

A robust optimization method for energy management of CCHP microgrid

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Abstract Energy management is facing new challenges due to the increasing supply and demand uncertainties, which is caused by the integration of variable generation resources, inaccurate load forecasts and non-linear efficiency curves. To meet these challenges, a robust optimization method incorporating piecewise linear thermal and electrical efficiency curve is proposed to accommodate the uncertainties of cooling, thermal and electrical load, as well as photovoltaic (PV) output power. Case study results demonstrate that the robust optimization model performs better than the deterministic optimization model in terms of the expected operation cost. The fluctuation of net electrical load has greater effect on the dispatching results of the combined cooling, heating and power (CCHP) microgrid than the fluctuation of the cooling and thermal load. The day-ahead schedule is greatly affected by the

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uncertainty budget of the load demand. The economy of the optimal decision could be achieved by adjusting different uncertainty budget levels according to control the conservatism of the model.

Keywords Combined cooling, Heating and power (CCHP), Microgrid, Piecewise linear, Robust optimization, Uncertainty

1 Introduction

The energy crisis and rising air pollution have led to a greater worldwide focus on energy efficiency methods. A promising approach for domestic power generation is a combined cooling, heating and power (CCHP) system [1-3], that can simultaneously provide cooling, heating and power energy. CCHP systems have also been referred to as trigeneration systems, and have been widely applied in hospitals, supermarkets, and schools [4–7]. CCHP microgrid is a complex system with many operation conditions, a variety of structures, and highly coupled characteristics caused by the physical connections among components. The optimal control strategy relies on the load profile and RES generation, which might show different patterns in the terms of different time scales, such as daily/weekly/monthly/seasonal patterns. It is also difficult to characterize the performance of the components because of the nonlinearity of their efficiency curves, which cannot be expressed as deterministic values. Considering these obstacles, energy management of a CCHP microgrid is challenging.

Many researches have been carried out about optimizing CCHP microgrid operation using different strategies and optimization methods. The performance of CCHP systems following a hybrid electric-thermal load (FHL) is compared with the performance of a CCHP following the electric load (FEL) and the thermal load (FTL) [8]. To compensate prediction error, an online optimal operation approach for CCHP microgrids based on model predictive control with feedback correction was proposed in [9]. A comparison between the CCHP systems and traditional systems was carried out in [10], in terms of the energysaving ratio and the cost-saving ratio. Chance constrained programming and particle swarm optimization were used in [11] to optimize economic dispatch of combined heat and power (CHP) system. The optimization model for planning operation of CCHP systems was presented in [12–14], and the mixed integer nonlinear programming model was then converted into a linear programming model by appropriate piecewise linear approximation of the nonlinear performance curve.

Any solution must address the impacts of uncertainties on optimal CCHP system operation. Stochastic optimization [15–18], chance-constrained stochastic optimization [11, 19, 20], fuzzy programs [21], and quantitative uncertainty analysis [22–24] have been applied in power generation and irrigation systems. However, the computational solutions to the stochastic optimization problem are intractable and only an approximate model can be used. Moreover, the probabilistic distribution or precise data parameters of the uncertainty parameters must be given, which is problematic in real-world applications.

Recently, the robust optimization has received significant attention in [25, 26] as a modelling framework for optimization under parameter uncertainty. The robust optimization seeks the commitment and dispatch of generation resources for immunizing against all possible uncertain situations. In [27], a robust optimization approach was proposed to accommodate the uncertainties of wind power and provide a robust unit commitment schedule for thermal generators under the worst wind power output scenario. Hajimiragha et al. [28] applied a robust model to analyze the electricity and transport sectors by considering the most relevant planning uncertainties and determining the impact of estimation errors on the parameters of the planning model. In considering the worst-case amount of harvested RES, [29] introduced a robust optimization approach to maintain the supply demand balance arising from intermittent RES. In [30], an inexact two-stage stochastic robust programming was proposed for residential micro-grid management-based on random demand. In [31, 32], a robust optimization method was introduced to determine the optimum capacity of distributed generation technologies for buildings under uncertain energy demands. The work in [33] used a robust optimization model for managing combined heat and power systems via linear decision rules. In [34-36], a utilized robust optimization model was utilized to manage building energy system with CHP systems considering the randomness of electrical and thermal load, as well as solar power production. However, [30, 34–36] did not consider battery cost, piecewise linear approximate the non-linear efficiency curves of the MT and their influence on dispatching results. Ramp limits and component operational and maintenance cost were also not considered. In addition, few research considered the situation that the fluctuation of different load have effect on the dispatching results of a CCHP microgrid under different robustness budget.

To deal with these problem, we employ the robust optimization approach incorporating a piecewise linear thermal and electrical efficiency curve to hedge the uncertainties of the power (cooling load, thermal load, electric load, and PV outputs) in this paper. Specifically, the uncertainties of the load and output PV in each period are within an interval defined by their lower and upper bounds and can be obtained based on the historical data or estimated with a confidence interval. This problem can be formulated as a min-max problem with the objective of minimizing the total cost under the worst scenario. We apply a tractable solution approach to solve robust optimization problem and verify the effectiveness of the proposed approach with computational results in this paper.

The remainder of this paper is organized as follows. Section 2 formulates the deterministic optimization model for energy management of a CCHP microgrid. Section 3 presents a detailed expression of the worst-case optimization model and the proposed robust interval optimization model for energy management of CCHP Microgrid. Section 4 presents numerical case study results, and conclusions are drawn in Section 5.

2 Deterministic optimal dispatching model for a CCHP microgrid

A schematic of the energy flows for the CCHP microgrid is shown in Fig. 1. This paper considers a CCHP microgrid that includes a PV cell, a battery, an MT, a gas boiler, an absorption chiller, an electric chiller, and heat exchanger, along with cooling, heating and power load.

