]. For feedback-based AD, the state used for feedback can be the capacitor current [17–32], the capacitor voltage [33–36], the inverter-side current [37], the grid current [38–41] or a combination of multiple states [42–50]. Among the feedback-based AD methods, proportional feedback of capacitor current is widely studied during last decade due to its simple implementation. For weighted average control, using the weighted average of the grid current and the inverter-side current, the LCL resonance is avoided [51–57]. All these control strategies have

CrossCheck date: 26 July 2017

Received: 27 January 2016/Accepted: 26 July 2017/Published online: 27 September 2017

© The Author(s) 2017. This article is an open access publication

✉ Jinming XU
xjinming01@163.com

Shaojun XIE
eeac@nuaa.edu.cn

¹ College of Automation Engineering, Nanjing University of Aeronautics and Astronautics, Nanjing, China

been reported to suppress the LCL resonance. Nevertheless, only a few comparative studies have been reported.

In [11], Dannehl et al. conducted a comparative study of filter-based AD with several different kinds of digital filters on the forward path, but differences with respect to other AD strategies were not revealed. In [33], by means of equivalent graph transformation, the concept of a virtual resistor revealed the relationship of PD and AD with capacitor voltage or current feedback. In [34], an effective analysis method unifying the inner feedback loop of capacitor current and voltage was presented. The studies in [33, 34] were limited to AD with feedback of the capacitor state. In [58], Xu et al. analyzed the basic principles of single-state feedback AD based on the capacitor current, capacitor voltage or grid current. The common features of single-state feedback-based ADs were found, but the differences among them and the differences with respect to other kinds of AD were not presented.

In summary, links between various strategies have not been released to the public by the previous work on LCL-resonance damping. The AD mechanisms studied in this paper will help to clarify the relationships among different strategies, and to derive novel strategies. A review of existing resonance damping strategies for AD is elaborated, and some novel ones are derived. Section 2 briefly describes the LCL resonance in the grid-connected inverter and analyses the mechanisms of AD strategies based on the state feedback. Sections 3 and 4 review the strategies for single-state and multi-state feedback, respectively. Section 5 investigates the robustness, implementation costs and impact of AD on grid current distortion with different strategies. Finally, Section 6 concludes this study.

2 Mechanisms of state feedback control to damp LCL resonance

2.1 Resonance of LCL filters in grid-connected inverters

Figure 1 shows the structure of a grid-connected LCL-filtered inverter which consists of the inverter-side inductor

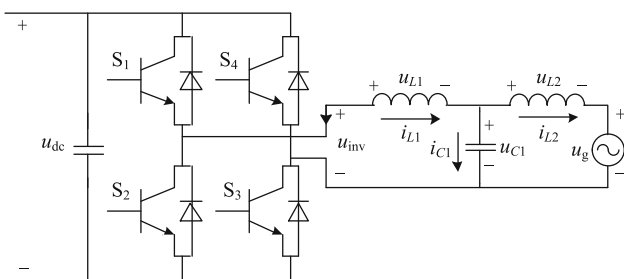


Fig. 1 Grid-connected LCL-filtered inverter

L_1 , capacitor C_1 and grid-side inductor L_2 . The voltage and current state parameters in the LCL filter are marked; u_{dc} is the dc-link voltage, u_{inv} is the output voltage of the inverter bridge, and u_g is the grid voltage. Depending on different practical applications, u_{dc} can be the output of a photovoltaic array, the output of a DC-DC converter or the DC bus voltage in the micro-grid system. As shown in Table 1, transfer functions from u_{inv} to every voltage or current state have a pair of non-damped poles at the resonance frequency ($f_{res} = \omega_{res}/2\pi$) so that a resonance peak exists. For instance, Bode plots for i_{L1} and i_{L2} are shown in Fig. 2.

Subject to the number of states participating in resonance damping, existing AD strategies are classified as single-state or multi-state feedback control.

2.2 Basic principles of single-state feedback control

2.2.1 Feedback compensation

The typical feedback compensation structure given in Fig. 3 indicates that a resonant term $G(s)$ can be controlled by the correct feedback $H(s)$.

Assuming that $G(s)$ exhibits a resonant peak at ω_{res} , the closed-loop frequency response at ω_{res} is expressed as:

$$\frac{C(j\omega_{res})}{R(j\omega_{res})} = \frac{G(j\omega_{res})}{1 + G(j\omega_{res})H(j\omega_{res})} \quad (1)$$

where $G(j\omega_{res})$ approximates infinity and $H(j\omega_{res})$ is the gain of active damping feedback at ω_{res} .

Feedback control theory indicates that feedback compensation would suppress the inherent resonance peak if the real part of $1 + G(j\omega)H(j\omega)$ around ω_{res} is greater than zero. Moreover, for the control in Fig. 3, the resonance peak in $C(s)$ is highly damped once negative feedback (i.e., $G(j\omega_{res})H(j\omega_{res}) > 0$) is achieved. The deeper the negative feedback, the higher the damping of the peak.

A unified control structure based on single-state feedback compensation is given in Fig. 4. The outer loop tracks the reference current i_{ref} while the inner loop is the feedback compensation aiming to damp the resonance. In Fig. 4, u is the output of the current controller $G_c(s)$, x represents one of the voltage and current states in the LCL filter, u_m is the modulation wave (i.e., the PWM reference), and k_{PWM} stands for the transfer function from u_m

Table 1 Transfer functions from inverter output to every state

$G_{u_{inv}}^{i_{L1}}(s) = \frac{1}{L_1 s} \cdot \frac{s^2 + \omega_f^2}{s^2 + \omega_{res}^2}$	$G_{u_{inv}}^{u_{L1}}(s) = \frac{s^2 + \omega_f^2}{s^2 + \omega_{res}^2}$
$G_{u_{inv}}^{i_{C1}}(s) = \frac{1}{L_1} \cdot \frac{s}{s^2 + \omega_{res}^2}$	$G_{u_{inv}}^{u_{C1}}(s) = \frac{1}{L_1 C_1} \cdot \frac{1}{s^2 + \omega_{res}^2}$
$G_{u_{inv}}^{i_{L2}}(s) = \frac{1}{L_1 L_2 C_1 s} \cdot \frac{1}{s^2 + \omega_{res}^2}$	$G_{u_{inv}}^{u_{L2}}(s) = \frac{1}{L_1 C_1} \cdot \frac{1}{s^2 + \omega_{res}^2}$

Note: $\omega_f^2 = 1/(L_2 C_1)$; $\omega_{res}^2 = (L_1 + L_2)/(L_1 L_2 C_1)$



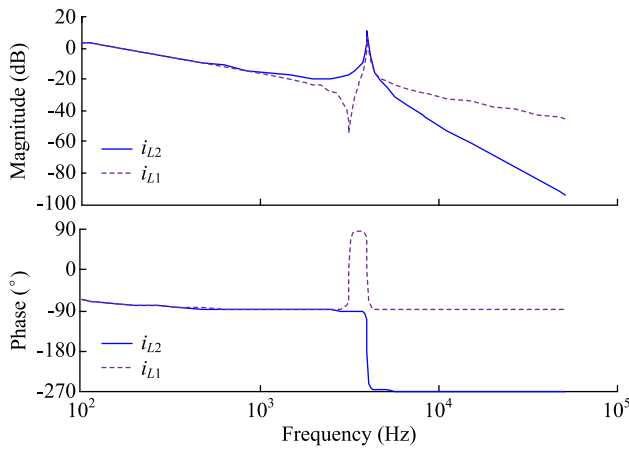


Fig. 2 Bode plots of transfer functions from u_{inv} to i_{L1} and i_{L2}

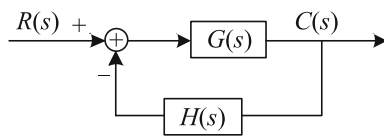


Fig. 3 Typical control structure of feedback compensation

to u_{inv} . Based on the principle of feedback compensation, detailed investigations of the proper $H(s)$ for each state will be presented later.

2.2.2 Cascade compensation

Besides AD based on feedback compensation, cascade (series) compensation is another feasible solution to damp the resonance peak. Cascade compensation is obtained by moving $H(s)$ in Fig. 3 onto the forward path, giving the structure shown in Fig. 5.

Another kind of AD is then derived. Its basic principle is to directly mitigate the peak at ω_{res} . Thus, $H(s)$ should have an extremely low gain at ω_{res} . Then, incorporating the LCL-filtered inverter, the unified control structure based on single-state cascade compensation is given in Fig. 6. Cascade compensation is directly implemented in the closed-loop control of i_{L1} or i_{L2} .

2.3 Basic principles of multi-state feedback control

Multi-state feedback control is achieved by a suitable linear combination of several states. On the one hand, feedback of the combination of states generates a novel

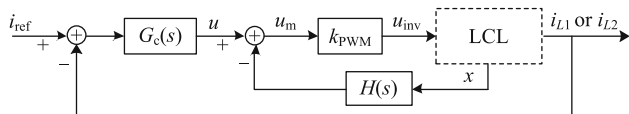


Fig. 4 Unified current control structure with active damping based on single-state feedback compensation

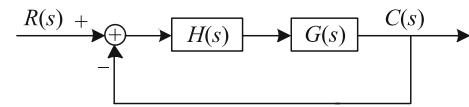


Fig. 5 Typical control structure of cascade compensation

state whose zeros can be assigned. On the other hand, the combined state feedback changes the poles of the system characteristic equation. Then, there are two basic strategies, zero placement and pole placement.

2.3.1 Zero-placement strategy

The unified control scheme of multi-state feedback control with the zero-placement strategy is shown in Fig. 7, where state x_f is a combination of the voltage and current states denoted as x_1, x_2, \dots, x_i with weights $f_1(s), f_2(s), \dots, f_i(s)$, respectively [54].

The transfer function from u_{inv} to x_f is the weighted sum of two or more transfer functions in Table 1:

$$G_{u_{inv}}^{x_f}(s) = f_1(s)G_{u_{inv}}^{x_1}(s) + f_2(s)G_{u_{inv}}^{x_2}(s) + \dots + f_i(s)G_{u_{inv}}^{x_i}(s) \tag{2}$$

The combination does not change the poles of (2) while a couple of conjugate zeros can be placed at ω_{res} to cancel the unstable resonance poles in the denominator. That is, the basic principle for the states x_1, x_2, \dots, x_i and the weights $f_1(s), f_2(s), \dots, f_i(s)$ can be expressed as:

$$(s^2 + \omega_{res}^2)G_{u_{inv}}^{x_f}(s)|_{s=\pm j\omega_{res}} = 0 \tag{3}$$

where the left side is the simplest form with the common divisor $(s^2 + \omega_{res}^2)$ removed. When (3) is satisfied, the simplest form of the transfer function from u_{inv} to x_f is:

$$G_{u_{inv}}^{x_f}(s) = \frac{N(s)}{D(s)} \tag{4}$$

where the numerator and denominator only contain the positive exponential of s .

The lowest order of the transfer functions in Table 1 is 2. Thus, for the sake of simplifying the control design, the order of (4) should be less than 2. Both $N(s)$ and $D(s)$ should be composed of only s^1 and s^0 . Accordingly, the transfer function has three forms: ① the order of $N(s)$ is 1 while that of $D(s)$ is 0; ② $N(s)$ and $D(s)$ are 1 or 0 at the same time; ③ the order of $N(s)$ is 0 while that of $D(s)$ is 1. Among these forms, the third one ensures that only a few

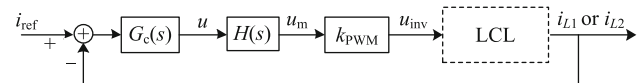


Fig. 6 Unified current control structure with active damping based on single-state cascade compensation

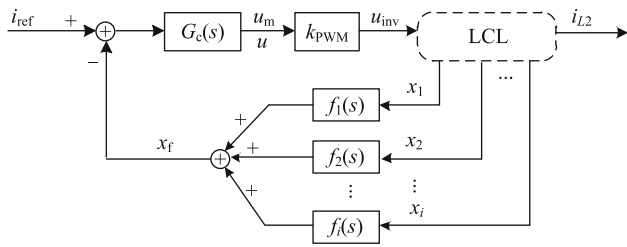


Fig. 7 Unified current control structure of multi-state feedback based on zero-placement strategy

harmonics exist in x_f and is most easily realized. Therefore, the transfer function from u_{inv} to x_f should be:

$$G_{u_{inv}}^{x_f}(s) = \frac{1}{Ls + R} \tag{5}$$

where L and R stand for the coefficient of s^1 and s^0 . This transfer function represents a grid-connected inverter with an L filter, where x_f stands for the current through the inductor, L is the inductance and R denotes the negligible parasitic resistance. In summary, with the zero-placement strategy, an L-filtered grid-connected inverter is virtually constructed from the LCL-filtered one so that current control is effected as control of the L-filtered inverter current x_f [52, 54].

2.3.2 Pole-placement strategy

The pole-placement strategy aims to directly assign all the system poles by the proper choice of state feedback. Figure 8 gives its general control block. Multi-state feedback uses a linear combination of several states. In total, there are 18 kinds of state feedback as shown in (6) where P , I and D stand for proportional, integral and derivative feedback, respectively. The number of states participating in the pole-placement can be 2, 3 or 4 [42–49].

$$x_f = F \left\{ \begin{bmatrix} i_{L1} & u_{L1} & i_{C1} & u_{C1} & i_{L2} & u_{L2} \end{bmatrix} \begin{bmatrix} P \\ I \\ D \end{bmatrix} \right\} \tag{6}$$

$$= F(i_{L1}P + i_{L1}I + i_{L1}D + u_{L1}P + u_{L1}I + \dots + u_{L2}P + u_{L2}I + u_{L2}D)$$

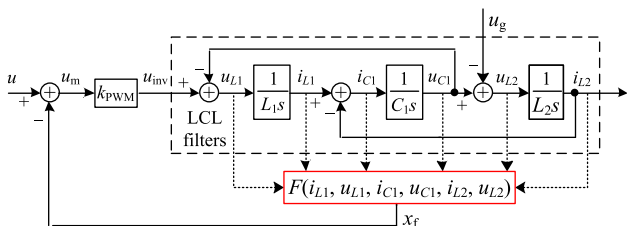


Fig. 8 Unified current control structure of multi-state feedback based on pole-placement strategy

3 Overview of resonance damping strategies with single-state feedback

For active damping based on single-state feedback, in order to make a negative feedback at ω_{res} , the open-loop phase responses from u to all the current and voltage states at ω_{res} need first to be clarified. Then, the requirement of the feedback term $H(s)$ will be obtained.

3.1 Phase characteristics around resonance frequency

Neglecting low-frequency components in u_g , u_{C1} equals u_{L2} . Thus, according to the relationship between current and voltage of inductors and capacitors, i_{C1} has a lead of 180° over i_{L2} (that is, the phases of i_{C1} and i_{L2} are opposite). In addition, because ω_{res} is larger than ω_f , the impedance of C_1 at ω_{res} is much smaller than that of L_2 . Therefore, the phase of i_{L1} around ω_{res} is the same as that of i_{C1} (i.e., with 180° lead over i_{L2} , as demonstrated by Fig. 2), but the amplitude of i_{L1} is smaller than that of i_{C1} according to Kirchhoff's current law. At ω_{res} , due to conjugate resonance poles, a sharp 180° lag occurs. Accordingly, assuming the phase of u_{inv} is 0° , phase variation trends of all the current states around ω_{res} are given in Fig. 9 (the dashed arrows show the increasing trend of ω). Then, considering that the voltage of the inductor is 90° ahead of its current and the capacitor voltage is 90° behind its current, the phases of the voltage states are also given in Fig. 9.