1. Optimization objective: The objective function contains cost and incomes:

$$\min C = \sum_{t=1}^{T} C_{grid} + C_{ng} + C_{bt} + C_{rm}$$
(1)

- a) Cost of interacting with the grid: $C_{grid}^{t} = (R_{grid}^{t} P_{grid}^{t} - R_{excess}^{t} P_{excess}^{t}) \Delta t \qquad (2)$
- b) Aging Cost of the battery [34]:



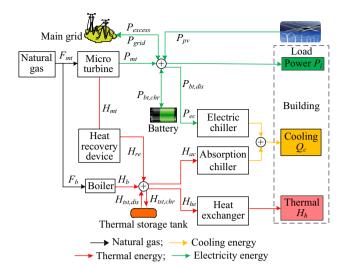


Fig. 1 Schematic of a CCHP microgrid

$$C_{bt}^{t} = R_{bt} (U_{bt,dis*}^{t} + U_{bt,chr*}^{t}) \Delta t$$
(3)

c) Natural gas cost:

$$C_{ng}^{t} = R_{ng}^{t} (F_{mt}^{t} + F_{b}^{t}) \Delta t$$
(4)

d) Running and maintenance cost:

$$C_{rm}^{t} = \begin{bmatrix} P_{mt}^{t} R_{mt,rm} + H_{b}^{t} R_{b,rm} + H_{h}^{t} / \eta_{he} R_{he,rm} \\ + H_{ac}^{t} R_{ac,rm} + P_{ec}^{t} R_{ec,rm} + P_{pv}^{t} R_{pv,rm} \\ + (P_{bt,chr}^{t} + P_{bt,dis}^{t}) R_{bt,rm} + (H_{tst,chr}^{t} + H_{tst,dis}^{t}) R_{tst,rm} \end{bmatrix} \Delta t$$
(5)

where C_{ng}^{t} , C_{grid}^{t} , C_{bt}^{t} , C_{rm}^{t} are the natural gas cost, the cost of interacting with the grid, the aging cost function of the battery, and the running and maintenance cost of the system in time period t, respectively; R_{ng}^{t} is the tariff for natural gas; F_{mt}^{t} , F_{h}^{t} are the fuel consumption of the MT and the boiler in period t, respectively; R_{grid}^{t} is the tariff for purchasing power from the main grid; R_{excess}^{t} is the tariff for selling power to the main grid; P_{grid}^{t} , P_{excess}^{t} are power provided by the main grid and sold to the main grid in period t, respectively; R_{bt}^{t} is charge/discharge of battery cycles cost; U_{c,bt^*}^t , U_{disc,bt^*}^t are the status flag transferring from charging to discharging and from discharging to charging of the battery in period t; P_{mt}^t , H_{mt}^t are the power and heat produced by the MT in period t; $P_{bt,chr}^{t}$, $P_{bt,dis}^{t}$ are the charge/discharge power of BT in period t; $H_{tst,chr}^{t}$, $H_{tst,dis}^{t}$ are the thermal power stored/released by TST in period t; H_{ac}^{t} is the heat required by the absorption chiller when handling the users' cooling requirements in period *t*; P_{ec}^{t} is the electricity demand of the electric chiller when handling the users' cooling requirements in period t; P_{pv}^{t} is the PV output in period t; and R_{rm} is the running and maintenance cost of the unit.

- 2. Constraints on the system: constraints include cooling balances, heating balances, electricity balances and operational constraints for each device.
 - a) Cooling balance:

$$COP_{ac} \cdot H_{ac}^t + COP_{ec} \cdot P_{ec}^t - Q_c^t = 0 \tag{6}$$

b) Thermal balance:

$$H_{re}^t + H_b^t - H_{ac}^t - H_{tst,dis}^t + H_{tst,chr}^t = H_h^t / \eta_{he} \quad (7)$$

where the recovered thermal energy H_{re}^t from the MT can be estimated as:

$$H_{re}^{t} = H_{mt}^{t} \eta_{re} \tag{8}$$

c) Electric power balance:

$$P_{mt}^{t} + P_{grid}^{t} + P_{ec}^{t} + P_{bt,dich}^{t} - P_{bt,chr}^{t} - P_{excess}^{t}$$
$$= P_{l}^{t} - P_{pv}^{t}$$
(9)

d) Micro gas turbine:

The relationship between the fuel energy (F_{mt}^t) and the power output (P_{mt}^t) can be modeled using a straight line [1].

$$F_{mt}^t = \alpha P_{mt}^t + \beta U_{mt}^t \tag{10}$$

where α , β are fuel-to-electric-energy conversion parameter, respectively; and U_{mt}^t is the binary variable that is equal to 1 if the MT is on in period *t* and 0 otherwise. The capacity and ramp rate constraints are define by (9)–(11):

$$U_{mt}^t P_{mt}^{\min} \le P_{mt}^t \le U_{mt}^t P_{mt}^{\max} \tag{11}$$

$$U_{mt}^{t} P_{mt}^{down} \le P_{mt}^{t} - P_{mt}^{t-1} \le U_{mt}^{t} P_{mt}^{up}$$
(12)

For each unit in the system, the input variables (consumed fuel and electricity) are related to the output variables (generated heat, electricity, cooling) by means of the nonlinear performance curves. Usually, low load results in low efficiency. As shown in Fig. 2, the thermal and electrical

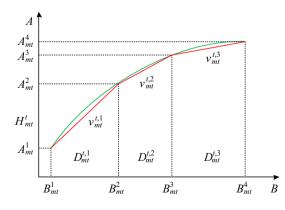


Fig. 2 Piecewise linear approximation of thermal and electrical efficiency curve of the MT



STATE GRID state grid electric power research institute efficiency of the MT is defined in (13)–(16) through piecewise linearization [12]. Because the nonlinear efficiency curve is changed to several line segments, the control problem can be modelled as a MILP:

$$P_{mt}^{t} = U_{mt}^{t} B_{mt}^{1} + \sum_{k=1}^{L_{mt}} D_{mt}^{t,k}$$
(13)

$$U_{mt}^{t} = \sum_{k=1}^{L_{mt}} v_{mt}^{t,k}$$
(14)

$$\sum_{j=k+1}^{L_{mt}} v_{mt}^{t,k} \le \frac{D_{mt}^{t,k}}{B_{mt}^{k+1} - B_{mt}^{k}} \le \sum_{j=k}^{L_{mt}} v_{mt}^{t,k}$$
(15)

$$H_{mt}^{t} = U_{mt}^{t} A_{mt}^{1} + \sum_{k=1}^{L_{mt}} g_{mt}^{k} D_{mt}^{t,k}$$
(16)

where H_{mt}^{t} is the heat produced by the MT; A_{mt}^{k} is the coefficient of the thermal and electrical efficiency curve; B_{mt}^{k} is the block limit of the thermal and electrical efficiency curve; g_{mt}^{k} is the slope of block k of the thermal and electrical efficiency curve; $v_{mt}^{t,k}$ is the binary variable encoding the thermal and electrical efficiency curve of the MT; and L_{mt} is the index set of the piecewise linear thermal and electrical efficiency curve.