3.2 Strategies based on feedback compensation

3.2.1 AD subject to different options of single state

Based on Sect. 2.2 and Fig. 9, it is easy to obtain the basic requirements for damping the resonance peak as well

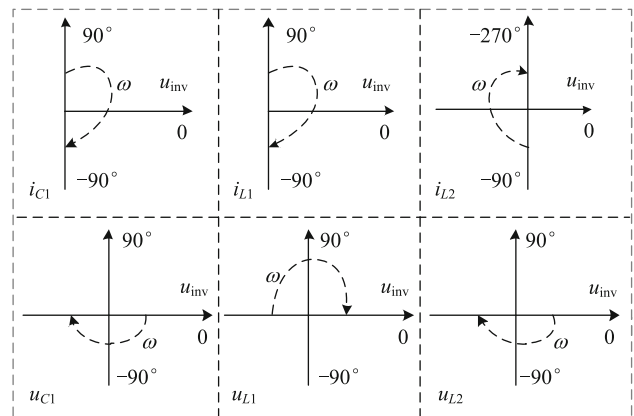


Fig. 9 Phase characteristics of current and voltage states around resonance frequency (i.e., $\omega_{res} \pm \Delta\omega$)

Table 2 Overview of existing resonance damping strategies based on single-state feedback

Single-state feedback control	State x	Requirements of $k_{\text{PWM}}H(j\omega_{\text{res}})$ for AD		$H(s)$ in typical applications		Notes
		Phase	Magnitude	Ignoring delay	Considering one-sample delay	
Feedback compensation in Fig. 4	i_{C1}	0°	$\gg 1$	k [17–25]	k for a low value of α [26, 31, 32, 34]; k with delay compensation [27, 28]	$\alpha = f_{\text{res}}/f_s$
	u_{C1}	90°	$\gg 1$	ks [33, 34] HPF [35]	ks with proper discretization for a medium-to-low value of α [34]; ks with proper discretization and delay compensation [74]	Backward discretization
	i_{L1}	0°	$\gg 1$	k	k with HPF (turnover frequency $< \omega_{\text{res}}$) and delay compensation [37]	No extra sensor for i_{L1} control
	u_{L1}	-90°	$\gg 1$	ks	\	Take care of signal sampling
	i_{L2}	$\pm 180^\circ$	$\gg 1$	ks^2 [38–41] $-ks/(s + \omega)$ [39]	$-ks/(s + \omega)$ for a low value of α or with delay compensation [39]	No extra sensor for i_{L2} control
	u_{L2}	90°	$\gg 1$	ks	\	Same AD with u_{C1} , but different low-frequency dynamic from u_{C1}
Cascade compensation in Fig. 6	i_{L1}	0° \	$\gg 1$ $\ll 1$	1 [59, 60]	1 for a low value of α [11, 12]; lead filter [11]; notch filter [11, 14]	No extra sensor for i_{L1} control Require accurate system information
	i_{L2}	$\pm 180^\circ$ \	$\gg 1$ $\ll 1$	Notch filter	1 for a high value of α [11, 12, 26]; low-pass filter [11]; notch filter [11, 16]	No extra sensor for i_{L2} control Require accurate system information

as to find a suitable AD feedback, as given in Table 2. For instance, in the following, the capacitor current is chosen as an example to explain the principle, while similar discussions on other states are not given. Recall the inner-loop control in Fig. 4 with $x = i_{C1}$ (in other words, Fig. 3 with $R(s) = u$ and $C(s) = i_{C1}$). As can be seen in Fig. 9, the phases of i_{C1} around ω_{res} are always in the first and fourth quadrants. The real part of the transfer function from u_m to i_{C1} in Fig. 4 (i.e., $G(s)$ in Fig. 3) around ω_{res} is always positive. Thus, the gain of $H(s)$ at ω_{res} should be positive for negative feedback, and the attenuation of the LCL resonance peak is higher with a larger gain of $H(s)$. Considering (1), to make the peak below 0 dB, $H(j\omega_{\text{res}})$ should be much larger than 1.

AD strategies based on feedback compensation are in essence the same while their differences mainly lie in the choice of states for feedback. Typical applications of proportional i_{C1} feedback can be found in [17–34]. For 1st-order derivative feedback of u_{C1} , a high-pass filter (HPF) with a similar response is an alternative solution [35].

Feedback of u_{L1} does have the ability of LCL resonance damping, but the measurement of u_{L1} is difficult. For i_{L2} , assuming $H(s) = ks^2$, the peak can be damped [38–41], but the high-order derivative is hard to implement with high reliability in practice. Thus, a novel AD based on i_{L2} feedback is proposed in [39], by using a modified HPF with an optimized parameter design. For feedback of u_{L2} , the difference from u_{C1} feedback is the low-frequency dynamic, considering that u_{C1} is $u_{L2} + u_g$.

3.2.2 Digital control delay impact

In a digital control system, the delay always exists between the signal sampling and the reloading of u_m . If the sampling is at the beginning of the control cycle and the PWM reference is reloaded at the end, the control delay reaches one period (also called one-sample delay). Moreover, the PWM inverter behaves as a zero-order hold. That is, k_{PWM} in the digital control system is:

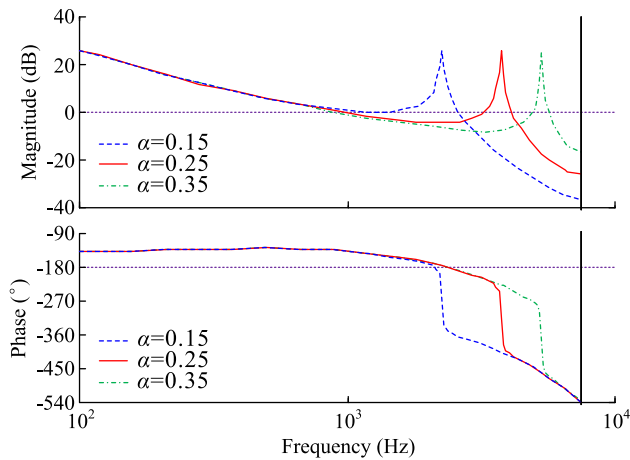


Fig. 10 Open-loop bode plots with only i_{L2} closed-loop control

$$k_{P_{PWM}} = |k_{P_{PWM}}|e^{-sT_d} \cdot \frac{1 - e^{-sT_s}}{sT_s} \tag{7}$$

$$\approx |k_{P_{PWM}}|e^{-sT_d}e^{-sT_s/2} = |k_{P_{PWM}}|e^{-s(T_d+T_s/2)}$$

where T_s is the sampling period; T_d is the delay between the sampling and the reloading of the PWM reference. The control delay causes a considerable phase lag at ω_{res} which is related to ω_{res} and the sampling frequency $f_s = 1/T_s$. The phase lag of (7) at ω_{res} is:

$$\varphi_{lag} = 2\pi \frac{T_d + T_s/2}{T_s} \cdot \frac{f_{res}}{f_s} = 2\pi \frac{T_d + T_s/2}{T_s} \alpha \tag{8}$$

Clearly, a larger α or T_d yields a larger phase lag. Note that α is always smaller than 1/2.

In fact, the delay in (7) could turn the original negative feedback to a positive one. For instance, for i_{C1} feedback, if the phase lag caused by the control delay is larger than 90° , $H(s)$ (here, k) multiplied by $k_{P_{PWM}}$ at ω_{res} is no longer positive. In this case, the proportional feedback of i_{C1} is no longer a negative one so that AD based on i_{C1} feedback becomes unstable. Moreover, if the lag exceeds 270° , $H(s)$ multiplied by $k_{P_{PWM}}$ at ω_{res} turns positive again. This indicates that positive proportional feedback of i_{C1} will be unstable if the phase lag of the control delay satisfies:

$$\frac{\pi}{2} \leq \varphi_{lag} \leq \frac{3\pi}{2} \tag{9}$$

With the use of (8) this implies:

$$\left(\frac{1}{4\alpha} - \frac{1}{2}\right)T_s \leq T_d \leq \left(\frac{3}{4\alpha} - \frac{1}{2}\right)T_s \tag{10}$$

For instance, with one-sample delay (i.e., $T_d = T_s$), the resonance still exists if α is between 1/6 and 1/2, as also analyzed in [26–32, 34]. If (10) is fulfilled, the feedback AD in Fig. 4 produces two unstable poles in the open-loop transfer function from i_{ref} to i_{L1} or i_{L2} , yielding some difficulties for robust design [27, 31].

3.3 Strategies based on cascade compensation

3.3.1 AD for inverter-side or grid current control

Cascade compensation is directly implemented in the closed-loop control of i_{L1} or i_{L2} in Fig. 6. Generally, a standard current controller $G_c(s)$ such as proportion integration (PI) or proportional derivative (PR) yields a negligible phase lag at ω_{res} . If the control delay is not considered, i_{L1} closed-loop control can guarantee stable operation in [59, 60], and it is unnecessary to use a notch filter as $H(s)$ to damp the LCL peak. For i_{L2} closed-loop control without control delay, a notch filter is needed because phase matching at ω_{res} is difficult to realize.