e) Storage battery: The MIP formulation of the battery energy model is represented by:

$$\begin{cases}
U_{bt,chr}^{t}P_{bt,chr}^{\min} \leq P_{bt,chr}^{t} \leq U_{bt,chr}^{t}P_{bt,chr}^{\max} \\
U_{bt,dis}^{t}P_{bt,dis}^{\min} \leq P_{bt,dis}^{t} \leq U_{bt,dis}^{t}P_{bt,dis}^{\max} \\
U_{bt,dis}^{t} + U_{bt,chr}^{t} \leq 1 \\
W_{bt}^{t} = W_{bt}^{t-1}(1 - \sigma_{bt}) + (\eta_{bt}^{chr}P_{bt,chr}^{t} - P_{bt,dis}^{t}/\eta_{bt}^{dis})\Delta t \\
W_{bt}^{\min} \leq W_{bt}^{t+1} \leq W_{bt}^{\max}
\end{cases}$$
(17)

Equations (14)–(15) represent the ramp rate constraints of the charging/discharging battery:

$$P_{bt,chr}^{down} \le P_{bt,chr}^{t+1} - P_{bt,chr}^{t-1} \le P_{bt,chr}^{up}$$

$$\tag{18}$$

$$P_{bt,dis}^{down} \le P_{bt,dis}^{t+1} - P_{bt,dis}^{t} \le P_{bt,dis}^{\mu p} \tag{19}$$

Equations (16)–(17) represent the status-transfer flag of the charging/discharging battery:

$$U_{bt,chr}^{t+1} - U_{bt,chr}^t \le U_{bt,chr*}^t \tag{20}$$

$$U_{bt,dis}^{t+1} - U_{bt,dis}^t \le U_{bt,dis*}^t \tag{21}$$

f) Thermal storage tank (TST):

$$\begin{cases} U_{tst,dis}^{t}H_{tst,dis}^{\min} \leq H_{tst,dis}^{t} \leq U_{tst,dis}^{t}H_{tst,dis}^{\max} \\ U_{tst,chr}^{t}H_{tst,chr}^{\min} \leq H_{tst,chr}^{t} \leq U_{tst,chr}^{t}H_{tst,chr}^{\max} \\ U_{tst,chr}^{t} + U_{tst,dis}^{t} \leq 1 \\ H_{ts}^{t} = H_{ts}^{t-1}(1 - \sigma_{tst}) + (\eta_{tst}^{chr}H_{tst,chr}^{t} - H_{tst,dis}^{t}/\eta_{tst}^{dis})\Delta t \\ H_{tst}^{\min} \leq H_{tst}^{t} \leq H_{tst}^{\max} \end{cases}$$

$$(22)$$

g) Power exchange between the main grid and microgrid:

$$\begin{cases} 0 \le P_{grid}^{i} \le U_{grid}^{t} P_{grid}^{\max} \\ 0 \le P_{excess}^{i} \le U_{excess}^{t} P_{grid}^{\max} \end{cases}$$
(23)

Mutual exclusion of status:

$$U_{grid}^t + U_{excess}^t \le 1 \tag{24}$$

3 Solution methodology

3.1 Robust decision-making model

A typical MILP model is defined in the following form:

$$\min \sum_{j=1}^{n} c_j x_j \tag{25}$$

s.t.
$$\sum_{i=1}^{n} a_{ij} x_j \le b_j, \forall i = 1, 2, \cdots, m$$
 (26)

$$x_j \ge 0, \forall j = 1, 2, \cdots, n \tag{27}$$

$$x_j \in \{0, 1\}$$
 for some $j = 1, 2, \cdots, n$ (28)

The uncertainty may reside in the coefficient a_{ii} , the objective function c or the right-hand side b. If these coefficients are unknown constants within known bounds, a meaningful robust MILP can be formulated. Unlike the modeling of uncertainty in stochastic programming, the uncertainty model in robust optimization is typically depicted as an uncertainty range. Each coefficient a_{ii} in the constraints of the constraints of the formulation (i.e., the coefficient of the i^{th} variable in the i^{th} constraint) is an independent, symmetrical and bounded random variable that can assume a value from the interval $[\bar{a}_{ij} - \hat{a}_{ij}, \bar{a}_{ij} + \hat{a}_{ij}]$, where \bar{a}_{ij} is the nominal value and \hat{a}_{ij} is the maximum deviation from the nominal value. The scaled deviation of a_{ij} can be denoted by $\eta_{ij} = (\bar{a}_{ij} -$ $(\hat{a}_{ij})/\bar{a}_{ij}$ or $\eta_{ij} = (\bar{a}_{ij} + \hat{a}_{ij})/\bar{a}_{ij}$, which is defined as the relative value of the forecast error and the realization of the uncertainty. In addition, when formulating a robust MILP



problem [26], it is necessary to define an integer control parameter denoted by Γ_i with values in the interval [0, $|J_i|$]; this is called the budget of uncertainty. $\Gamma_i = 0$ yields the nominal problem and thus does not incorporate uncertainty, whereas $\Gamma_i = |J_i|$ corresponds to interval-based uncertainty sets and leads to the most conservative case. The η_{ij} value is constrained as:

$$\sum_{j \in J_i} \eta_{ij} \le \Gamma_i \tag{29}$$

A robust optimization formulation seeks for optimal solutions that optimize the objective function and meet the problem requirements for all possible uncertainties in constraint coefficients. As a result, the variables are independent of the uncertain parameters. In a worst-case analysis that accounts for uncertainty, we consider the following problem (30)–(33):

$$\min \sum_{j=1}^{n} c_j x_j \tag{30}$$

s.t.
$$\sum_{j=1}^{n} a_{ij} x_j + \max \sum_{j \in J_i} \hat{a}_{ij} \eta_{ij} x_j \le b_j, \forall i = 1, 2, \cdots, m$$
(31)

$$x_i \ge 0, \forall j = 1, 2, \cdots, n \tag{32}$$

$$x_j \in \{0, 1\}$$
 for some $j = 1, 2, \cdots, n$ (33)

For the i^{th} constraint, the auxiliary problem (34)–(36) is shown as follows:

$$\max \sum_{j \in J_i} \hat{a}_{ij} \eta_{ij} |x_j|$$
(34)

s.t.
$$\sum_{j\in J_i} \eta_{ij} \le \Gamma_i$$
 (35)

$$0 \le \eta_{ij} \le 1 \tag{36}$$

Accordingly, the dual of problem (34)–(36) is shown as problem (37)–(40):

$$\min z_i \Gamma_i + \sum_{j \in J_i} p_{ij} \tag{37}$$

s.t.
$$z_i + p_{ij} \ge \hat{a}_{ij} y_j, \forall i, j \in J_i$$
 (38)

$$|x_i| \le y_i \tag{39}$$

$$z_i, p_{ij}, y_j \ge 0 \tag{40}$$

where z_i and p_{ij} are the dual decision variables for constraints (35)–(36) of the auxiliary problem. When incorporating model (37)–(40) into the original problem (30)– (33), the robust linear counterpart is formulated as:

$$\min \sum_{j=1}^{n} c_j x_j \tag{41}$$

s.t.
$$\sum_{j \in J_i} a_{ij} x_j + z_i \Gamma_i + \sum_{j \in J_i} p_{ij} \le b_i$$
(42)

$$x_j \ge 0, \forall j = 1, 2, \cdots, n \tag{43}$$

$$x_j \in \{0, 1\}$$
 for some $j = 1, 2, \cdots, n$ (44)

$$z_i + p_{ij} \ge \hat{a}_{ij} y_j, \forall i, j \in J_i \tag{45}$$

$$|x_j| \le y_j \tag{46}$$

$$z_i, p_{ij}, y_j \ge 0 \tag{47}$$

3.2 Uncertain energy output formulation

In general, the optimal operation of a CCHP microgrid is associated with uncertainties from cooling, thermal and electrical load, and the PV output. The randomness of cooling and thermal load is affected by the weather surrounding the buildings; the electrical load in the buildings are influenced by the level of consumer activities, and the power output of a PV unit can be impacted by the radiation of the sun and the ambient weather. Because of these factors, it is difficult to precisely characterise their power value. In this paper, we assume that these power values fall within the intervals of $Q_{c,u}^t \in [Q_c^t - Q_c^{ld}, Q_c^t + Q_c^{ud}], H_{h,u}^t \in [H_h^t - H_h^{ld}, H_h^t + H_h^{ud}], P_{l,u}^t \in [P_l^t - P_l^{ld}, P_l^t + P_l^{ud}], \text{ and } P_{pv,u}^t \in [P_{pv}^t - P_{pv}^{ld}, P_{pv}^t + P_{pv}^{ud}], \text{ with } Q_c^t, H_h^t, P_l^t \text{ and } P_{pv}^t \text{ represent}$ senting the predicted value in period t and $Q_{c,u}^t$, $H_{h,u}^t$, $P_{l,u}^t$ and $P_{pv,u}^{t}$ representing sets of possible cooling, thermal and electrical load and the output PV. Q_c^{ld} , Q_c^{ud} , H_h^{ld} , H_h^{ud} , P_l^{ld} , P_l^{ud} , P_{pv}^{ld} and P_{pv}^{ud} representing the allowed maximum deviations above and below Q_c^t , H_h^t , P_l^t and P_{pv}^t , respectively, which can take any values with their uncertain interval. For this approach, Γ_c^t , Γ_h^t , Γ_{nl}^t represent cardinality budgets [26] introduced to adjust the ranges of uncertainty for the cooling, thermal and net electricity load $(P_l^t - P_{mv}^t)$ in period t by the system operators, respectively; these affect the robustness of the problem against the level of conservatism of the solution.

The worst-case scenario is the key aspect of the robust interval optimization model; it is a set of parameter values such that the security for any other scenarios can be guaranteed if and only if there is a feasible solution under this scenario [32–35]. Therefore, the expressions in (48), (51) and (54), can be interpreted as the security requirements of the CCHP microgrid under the worst-case scenarios of uncertain parameters (cooling, thermal, electrical load and PV output):

$$COP_{ac} \cdot H_{ac}^{t} + COP_{ec} \cdot P_{ec}^{t} = \max Q_{c,u}^{t}$$
$$= Q_{c}^{t} + \max \{ \eta_{c}^{ld} Q_{c}^{ld} + \eta_{c}^{ud} Q_{c}^{ud} \}$$
(48)



$$\eta_c^{ld} + \eta_c^{ud} \le \Gamma_c^t \tag{49}$$

$$0 \le \eta_c^{ld}, \eta_c^{ud} \le 1 \tag{50}$$

$$H_{re}^{t} + H_{b}^{t} - H_{ac}^{t} - H_{tst,dis}^{t} + H_{tst,chr}^{t} = \max(H_{h,u}^{t})/\eta_{he}$$