3.3.2 Digital control delay impact

Given that the major feature of the delay is the phase lag, the delay behaves as a phase compensator so that single-loop control can work stably in some cases. For instance, for $T_d = T_s$, i_{L2} closed-loop control cannot easily stabilize the inverter because of insufficient phase lag at ω_{res} when α is lower than 1/6 (c.f. (10)). Figure 10 shows open-loop Bode plots with different α . According to the Nyquist stability criterion [11], when α is 0.15, the system is unstable because there is a -180° crossing at the frequency where the gain is above 0 dB; conversely, when α is 0.25 or 0.35, the system is stable. The situation for i_{L1} closed-loop control is opposite to that for i_{L2} closed-loop control because of the different phases of i_{L1} and i_{L2} as depicted in Figs. 2 and 9. In summary, for low ω_{res} , it is possible to use i_{L1} closed-loop control, while it is hard for the i_{L2} closed-loop control to be stable. For high ω_{res} , i_{L1} closed-loop control is no longer stable, while i_{L2} closed-loop control works well [11, 12, 26, 61–63].

When the delay cannot provide proper phase matching for damping the resonance, the gain $H(s)$ in Fig. 6 is needed. The performance with three kinds of $H(s)$ are studied in [11]. The lead-lag or low-pass digital filter can introduce a slight lead or lag in phase so that phase matching can be further adjusted. The notch filter damps the resonance through direct magnitude adjustment as long as it has an extremely low gain at ω_{res} . Filter-based AD has been broadly discussed in [11–16].

4 Overview of resonance damping strategies with multi-state feedback

4.1 Multi-state feedback control based on zero-placement

4.1.1 Choices of state feedback for zero-placement

In Fig. 7, at least, two states are required to facilitate the zero-placement. Based on the principle in Sect. 2.3.1,



several possible combinations can be obtained. Detailed derivations can be found in [54]. It is found that both weighted average control (WAC) and split capacitor current (LCCL) control in [51–55] are typical applications and use exactly the same weights. In WAC, x_1 is i_{L1} , x_2 is i_{L2} , $f_1(s)$ equals $L_1/(L_1 + L_2)$, and $f_2(s)$ equals $L_2/(L_1 + L_2)$. With the use of Kirchhoff’s current law, the split capacitor current in [51] also equals $f_1(s)i_{L1} + f_2(s)i_{L2}$.

4.1.2 Drawbacks of zero-placement based strategy

The zero-placement current control is effected as control of an L-filtered inverter, but it is stressed that i_{L2} is the final output current of the high-order inverter system. The transfer function from x_f to i_{L2} can be expressed as:

$$G_{x_f}^{i_{L2}}(s) = \frac{\omega_{res}^2}{s^2 + 2\xi\omega_{res}s + \omega_{res}^2} \tag{11}$$

where ξ is the slight damping related to the parasitic resistor. The resonance poles are still observed in the final output. Therefore, zero-placement does not solve the potential resonance in i_{L2} [56]. If the proportional gain of $G_c(s)$ is increased, the control bandwidth increases, but the peak produced by the under-damped conjugate poles also increases. The solid line in Fig. 11 shows the Bode plot of the closed-loop transfer function from i_{ref} to i_{L2} with only the zero-placement current control. The peak occurs at ω_{res} ($L_1 = 1$ mH, $L_2 = 1$ mH, $C_1 = 10$ μ F). Thus, the inverter with only zero-placement works stably with no resonance harmonics if the harmonic interference, especially around ω_{res} , are negligible. However, if there are significant disturbances (e.g., a sudden change of current reference), resonance harmonics will be aroused.

4.1.3 Improvements of zero-placement based strategy

As discussed in Sect. 3.2, AD strategies based on single-state feedback compensation are able to damp the resonance peak. When combined with single-state feedback AD, an

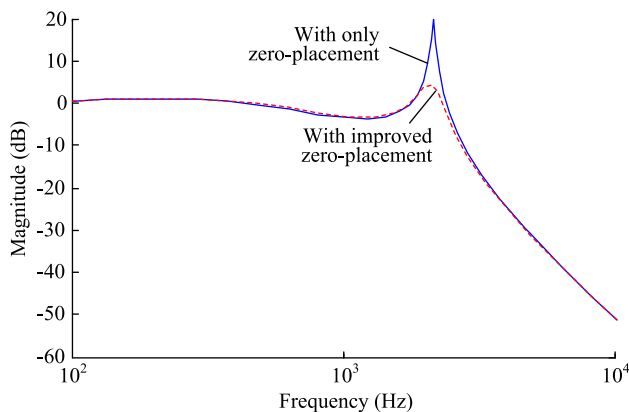


Fig. 11 Characteristics of grid current with different zero-placement

improved zero-placement based control structure is obtained, as shown in Fig. 12. The main disadvantage of introducing the feedback of x_{AD} is the need to sample an extra current or voltage. Thus, AD should avoid the need for an extra state if possible. For instance, when x_1 and x_2 are i_{L1} and i_{L2} , x_{AD} can be one of $\{i_{C1}, i_{L1}, i_{L2}\}$, considering that the difference between i_{L1} and i_{L2} is exactly i_{C1} [56]. The dashed line in Fig. 11 shows the characteristic of i_{L2} with the improved strategy, and the resonance peak is highly suppressed.

4.1.4 Control delay impact

The interval between x_1 sampling and x_2 sampling is denoted as T_{d1} , and that between x_2 sampling and PWM reloading is denoted as T_{d2} . The transfer function from u_{inv} to x_f in Fig. 12 can be expressed as:

$$G_{u_{inv}}^{x_f}(s) = f_1(s)G_{u_{inv}}^{x_1}(s)e^{-sT_{d1}} + f_2(s)G_{u_{inv}}^{x_2}(s) \tag{12}$$

The delay time T_{d2} does not affect the generation of the novel state x_f , but T_{d1} does. If T_{d1} is large, cancelling the resonance poles in (12) is not possible unless the weight $f_1(s)$ or $f_2(s)$ contains a corresponding exponential factor. Luckily, for a digital signal processor (DSP) with a clock frequency of hundreds of megahertz, the time interval between sequential sampling of two signals is negligible so that zero-pole cancellation at the resonance frequency in (12) is still fulfilled approximately.

However, for the extra active damping loop in Fig. 12, the control delay will have a non-negligible impact on its performance, as discussed in Sect. 3.2.

4.2 Multi-state feedback control based on pole-placement

It should be noted that conventional full state feedback control in [44] and the slide mode control in [50] are the typical implementation of (6) with the use of proportional feedback of i_{L1} , i_{L2} and u_{C1} . This kind of multi-state feedback control requires sampling several current and voltage signals. Generally, according to the relationships among the current and voltage states, the choice of states is indeed flexible [49]. For instance, for full state feedback

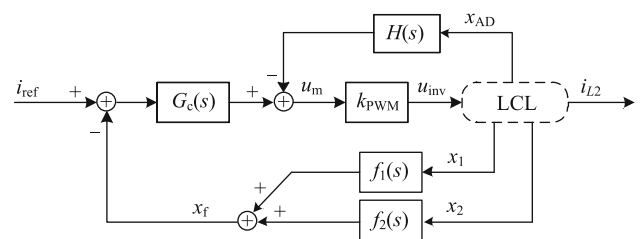


Fig. 12 Unified structure of improved zero-placement based strategies with extra active damping

Table 3 Overview of existing resonance damping strategies based on multi-state feedback

Multi-state feedback control	Requirements	Typical applications	Notes
Zero-placement	Without damping	Eq. (5) WAC [52–55, 57] LCCL current control [51]	Poor performance under disturbances
	With PD	Eq. (5) Minimize power loss WAC with a resistor in series with C_1 [52, 56]	Trade-off between Robustness and loss
	With AD	Avoid extra state for x_{AD} WAC with $x_{AD} = i_{C1}$ [56]	Delay has impact on AD performance (refer to Table 2)
Pole-placement	Sufficient state feedback from (6) for free placement of system poles	Full state feedback control, slide model control, i.e., $x_f = F(i_{L1}P + u_{C1}P + i_{L2}P)$ [42–50] $x_f = F(i_{C1}P + i_{C1}I + i_{L2}P + i_{L2}I)$ [49] $x_f = F(i_{L1}P + i_{L1}I + i_{L2}P + i_{L2}I)$	The design is mostly focused

control, proportional feedback of u_{C1} can be replaced by integral feedback of i_{C1} due to the inherent relation between i_{C1} and u_{C1} . The choice of state feedback can be optimized to reduce the number of sensors.

Studies [42] and [49] treat k_{PWM} as 1 with no delay. However, the control delay which exists in k_{PWM} will make the locations of poles vary from the expected ones. To solve this inconvenience, in [42], researchers try to use the Smith predictor to eliminate the delay impact. For the pole-placement design in the z -domain, another way is to take account the control delay by introducing an extra state. For instance, considering that the control delay appears as z^{-1} , the inverter output voltage was included in the state vector [44–48], and several parameter design methods for full state feedback control were proposed in [45, 46, 48].

Table 3 gives a general overview of the existing multi-state feedback strategies.

5 Discussions

In practice, the question is how to choose appropriately for a specific application from so many available current control strategies. Firstly, stability and robustness have to be assured. Secondly, different strategies require different numbers of sensors. Thirdly, using different states for feedback might yield different abilities to suppress low-order grid current harmonics depending on the low-frequency components of the selected states.

5.1 Stability and robustness improvement

System instability related to LCL resonance can be solved by single-state or multi-state feedback AD. When control delays do not exist, the existing current control

strategies with AD have all been proved to work very well for any LCL parameters [18–24, 34, 39, 60].

Recently, many researchers paid special attention to stability and robustness in the presence of some non-ideal factors. It is concluded in Sects. 3 and 4 that control delay impacts on single-state feedback AD a lot while it has negligible impact on multi-state feedback AD. Besides delay, in practical application the filter parameters may vary from their design values and the grid at the PCC has non-negligible impedance. The studies in [6, 27–32], and [64–68] showed that the resonance frequency is significantly reduced when the filter parameters and the grid impedance are varied.

5.1.1 Single-state feedback AD

For i_{C1} feedback AD (a typical single-state feedback AD), the theoretical derivations in [27–32] discussed the detailed design principle to maintain stability and showed that dual-loop current control could be stable even when the inner-loop AD was unstable (i.e., α fulfills (10)). However, a sharp decrease of ω_{res} , challenged this robustness. Improving the stability of inner-loop AD was critical for improving robustness [31]. Thus, considering that digital delay causes instability of inner-loop AD, delay compensation should be used to improve stability and robustness [27, 31].

Implementating delay compensation is no longer complex nowadays. Several delay compensation methods have been proposed:

- 1) Given that α is equal to f_{res}/f_s , increasing f_s can put α outside the range in (10).
- 2) According to (8), reducing T_d can reduce the phase lag. Then the critical value of α is increased so that a filter with a high ω_{res} will become easier to damp. Adjusting the sampling instant or the reloading instant of u_m [27, 28] can greatly reduce T_d ; but aliasing in the



sampling process should be treated properly, as discussed in [69, 70]. A modified duty cycle generation method based on area equivalence proposed in [71] can also greatly reduce T_d . The multi-sampling method in [72] can reduce the delay to some extent.

- 3) A digital filter featuring phase advance is also a possible way to compensate phase lag, including the lead filter [29, 30], the high-pass filter [31], the second-order generalized integrator (SOGI) [73, 74] and so on. The study in [31] compared some delay compensation methods and recommended reducing T_d as a promising choice.

5.1.2 Single-state cascade AD

Studies discussed in Sect. 3.3 show that stability with single-state cascade AD relies too much on accurate system information including the delay time and the real resonance frequency. Therefore, when the filter parameters and the grid impedance vary widely, stability may be seriously affected. Figure 13 shows the inverter output waveform with notch-filtered AD [11] with $L_1 = L_2 = 1$ mH and $C_1 = 10$ μ F (the following sections will also use these parameters). Before 85 ms, the inverter works well; however, many resonance harmonics are aroused after the grid impedance increases.

The study in [13] tried to design the notch frequency away from the default resonance frequency so that notch-filter AD worked stably when the grid impedance varied within a certain range. In order to maintain a high robustness in the case of widely varying grid impedance, [14] proposed to adjust the notch frequency by estimating the grid impedance on- or off-line. To avoid using grid impedance estimation, [75] used a hybrid method which comprised passive damping and notch filter AD. The robustness with single-state cascade AD was enhanced, but the power loss was increased.

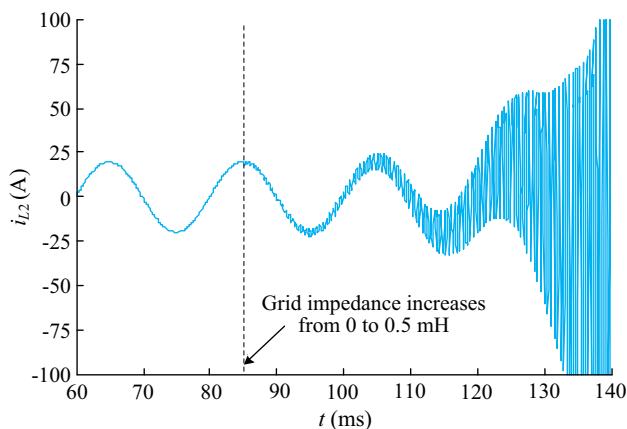


Fig. 13 Current waveform with notch-filter AD subjected to the step change of grid impedance value

5.1.3 Multi-state feedback AD

Pole-placement based multi-state feedback is robust because of the full controllability of the inverter dynamics, as analyzed in [44, 46, 50]. However, for zero-placement based multi-state feedback, the weights $f_1(s)$ and $f_2(s)$ closely relate to the filter parameters. For instance, in the WAC, $f_1(s)$ and $f_2(s)$ depend on L_1 and L_2 . If the real value of L_1 or L_2 varies, the cancellation of unstable resonance poles will be affected. Thus, in [56], an improved WAC with extra i_{C1} feedback (i.e., $x_{AD} = i_{C1}$ in Fig. 12) is used for high robustness. Figure 14 shows the current waveform with improved zero-placement and extra AD control in the case that L_1 varies away from its default value (i.e., the real L_1 is 1.1 mH). Before 45 ms, only zero-placement current control is enabled and a large number of resonance harmonics are stimulated by the mismatch of filter and control parameters. Once the extra AD is enabled, the resonance is eliminated rapidly.

5.2 Implementation costs

The number of sensors is an important contributor to implantation costs, and depends on the choice of current for tracking i_{ref} and the choice of states for damping control. Table 4 shows the required sensors for existing current control strategies. Generally speaking, multi-state feedback based control requires more sensors than the single-state feedback based control. Especially for a three-phase inverter, too many high-precision sensors are needed for multi-state feedback. Among all the existing control strategies, grid current outer-loop control with grid current AD in [39, 40], grid current single-loop control with filter-based AD and inverter-side current single-loop control with

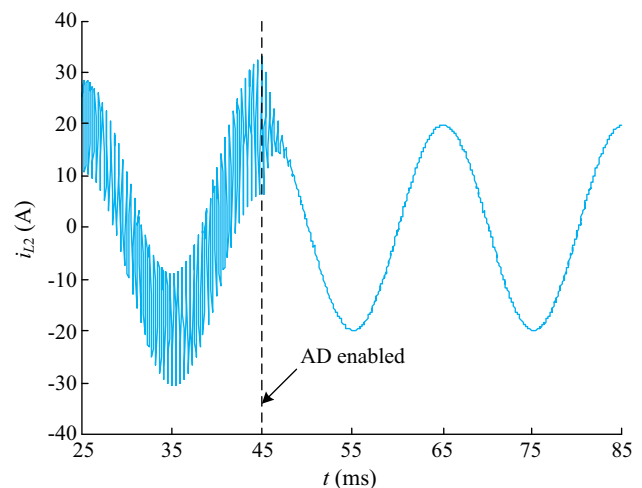


Fig. 14 Current waveform with the improved zero-placement strategy in the case of mismatched filter parameters

Table 4 Comparisons of robustness, sensors and grid current distortions with different strategies

Typical current control	AD category	Robustness	Sensors (except u_g)		Does the AD contribute to grid current distortion?	Notes
			Voltage	Current		
i_{L2} outer-loop with i_{C1} AD	Single-state feedback compensation	High with delay compensations in [27–31, 71–73]	0	2	Yes	Full feedforward of u_g is used to eliminate AD impact [19]
i_{L2} outer-loop with u_{C1} AD			1	1	Yes	Proportional feedforward of u_g cannot eliminate AD impact
i_{L2} outer-loop with i_{L2} AD			0	1	No	/
i_{L2} single-loop with/without filter-based AD	Single-state cascade compensation	Usually poor, but can be improved in [13, 14, 75]	0	1	No	/
i_{L1} single-loop with/without filter-based AD			0	1	No	i_{L2} is indirectly controlled
WAC control	Multi-state zero-placement	Poor	0	2	Yes	
WAC with $x_{AD} = i_{C1}$		High	0	2	Yes	
Full state feedback control	Multi-state pole-placement	High	1	2	Yes	Proportional feedforward of u_g cannot eliminate AD impact [47, 49]
$x_f = F(i_{L1}P + i_{L1}I + i_{L2}P + i_{L2}I)$			0	2	Yes	Recent studies focus on reducing the number of sensors [76–83]

filter-based AD [11, 12] need to sample only one current for current control. To minimize the number of sensors for multi-state feedback control, estimation algorithms should be used. Recently, studies in [76, 77] and [78–83] separately gave some good examples for slide model control and full-state feedback control.