= $H_{t}^{t}/\eta_{he} + \max\{\eta_{c}^{ld}H_{c}^{ld} + \eta_{c}^{ud}H_{c}^{ud}\}/\eta_{he}$ (51)

$$\eta_h^{ld} + \eta_h^{ud} \le \Gamma_h^t \tag{52}$$

$$0 \le \eta_h^{ld}, \eta_h^{ud} \le 1 \tag{53}$$

$$P_{mt}^{i} + P_{grid}^{i} + P_{br,chr}^{i} + P_{ec}^{i} - P_{excess}^{i} - P_{bt,dis}^{i}$$

$$= \max(P_{l,u}^{t} - P_{pv,u}^{t})$$

$$= P_{l}^{t} - P_{pv}^{t} + \max\left\{\eta_{l}^{ld}P_{l}^{ld} + \eta_{l}^{ud}P_{l}^{ud} - \eta_{pv}^{ld}P_{pv}^{ld} - \eta_{pv}^{ud}P_{pv}^{ud}\right\}$$
(54)

$$\eta_l^{ld} + \eta_l^{ud} + \eta_{pv}^{ld} + \eta_{pv}^{ud} \le \Gamma_{nl}^t \tag{55}$$

$$0 \le \eta_l^{ld}, \eta_l^{ud}, \eta_{pv}^{ld}, \eta_{pv}^{ud} \le 1$$
(56)

where η_c^{ld} , η_c^{ud} are the scaled deviations for the random cooling load; η_h^{ld} , η_h^{ud} are the scaled deviations for the random thermal load. Similarly, η_l^{ld} , η_l^{ud} , η_p^{ud} , η_{pv}^{ud} , η_{pv}^{ud} are the scaled deviations for the random electrical load and the PV output.

Identifying the worst-case scenarios when cooling, thermal, and electric load and PV vary within their uncertain intervals requires transforming (21), (22) and (24) into an equivalent max optimization problem (48), (51) and (53) for calculating the worst-case scenarios.

Thus, a CCHP microgrid economic dispatch model is a min-max optimization problem. To make the above problem tractable, (57), (63) and (69) must be converted into corresponding dual problems (60), (66) and (72) by introducing dual variables λ_c^t , π_{cl}^{t+} , π_{cl}^{t-} , λ_h^t , π_{hl}^{t+} , π_{hl}^{t-} , λ_{nl}^t , π_{ll}^{t+} , π_{ll}^{t-} π_{pv2}^{t+} , and π_{pv2}^{t-} .

$$\max \eta_c^{ld} Q_c^{ld} + \eta_c^{ud} Q_c^{ud}$$
(57)
s.t.
$$\eta_c^{ld} + \eta_c^{ud} < \Gamma_c^t$$
(58)

$$0 \le \eta_c^{ld}, \eta_c^{ud} \le 1 \tag{59}$$

$$\min \lambda_c^t \Gamma_c^t + \pi_{c1}^{t+} + \pi_{c1}^{t-} \tag{60}$$

$$\Rightarrow \begin{cases} \text{s.t.} \quad \lambda_{c}^{t} + \pi_{c1}^{t-} \ge Q_{c}^{ld}, \lambda_{c}^{t} + \pi_{c2}^{t+} \ge Q_{c}^{ud} \quad (61) \\ \lambda_{c}^{t}, \pi_{c1}^{t+}, \pi_{c1}^{t-} \ge 0 \quad (62) \end{cases}$$

$$\int \max(\eta_h^{ld} H_h^{ld} + \eta_h^{ud} H_h^{ud}) / \eta_{he} \tag{63}$$

s.t.
$$\eta_u^{ld} + \eta_h^{ud} \le \Gamma_h^t$$
 (64)

$$\begin{pmatrix} 0 \le \eta_h^{-}, \eta_h^{--} \le 1 \\ \min \lambda_t^{t} \Gamma_t^{t} + \pi_t^{t+} + \pi_t^{t-} \\ \end{pmatrix}$$
(65)

$$\Rightarrow \begin{cases} \text{s.t.} \quad \lambda_{c}^{t} + \pi_{h1}^{t-} \ge H_{h}^{ld}, \lambda_{h}^{t} + \pi_{h1}^{t-} \ge H_{h}^{ud} \quad (67) \\ \lambda_{h}^{t}, \pi_{h1}^{t-}, \pi_{h1}^{t-} \ge 0 \qquad (68) \end{cases}$$

$$+ \pi_{h1}^{t-}$$
(66)
 $h_{h} + \pi_{h1}^{t+} \ge H_{h}^{ud}$ (67)

$$\lambda_h^t, \pi_{h1}^{t+}, \pi_{h1}^{t-} \ge 0 \tag{68}$$

$$\begin{cases} \max \eta_{l}^{ld} P_{l}^{ld} + \eta_{l}^{ud} P_{l}^{ud} - \eta_{pv}^{ld} P_{pv}^{ld} - \eta_{pv}^{ud} P_{pv}^{ud} \ (69) \\ \text{s.t.} \quad \eta_{l}^{ld} + \eta_{l}^{ud} + \eta_{pv}^{ld} + \eta_{pv}^{ud} \leq \Gamma_{nl}^{t} \ (70) \\ 0 \leq \eta_{l}^{ld}, \eta_{l}^{ud}, \eta_{pv}^{ld}, \eta_{pv}^{ud} \leq 1 \ (71) \end{cases}$$

$$\begin{cases} \min \lambda_{nl}^{t} \Gamma_{nl}^{t} + \pi_{l1}^{t+} + \pi_{l1}^{t-} + \pi_{pv2}^{t+} + \pi_{pv2}^{t-} \ (72) \\ \text{s.t.} \quad \lambda_{nl}^{t} + \pi_{l1}^{t-} \geq P_{l}^{ld}, \lambda_{nl}^{t} + \pi_{l2}^{t+} \geq P_{l}^{ud} \ (73) \\ \lambda_{nl}^{t} + \pi_{nv}^{t-} \geq - P_{nv}^{ld}, \lambda_{nl}^{t} + \pi_{nv}^{t+} \geq - P_{nv}^{ud} \ (74) \end{cases}$$

$$\lambda_{nl}^{t}, \pi_{l1}^{t+}, \pi_{l1}^{t-} \pi_{pv2}^{t+}, \pi_{pv2}^{t-} \ge 0$$
(75)

Finally, a tractable robust model can be formulated as:

$$\min C = C_{grid} + C_f + C_{bt} + C_{rm} \tag{76}$$

$$COP_{ac} \cdot H_{ac}^{t} + COP_{ec} \cdot P_{ec}^{t} = Q_{c}^{t} + \lambda_{c}^{t} \Gamma_{c}^{t} + \pi_{c1}^{t+} + \pi_{c1}^{t-}$$
(77)

$$P_{mt}^{t} + P_{grid}^{t} + P_{bt,chr}^{t} + P_{ec}^{t} - P_{excess}^{t} - P_{bt,dis}^{t} = P_{l,u}^{t} - P_{pv,u}^{t}$$
$$= P_{l}^{t} - P_{pv}^{t} + \lambda_{nl}^{t} \Gamma_{nl}^{t} + \pi_{l1}^{t+} + \pi_{l1}^{t-} + \pi_{pv2}^{t+} + \pi_{pv2}^{t-}$$
(79)

along with (1)-(20), (23), (60)-(62), and (66)-(68), (73)-(75).