Usually, sampling and control are implemented in digital signal processing (DSP). More time is available for calculation if the sampling frequency is much lower than the DSP clock. Considering that the sampling frequency is usually several to dozens of kHz and the DSP clock is hundreds of MHz [4–6, 11, 12, 19], the calculation can all be finished within one sampling period.

5.3 Current distortion caused by grid voltage harmonics

Grid voltage distortion is the main cause of grid current distortion. Recall the LCL filter structure in Fig. 1. Kirchhoff’s current and voltage laws tell:

$$\begin{cases} u_{C1} = u_{L2} + u_g \\ i_{L1} = i_{C1} + i_{L2} \end{cases} \quad (13)$$

Without considering the current control loop, the low-order voltage harmonics in u_g occur in u_{C1} . Given that i_{C1} has an inherent relation with u_{C1} , i_{C1} also has low-order current harmonics related to the grid voltage harmonics. Furthermore, according to the second equation in (13), i_{L1} also relates closely to the grid voltage harmonics. A similar argument applies to u_{L1} . In summary, compared with feedback of u_{L2} or i_{L2} , the feedback of u_{C1} , i_{C1} , i_{L1} or u_{L1} will add considerable information about grid voltage harmonics into the control loop so the grid current quality can be improved.

The above deduction can also be derived theoretically. When state feedback is used, the grid voltage impact can be directly observed through the transfer function from u_g to i_{L2} . Recall Fig. 8. Clearly, the u_{C1} , i_{C1} , i_{L1} and u_{L1} feedback loops all have no contact with the forward path from u_g to i_{L2} through $-1/L_2s$, while the i_{L2} and u_{L2} feedback loops have contact. Therefore, according to Mason’s gain formula, extra



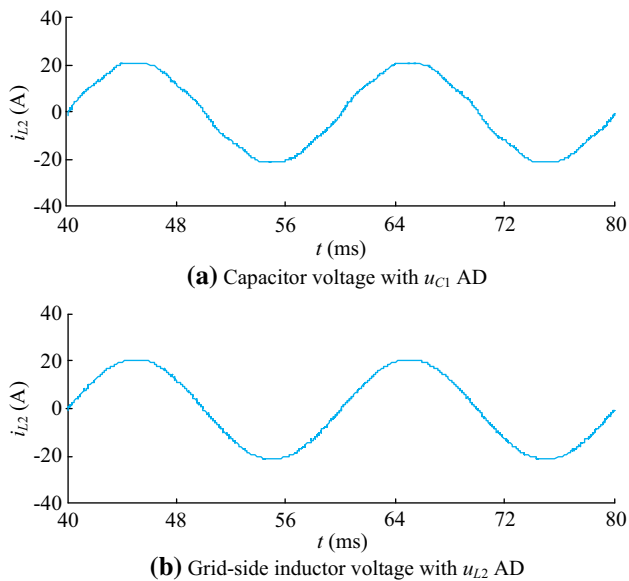


Fig. 15 Distorted grid current waveforms with different feedback AD

terms which are related to the feedback of u_{C1} , i_{C1} , i_{L1} and u_{L1} will occur in the numerator of the transfer function from u_g to i_{L2} . Consequently, grid voltage harmonics in the case of u_{C1} , i_{C1} , i_{L1} and u_{L1} feedback will have extra impact on the grid current quality. For this reason, the full feedforward method uses a 1st-order derivative feedforward of u_g to improve the grid current quality in [19] and [47]. The above investigations are also synthesized in Table 4.

In order to show the effect of different choices of x on grid current distortion, Fig. 15 provides some grid current waveforms with the single-state control in Fig. 4 and identical control parameters when x is u_{C1} or u_{L2} . The grid voltage contains 5% 5th and 7th voltage harmonics. It is found that the grid current with AD feedback of u_{C1} is noticeably distorted, so the above deduction is verified.

5.4 Summary

In order to improve the inverter performance as well as to minimize the implementation cost, current control strategies should exhibit a high robustness, require as few sensors as possible and have negligible impact on grid current distortion. Table 4 gives a general overview.

For the single-state strategies, existing studies mainly focused on improving robustness with the capacitor current AD. But such AD requires an additional sensor and has some adverse impact on grid current distortion. Future studies on improving AD when sampling only the grid current may be necessary, considering that minimal sensors are required and the impact of such AD on low-order grid current distortion is negligible.

Multi-state feedback strategies all need many sensors so the cost is relatively high, especially for three-phase systems. Besides, the multi-state feedback strategies have some adverse impact on the suppression of low-order grid current harmonics because of the use of capacitor voltage, capacitor current, or inverter-side current feedback. But it is noted that these strategies (except those with WAC) are very robust. Thus, recent studies focused on reducing the implementation cost.

6 Conclusions

In this study, the basic principles for resonance damping are analyzed. Existing LCL resonance damping strategies are sorted into four categories, i.e., single-state feedback compensation, single-state cascade compensation, multi-state zero-placement and multi-state pole-placement. Instability caused by the LCL filter can be solved by state feedback with any of the above four mechanisms. Then, a systematic study is provided to reveal not only the similarities but also differences among various LCL-resonance damping strategies. On the basis of the basic control mechanisms, some novel or improved strategies can be derived. Lastly, a comparative investigation of existing strategies has been done in order to reveal the future focus of research on LCL-resonance damping. The objective is simultaneously to improve the inverter performance, e.g., robustness and grid current harmonics rejection, and to minimize the implementation cost.

Acknowledgements This work was supported by National Natural Science Foundation of China (No. 51477077).

Open Access This article is distributed under the terms of the Creative Commons Attribution 4.0 International License (<http://creativecommons.org/licenses/by/4.0/>), which permits unrestricted use, distribution, and reproduction in any medium, provided you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons license, and indicate if changes were made.

References

- [1] Blaabjerg F, Teodorescu R, Liserre M et al (2006) Overview of control and grid synchronization for distributed power generation systems. *IEEE Trans Ind Electron* 53(5):1398–1409
- [2] Zeng Z, Yang H, Zhao R et al (2013) Topologies and control strategies of multi-functional grid-connected inverters for power quality enhancement: a comprehensive review. *Renew Sustain Energy Rev* 24:223–270
- [3] Liu X, Cramer AM, Liao Y (2015) Reactive power control methods for photovoltaic inverters to mitigate short-term voltage magnitude fluctuations. *Electr Power Syst Res* 127:213–220
- [4] Zheng X, Xiao L, Lei Y et al (2015) Optimisation of LCL filter based on closed-loop total harmonic distortion calculation model of the grid-connected inverter. *IET Power Electron* 8(6):860–868

- [5] Wu W, He Y, Blaabjerg F (2012) An LLCL power filter for single-phase grid-tied inverter. *IEEE Trans Power Electron* 27(2):782–789
- [6] Sanatkar-Chayjani M, Monfared M (2016) Stability analysis and robust design of LCL with multituned traps filter for grid-connected converters. *IEEE Trans Ind Electron* 63(11):6823–6834
- [7] Alzola RP, Liserre M, Blaabjerg F et al (2013) Analysis of the passive damping losses in LCL-filter-based grid converters. *IEEE Trans Power Electron* 28(6):2642–2646
- [8] Wu W, He Y, Tang T et al (2013) A new design method for the passive damped LCL and LLCL filter-based single-phase grid-tied inverter. *IEEE Trans Ind Electron* 60(10):4339–4350
- [9] Wu W, Sun Y, Huang M et al (2014) A robust passive damping method for LLCL-filter-based grid-tied inverters to minimize the effect of grid harmonic voltages. *IEEE Trans Power Electron* 29(7):3279–3289
- [10] Beres RN, Wang X, Liserre M et al (2016) A review of passive power filters for three-phase grid-connected voltage-source converters. *IEEE J Emerg Sel Top Power Electron* 4(1):54–69
- [11] Dannehl J, Liserre M, Fuchs FW (2011) Filter-based active damping of voltage source converters with LCL filter. *IEEE Trans Ind Electron* 58(8):3623–3633
- [12] Dannehl J, Wessels C, Fuchs FW (2009) Limitations of voltage-oriented PI current control of grid-connected PWM rectifiers with LCL filters. *IEEE Trans Ind Electron* 56(2):380–388
- [13] Yao W, Yang Y, Zhang X et al (2017) Design and analysis of robust active damping for LCL filters using digital notch filters. *IEEE Trans Power Electron* 32(3):2360–2375
- [14] Pena-Alzola R, Liserre M, Blaabjerg F et al (2014) A self-commissioning notch filter for active damping in three phase LCL-filter based grid-tied converter. *IEEE Trans Power Electron* 29(12):6754–6761
- [15] Bahrani B, Vasiladiotis M, Rufer A (2014) High-order vector control of grid-connected voltage-source converters with LCL-filters. *IEEE Trans Ind Electron* 61(6):2767–2775
- [16] Zhang S, Jiang S, Lu X et al (2014) Resonance issues and damping techniques for grid-connected inverters with long transmission cable. *IEEE Trans Power Electron* 29(1):110–120
- [17] Twining E, Holmes DG (2003) Grid current regulation of a three-phase voltage source inverter with an LCL input filter. *IEEE Trans Power Electron* 18(3):888–895
- [18] Liu F, Zhou Y, Duan S et al (2009) Parameter design of a two-current-loop controller used in a grid-connected inverter system with LCL filter. *IEEE Trans Power Electron* 56(11):4483–4491
- [19] Wang X, Ruan X, Liu S et al (2010) Full feedforward of grid voltage for grid-connected inverter with LCL filter to suppress current distortion due to grid voltage harmonics. *IEEE Trans Power Electron* 25(12):3119–3127
- [20] He J, Li YW (2012) Generalized closed-loop control schemes with embedded virtual impedances for voltage source converters with LC or LCL filters. *IEEE Trans Power Electron* 27(4):1850–1861
- [21] Tang Y, Loh PC, Wang P et al (2012) Generalized design of high performance shunt active power filter with output LCL filter. *IEEE Trans Ind Electron* 59(3):1443–1452
- [22] Xu J, Xie S, Tang T (2013) Evaluations of current control in weak grid case for grid-connected LCL-filtered inverter. *IET Power Electron* 6(2):227–234
- [23] Mukherjee N, De D (2013) Analysis and improvement of performance in LCL filter-based PWM rectifier/inverter application using hybrid damping approach. *IET Power Electron* 6(2):309–325
- [24] Bao C, Ruan X, Wang X et al (2014) Step-by-step controller design for LCL-type grid-connected inverter with capacitor-current-feedback active-damping. *IEEE Trans Power Electron* 29(3):1239–1253
- [25] Jia Y, Zhao J, Fu X (2014) Direct grid current control of LCL-filtered grid-connected inverter mitigating grid voltage disturbance. *IEEE Trans Power Electron* 29(3):1532–1541
- [26] Parker SG, McGrath BP, Holmes DG (2014) Regions of active damping control for LCL filters. *IEEE Trans Ind Appl* 50(1):424–432
- [27] Pan D, Ruan X, Bao C et al (2014) Capacitor-current-feedback active damping with reduced computation delay for improving robustness of LCL-type grid-connected inverter. *IEEE Trans Power Electron* 29(7):3414–3427
- [28] Yang D, Ruan X, Wu H (2015) A real-time computation method with dual sampling modes to improve the current control performances of the LCL-type grid-connected inverter. *IEEE Trans Ind Electron* 62(7):4563–4572
- [29] Zou Z, Wang Z, Cheng M (2014) Modeling, analysis, and design of multifunction grid-interfaced inverters with output LCL filter. *IEEE Trans Power Electron* 29(7):3830–3839
- [30] Li X, Wu X, Geng Y et al (2015) Wide damping region for LCL-type grid-connected inverter with an improved capacitor-current-feedback method. *IEEE Trans Power Electron* 30(9):5247–5259
- [31] Xu J, Xie S, Zhang B (2016) Stability analysis and improvement of the capacitor current active damping of the LCL filters in grid-connected applications. *Journal of Power Electronics* 16(4):1565–1577
- [32] Lyu Y, Lin H, Cui Y (2015) Stability analysis of digitally controlled LCL-type grid-connected inverter considering the delay effect. *IET Power Electron* 8(9):1651–1660
- [33] Wessels C, Dannehl J, Fuchs FW (2008) Active damping of LCL-filter resonance based on virtual resistor for PWM rectifiers-stability analysis with different filter parameters. In: *Proceedings of the IEEE power electronics specialists conference, Rhodes, Greece, 15–19 June 2008*, 7 pp
- [34] Dannehl J, Fuchs FW, Hansen S et al (2010) Investigation of active damping approaches for PI-based current control of grid-connected pulse width modulation converters with LCL filters. *IEEE Trans Ind Appl* 46(4):1509–1517
- [35] Malinowski M, Bernet S (2008) A simple voltage sensorless active damping strategy for three-phase PWM converters with an LCL filter. *IEEE Trans Ind Electron* 55(4):1876–1880
- [36] Komurcugil H, Altin N, Ozdemir S et al (2016) Lyapunov-function and proportional-resonant-based control strategy for single-phase grid-connected VSI with LCL filter. *IEEE Trans Ind Electron* 63(5):2838–2849
- [37] Xu J, Xie S, Kan J et al (2015) An improved inverter-side current feedback control for grid-connected inverters with LCL filters. In: *Proceedings of the 9th international conference on power electronics and ECCE Asia, Seoul, Korea, 1–5 June 2015*, 6 pp
- [38] Dick CP, Richter S, Rosekeit M et al (2007) Active damping of LCL resonance with minimum sensor effort by means of a digital infinite impulse response filter. In: *Proceedings of the European conference on power electronics and applications, Aalborg, Denmark, 2–5 Sept 2007*, 8 pp
- [39] Xu J, Xie S, Tang T (2014) Active damping-based control for grid-connected LCL-filtered inverter with injected grid current feedback only. *IEEE Trans Ind Electron* 61(9):4746–4758
- [40] Wang X, Blaabjerg F, Loh PC (2016) Grid-current-feedback active damping for LCL resonance in grid-connected voltage-source converters. *IEEE Trans Power Electron* 31(1):213–223
- [41] Wang J, Yan JD, Jiang L (2016) Pseudo-derivative-feedback current control for three-phase grid-connected inverters with LCL filters. *IEEE Trans Power Electron* 31(5):3898–3912
- [42] Magueed FA, Svensson J (2005) Control of VSC connected to the grid through LCL filter to achieve balanced currents. In:



- Proceedings of the fortieth IAS annual meeting, Hong Kong, China, 2–6 Oct 2005, 7 pp
- [43] Wu E, Lehn PW (2006) Digital current control of a voltage source converter with active damping of LCL resonance. *IEEE Trans Power Electron* 21(5):1364–1373
- [44] Dannehl J, Fuchs FW, Hansen S (2010) PI state space current control of grid-connected PWM converters with LCL filters. *IEEE Trans Power Electron* 25(9):2320–2330
- [45] Massing JR, Stefanello M, Gründling HA et al (2012) Adaptive current control for grid-connected converters with LCL filter. *IEEE Trans Ind Electron* 59(12):4681–4693
- [46] Huerta F, Pizarro D, Cobrecas S et al (2012) LQG servo controller for the current control of grid-connected voltage-source converters. *IEEE Trans Ind Electron* 59(11):4272–4284
- [47] Xue M, Zhang Y, Kang Y et al (2012) Full feedforward of grid voltage for discrete state feedback controlled grid-connected inverter with LCL filter. *IEEE Trans Power Electron* 27(10):4234–4247
- [48] Maccari LA Jr, Massing JR, Schuch L et al (2014) LMI-based control for grid-connected converters with LCL filters under uncertain parameters. *IEEE Trans Power Electron* 29(7):3776–3785
- [49] Xu J, Xie S, Tang T (2013) Systematic current control strategy with pole assignment for grid-connected LCL-filtered inverters. *J Power Electron* 13(3):447–457
- [50] Hao X, Yang X, Liu T et al (2013) A sliding-mode controller with multi-resonant sliding surface for single-phase grid-connected VSI with an LCL filter. *IEEE Trans Power Electron* 28(5):2259–2268
- [51] Shen G, Xu D, Cao L et al (2008) An improved control strategy for grid-connected voltage source inverters with an LCL filter. *IEEE Trans Power Electron* 23(4):1899–1906
- [52] Shen G, Zhu X, Zhang J et al (2010) A new feedback method for PR current control of LCL-filter-based grid-connected inverter. *IEEE Trans Ind Electron* 57(6):2033–2041
- [53] Shen G, Zhang J, Li X et al (2010) Current control optimization for grid-tied inverters with grid impedance estimation. In: Proceedings of the twenty-fifth annual IEEE applied power electronics conference and exposition, Palm Springs, USA, 21–25 Feb 2010, 6 pp
- [54] Xu J, Xie S (2013) Current control based on zero-placement strategy for grid-connected LCL-filtered inverters. In: Proceedings of the IEEE ECCE Asia Downunder, Melbourne, Australia, 3–6 June 2013, 6 pp
- [55] He N, Xu D, Zhu Y et al (2013) Weighted average current control in a three-phase grid inverter with an LCL filter. *IEEE Trans Power Electron* 28(6):2785–2797
- [56] Xu J, Xie S (2013) Optimization of weighted current control for grid-connected LCL-filtered inverters. In: Proceedings of the IEEE ECCE Asia Downunder, Melbourne, Australia, 3–6 June 2013, 6 pp
- [57] He J, Li YW, Liang X et al (2017) Deadbeat weighted average current control with corrective feed-forward compensation for microgrid converters with non-standard LCL filter. *IEEE Trans Power Electron* 32(4):2661–2674
- [58] Xu J, Xie S, Xiao H (2012) Research on control mechanism of active damping for LCL filters. Proceedings of the CSEE 32(9):27–33
- [59] Teodorescu R, Blaabjerg F, Borup U et al (2004) A new control structure for grid-connected LCL PV inverters with zero steady-state error and selective harmonic compensation. In: Proceedings of the IEEE applied power electronics conference and exposition, California, USA, 22–26 Feb 2004, 7 pp
- [60] Tang Y, Loh PC, Wang P et al (2012) Exploring inherent damping characteristic of LCL-filters for three-phase grid-connected voltage source inverters. *IEEE Trans Power Electron* 17(3):1433–1442
- [61] Wang J, Yan JD, Jiang L et al (2016) Delay-dependent stability of single-loop controlled grid-connected inverters with LCL filters. *IEEE Trans Power Electron* 31(1):743–757
- [62] Tang Y, Yao W, Loh PC et al (2016) Design of LCL filters with LCL resonance frequencies beyond the nyquist frequency for grid-connected converters. *IEEE J Emerg Sel Top Power Electron* 4(1):3–14
- [63] Sanatkar-Chayjani M, Monfared M (2016) Design of LCL and LLCL filters for single-phase grid connected converters. *IET Power Electron* 9(9):1971–1978
- [64] Cespedes M, Sun J (2014) Impedance modeling and analysis of grid-connected voltage-source converters. *IEEE Trans Power Electron* 29(3):1254–1261
- [65] Xu J, Xie S, Tang T (2014) Improved control strategy with grid-voltage feedforward for LCL-filter-based inverter connected to weak grid. *IET Power Electron* 7(10):2660–2671
- [66] Wu TF, Lin LC, Yao N et al (2015) Extended application of D- Σ digital control to a single-phase bidirectional inverter with an LCL filter. *IEEE Trans Power Electron* 30(7):3903–3911
- [67] Tan S, Geng H, Yang G (2016) Impedance matching based control for the resonance damping of microgrids with multiple grid connected converters. *Journal of Power Electronics* 16(6):2338–5805
- [68] Chen X, Zhang Y, Wang S et al (2017) Impedance-phased dynamic control method for grid-connected inverters in a weak grid. *IEEE Trans Power Electron* 32(1):274–283
- [69] Zhang B, Xu J, Xie S (2016) Analysis and suppression of the aliasing in real-time sampling for grid-connected LCL-filtered inverters. In: Proceedings of the IEEE 11th conference on industrial electronics and applications, Hefei, China, 5–7 June 2016, 6 pp
- [70] Liu R, Li B, Duan S (2014) Analysis and suppression of alias in digitally controlled inverters. *IEEE Trans Ind Inf* 10(1):655–665
- [71] Chen C, Xiong J, Wan Z et al (2017) A time delay compensation method based on area equivalence for active damping of an LCL-type converter. *IEEE Trans Power Electron* 32(1):762–772
- [72] Zhang X, Chen P, Yu C et al (2017) Study of current control strategy based on multi-sampling for high-power grid-connected inverters with LCL-filter. *IEEE Trans Power Electron* 32(7):5023–5034
- [73] Xin Z, Wang X, Loh PC et al (2017) Grid-current feedback control for LCL-filtered grid converters with enhanced stability. *IEEE Trans Power Electron* 32(4):3216–3228
- [74] Xin Z, Loh PC, Wang X et al (2016) Highly accurate derivatives for LCL-filtered grid converter with capacitor voltage active damping. *IEEE Trans Power Electronics* 31(5):3612–3625
- [75] Liu Y, Wu W, He Y et al (2016) An efficient and robust hybrid damper for LCL- or LLCL-based grid-tied inverter with strong grid-side harmonic voltage effect rejection. *IEEE Trans Ind Electron* 63(2):926–936
- [76] Guzman R, Vicuna LGD, Camacho A et al (2013) Active damping control for a three phase grid-connected inverter using sliding mode control. In: Proceedings of the 39th annual conference of the IEEE Industrial Electronics Society, Vienna, Austria, 10–13 Nov 2013, 6 pp
- [77] Komurcugil H, Ozdemir S, Sefa I et al (2016) Sliding-mode control for single-phase grid-connected LCL-filtered VSI with double-band hysteresis scheme. *IEEE Trans Ind Electron* 63(2):864–873
- [78] Nishida K, Ahmed T, Nakaoka M (2014) A novel finite-time settling control algorithm designed for grid connected three phase inverter with an LCL type filter. *IEEE Trans Ind Appl* 50(3):2005–2020

- [79] Kukkola J, Hinkkanen M (2014) Observer-based state-space current control for a three-phase grid-connected converter equipped with an LCL filter. *IEEE Trans Ind Appl* 50(4):2700–2709
- [80] Eren S, Pahlevaninezhad M, Bakhshai A et al (2013) Composite nonlinear feedback control and stability analysis of a grid-connected voltage source inverter with LCL filter. *IEEE Trans Ind Electron* 60(11):5059–5074
- [81] Bao X, Zhuo F, Tian Y et al (2013) Simplified feedback linearization control of three-phase photovoltaic inverter with an LCL filter. *IEEE Trans Power Electron* 28(6):2739–2752
- [82] Busada CA, Gomez JS, Solsona JA (2015) Full-state feedback equivalent controller for active damping in LCL-filtered grid-connected inverters using a reduced number of sensors. *IEEE Trans Ind Electron* 62(10):5993–6002
- [83] Guzman R, Vicuna LGD, Morales J et al (2017) Model-based active damping control for three-phase voltage source inverters with LCL filter. *IEEE Trans Power Electron* 32(7):5637–5650

Jinming XU received the B.S. degree in electrical engineering from Nanjing University of Aeronautics and Astronautics (NUAA), Nanjing, China, in 2009, and received the Ph.D. degree in power electronics from NUAA in 2017. He received the 2015 IET Power Electronics Premium Award. In 2017, he joined the College of Automation Engineering, NUAA, where he is currently a lecturer. His current main research interests include the grid-connected inverters and control strategies.

Shaojun XIE received the B.S., M.S., and Ph.D. degrees in Electrical Engineering from Nanjing University of Aeronautics and Astronautics (NUAA), Nanjing, China, in 1989, 1992, and 1995, respectively. In 1992, he joined the Faculty of Electrical Engineering Teaching and Research Division, NUAA, where he is currently a Professor at the College of Automation Engineering. He has authored many technical papers published in many international journals and conference proceedings. His main research interests include aviation electrical power supply systems and power electronic conversion.