4 Case study

To verify the performance of the proposed algorithm, a CCHP building in Shanghai, China, was used in a case study. The building has twelve floors with a total square footage of 6000 m^2 and an average floor height of 3.8 m. Figure 3 shows the hourly PV output and the cooling, heating, and power load for representative days during the summer.

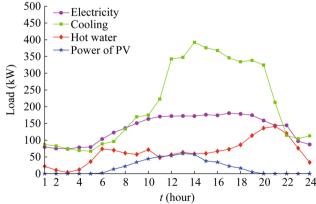


Fig. 3 Hourly PV power, and cooling, heating, and power load of the building



Table 1 Time-of-use price

Period	Time	Purchase price (\$/kWh)	Sell price (\$/kWh)
Peak load period	8:00-10:59	0.1974	0.099
	13:00-14:59		
	18:00-20:59		
Flat load period	6:00–7:59	0.123	0.099
	11:00-12:59		
	15:00-17:59		
	21:00-21:59		
Off-peak load period	22:00-5:59	0.0585	0.099

Table 2 Parameters values

Parameters	Value	Parameters	Value
α, β	2.67, 11.43	K _{om,pv}	0.00205 \$/kWh
η_b	0.73	$K_{om,bt}$	0.00106 \$/kWh
η_{hr}	0.75	K _{om,tst}	0.0031 \$/kWh
η_{he}	0.9	P_{mt}^{\min}	30 kW
COP_{ec}	4	P_{mt}^{\max}	200 kW
COP_{ac}	0.9	P_b^{\min}	0
η_{bt}^{chr}	0.95	P_b^{\max}	258 kW
η_{bt}^{dis}	0.95	P_{grid}^{\min}	0
σ_{bt}	0.02	P_{grid}^{\max}	200 kW
η_{tst}^{chr}	0.9	P_{bt}^{\min}	170 kW
η_{tst}^{dis}	0.9	P_{bt}^{\max}	-250 kW
σ_{tst}	0.1	W_{bt}^{\min}	100 kWh
R_{ng}	0.4561 \$/m ³	W_{bt}^{\max}	500 kWh
H_{ng}	9.78 kWh/m ³	H_{tst}^{\min}	-200 kW
K _{om,mt}	0.026 \$/kWh	H_{tst}^{\min}	200 kW
K _{om,b}	0.0027 \$/kWh	W_{tst}^{\min}	0 kW
K _{om,he}	0.001 \$/kWh	W_{tst}^{\max}	500 kW
Kom,ac	0.0024 \$/kWh	R_{bt}^{t}	8.05 \$
Kom,ec	0.0016 \$/kWh	$P^{\mu p}_{mt}$	60 kWh
$P_{bt}^{up}, P_{bt}^{down}$	40 kWh	P_{mt}^{down}	60 kWh

The CCHP system consists of a photovoltaic system (80 kW), a battery (200 kWh), a gas micro turbine (200 kW), a boiler (258 kW), an electric chiller (100 kW), an absorption chiller (200 kW), a heat exchanger (200 kW), and a thermal storage tank (150 kWh), as shown in Fig. 1. Table 1 is the peak-valley price of the double system electricity price in summer and selling prices at different times of the day [37, 38]. The fuel we chose here is a widely used fuel, which is natural gas, and its price is 0.4561 \$/m³. Table 2 lists the remaining parameters used in this study as referenced by [1, 9, 39].

 Table 3
 Average probability of potential power falling into uncertainty set

ρ	Probability
0.9	0.973
0.7	0.947
0.5	0.836
0.3	0.743
0.1	0.674

Table 4 Five cases for energy management of CCHP microgrid

Case	Efficiency curves		Model		
	Constant	Nonlinear	Piecewise linear	Deterministic	Robust
1	~			v	
2	~				~
3			v	~	
4			v		~
5		~			

Based on the observation of historical data, it has been shown that hourly PV power and cooling, heating, and power load follow a normal distribution with a mean value μ and standard deviation σ during for representative days in summer, as shown in Fig. 2 and Table 11. To estimate the uncertainties of PV power and the cooling, heating, and power load, the fluctuation of the uncertainties are defined as:

$$\Delta \theta_{i,t} = \frac{\sigma_{i,t}}{\sqrt{1-\rho}} \tag{80}$$

where $\Delta \theta_{i,t}$ is the fluctuation range of the *i*-th uncertainty (including the PV output and the cooling, heating, and power load). The upper fluctuation of each uncertainty is expressed as $\Delta \theta_{i,t}$ (i.e., $Q_c^{ud} = \Delta \theta_{c,t}$, $H_h^{ud} = \Delta \theta_{h,t}$, $P_l^{ud} = \Delta \theta_{l,t}$ and $P_{pv}^{ud} = \Delta \theta_{pv,t}$), whereas the lower fluctuation of the each uncertainty is modelled as $-\Delta \theta_{i,t}$ (i.e., $Q_c^{ld} = -\Delta \theta^{c,t}$, $H_h^{ld} = -\Delta \theta_{h,t}$, $P_l^{ld} = -\Delta \theta_{l,t}$, $P_{pv}^{ld} = -\Delta \theta_{pv,t}$). The fluctuation interval can be controlled effectively by adjusting the parameter value of ρ_{it} .

To demonstrate the effectiveness of the uncertain set in the robust optimization model, a Monte-Carlo simulation was adopted to sample the cooling, heating and electrical power randomly. We then determined the probability of each interval that fell into the uncertain interval and calculated the average probability of each interval.

It can be seen from Table 3 that with the decrease of ρ , the probability that the cooling, heating and electrical power and PV output are included in the uncertain set also



L

 Table 5 Comparison three efficiency curves

Case	Operation cost (\$)	Computing time (s)
1	500.07	0.87
3	496.5	1.31
5	498.76	138

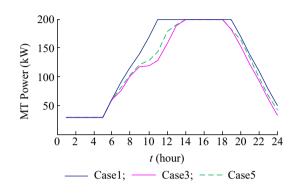


Fig. 4 Comparison of the MT power considering constant, piecewise linear and nonlinear efficiency curve model

decreases. When the value of ρ reaches 0.9, it can be guaranteed that the probability will reach 97%; however, when the value decreases to 0.1, the probability decreases to 67%. Therefore, the conservativeness of robust optimization model can be controlled effectively by adjusting the parameter value of ρ .

To analyze the effectiveness of the proposed model, five cases are studied and simulated as shown in Table 4, in which ' \checkmark ' means that source is in the CCHP microgrid. The MILP robust optimization model is solved by Cplex [40]. The PSO approach was applied to solve the case 5, which used nonlinear efficiency curves [11].

4.1 Comparison of three efficiency models under deterministic optimization

Table 5 summarizes the operating cost and computing times of the three aforementioned approaches when an optimality parameter was specified. The three methods yield similar solutions in terms of total operating cost, though Case 3 obtained a lower operating cost than Case 1 and 5 because a global optimization result was guaranteed for the MILP. Meanwhile, Case 3 achieved a more accurate system operating status than Case 1 and 5, without sacrificing computational advantage.

As shown in Fig. 4, compared with Case 3, there were different MT optimization results for the CCHP microgrid in Cases 1 and 5. In Case 1, the MT provided its rated power in periods 12 to 19 but operated at rated power during periods 14 to 18 in Case 3. In all time periods, the

 Table 6 Comparison of different efficiency curves under robust models

ρ	Case 2 (\$)	Case 4 (\$)
0.9	545.90	542.94
0.7	541.13	537.48
0.5	530.52	528.36
0.3	525.18	522.13
0.1	513.35	510.24

scheduling curves of the MT were extremely similar for both Case 3 and Case 5. In Case 5, the power generated by the MT was greater than Case 3 in periods 7 to 13 and 19 to 24, which could not determine global optimization results through comparing the optimization results for both deterministic and robust cases when considering the piecewise linear efficiency curve model in detail.

4.2 Comparison of constant efficiency model and piecewise linear efficiency curve model under robust optimization

Table 6 provides the simulated running cost under different load and PV uncertainties, using constant and piecewise linear efficiency curves, respectively. It shows that when the fluctuation interval of the uncertainties increases, the running cost of the robust case increases.

Figure 5 shows the operating conditions of the MT, the exchange power with the main grid, the electric chiller power, and the gas boiler power during the entire scheduling horizon at different uncertainty levels during the summer when $\rho = 0.9$. When coping with the fluctuation of load and PV output, the power generated by the MT in the robust case was always greater than in the corresponding deterministic case due to the response of the MT to the uncertainty of the cooling, thermal and electrical energy requests. Meanwhile, the CCHP microgrid sold less extra power to the main grid, and coordinated the power of the electric chiller and absorption chiller. In considering the aging cost, the scheduling curves of the battery were extremely similar for both the deterministic and robust cases in all time periods.

Compared with the constant efficiency model, there were different dispatching results for the CCHP microgrid in the piecewise linear efficiency model. In Case 2, the MT provided rated power during periods 11 to 19 but operated at rated power during periods 13 to 19 in Case 4. In Cases 3 and 4, the CCHP microgrid sold almost no extra power to the main grid during periods 9 to 11; however, it sold more extra power to the main grid during these periods in Cases 1 and 2. The TST charged more heating power during periods 9 to 12 and discharged more heating power during periods 18 to



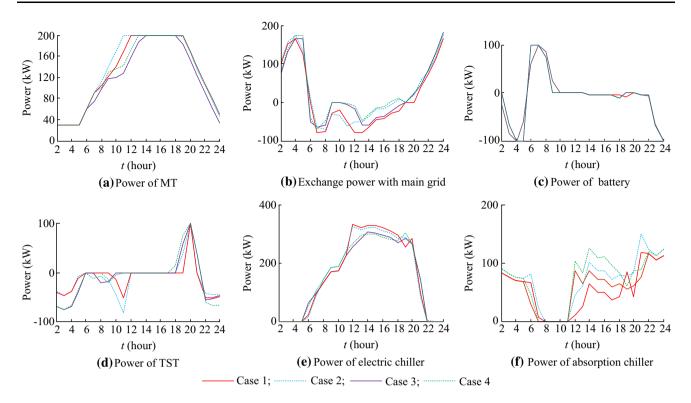


Fig. 5 Comparison of the deterministic and robust case for CCHP microgrid ($\rho = 0.9$)

21 than in the constant efficiency model. In all time periods, the scheduling curves of the electric chiller were extremely similar for both Case 1 and Case 2, but the power of the electric chiller was greater than in the piecewise linear efficiency model during periods 11 to 18. In addition, the power of the absorption chiller provided more cooling power during periods 12 to 18 in piecewise linear efficiency model.

To show the effectiveness of robust optimization and its applicability in a real-time environment, Monte Carlo simulation is applied to generate different realizations of load and RES generation. The size of the sample is set to be 1000. The expected intra-day operation cost of the robust optimization and the deterministic optimization can be calculated under the day-ahead schedule. The expected operation cost of two optimization models are shown in Table 7. It can be seen from Table 7 that with the increase of ρ , compared with robust optimization, the operating cost of deterministic optimization was increasing. When ρ

Table 7 Expected cost of robust model and deterministic model

ρ	Case 4 (\$)	Case 3 (\$)	Increased (%)
0.1	502.58	503.47	0.18
0.3	510.83	514.22	0.27
0.5	517.26	526.85	1.85
0.7	526.87	540.24	2.54
0.9	538.46	555.96	3.25

equals to 0.1/0.3, the expected cost of deterministic approach is almost the same with robust optimization approach, only increased by 0.18%/0.27%, respectively. When ρ equals to 0.5/0.7/0.9, expected cost of the deterministic approach is more than robust optimization approach, increased by 1.85%/2.54%/3.25%, respectively. The economy of the optimal decision could be achieved by adjusting the fluctuation interval of uncertainty set to control the conservatism of the model.

4.3 Influence of uncertainty budget levels on the system fluctuation ($\rho = 0.9$)

Compared with no fluctuation of the cooling, thermal and net electrical load, Figs. 6, 7 and 8 shows the adjusted

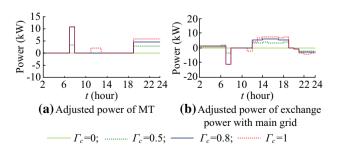


Fig. 6 Effect of robustness budget in controlling the uncertain ranges of cooling load



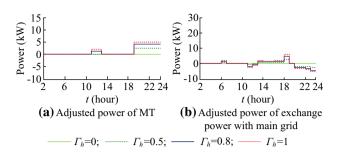


Fig. 7 Effect of robustness budget in controlling the uncertain ranges of thermal load

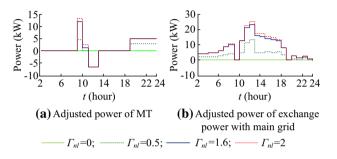


Fig. 8 Effect of robustness budget in controlling the uncertain ranges of electrical load and PV

power of the MT and the exchange power with the main grid in different robustness budgets in controlling the uncertain ranges of cooling, thermal and net electricity load when $\rho = 0.9$. In Fig. 6, Γ_h and Γ_{nl} are fixed at 1 and 2, respectively, to ensure the worst-case thermal and net electrical load. Γ_c is adjusted from 0 to 1. $\Gamma_c = 0$ denotes there are no cooling load fluctuation; $\Gamma_c = 1$ denotes the worst-case cooling load. Table 8 shows the change of operating cost with the increase of robustness budget Γ_c .

In Fig. 7, Γ_c and Γ_{nl} are fixed at 1 and 2, respectively, to ensure the worst-case cooling and net electricity load; the uncertainty set of the thermal load is enlarged by increasing the robustness Γ_h from 0 to 1. Table 9 shows the change of operating cost as the robustness budget Γ_h increase.

In Fig. 8, Γ_c and Γ_h are fixed at 1 and 1, respectively, to ensure the worst-case cooling and thermal load; the uncertainty set of the net electrical load are enlarged by increasing the robustness Γ_{nl} from 0 to 2. Table 10 shows

Table 8 Operating cost with various Γ_c ($\Gamma_h = 1$, $\Gamma_{nl} = 2$)

Γ_c	Case 4 (\$)	Increased (%)
0	530.6	0
0.5	536.74	1.16
0.8	540.45	1.86
1	542.94	2.33

Table 9 Operating cost with various Γ_h ($\Gamma_c = 1$, $\Gamma_{nl} = 2$)

Γ_h	Case 4 (\$)	Increased (%)
0	539.3	0
0.5	541.11	0.03
0.8	542.21	0.05
1	542.94	0.07

Table 10 Operating cost with various Γ_{nl} ($\Gamma_c = 1$, $\Gamma_h = 1$)

-	•	
Γ_{nl}	Case 4 (\$)	Increased (%)
0	512.49	0
0.5	523.55	2.16
0.8	530.22	3.46
1	534.65	4.52
1.3	537.14	4.81
1.6	539.62	5.29
1.8	541.28	5.62
2	542.94	5.94

the change of operating cost as the robustness budget Γ_{nl} increase.

Tables 8, 9 and 10 show that with the increase of the robustness budget Γ (Γ_c , Γ_h and Γ_{nl}), the operating cost of the robust case increases. When Γ_c is adjusted from 0 to 1 ($\Gamma_h = 1$ and $\Gamma_{nl} = 2$), the operating cost increases by 2.33%. When Γ_h is adjusted from 0 to 1 ($\Gamma_c = 1$ and $\Gamma_{nl} = 2$), the operating cost increases by 0.07%. When Γ_{nl} is adjusted from 0 to 2 ($\Gamma_c = 1$ and $\Gamma_h = 1$), the operating cost increases by 5.94%. The differences in the operating cost show that the fluctuation of net electrical load has the more significantly effect on the operating cost of the CCHP microgrid than the fluctuation of the cooling or thermal.

Figures 6, 7 and 8 show that with the increase of the robustness budget Γ (Γ_c , Γ_h and Γ_{nl}), there are different dispatching results for the CCHP microgrid under different uncertainty budget levels of different energy (cooling, thermal and electrical). The fluctuation of net electrical load have the greater effect on the dispatching results of the CCHP microgrid than the fluctuation of the cooling or thermal.

In general, these dispatching results demonstrate that uncertainties in the load and PV outputs are mitigated by the MT, the exchange power with the main grid, and other components.The thermal fluctuation during the summer subtly change the dispatching results, which reduce the impact on the superior power grid. When the fluctuation in cooling load, electrical load and PV become increase, the exchange power with the main grid will change with the system electric power fluctuation, which have impacts on the superior grid. These fluctuation can be suppressed not only by adjusting the MT but also coordinating other equipment.



5 Conclusion

This paper presented a robust optimization method that considered piecewise linear thermal and electrical efficiency curves to hedge the uncertainties of the cooling, thermal, and electrical load and solar power generation for the energy management of a CCHP microgrid. A worstcase security-constrained economic optimization model was developed and a strong duality theory was used to transform the problem into a MILP formulation. The robustness could also be adjusted to control the conservativeness of the proposed model.

By characterizing a piecewise linear thermal and electrical efficiency curve model instead of constant efficiencies or non-fixed efficiency models, the operating status of the system could be reflected exactly without sacrificing problem linearity.

The simulation results showed that fluctuation of the system have less effect on the dispatching results of the battery when considering the aging cost. Meanwhile, the robust optimization approach performs better than the deterministic optimization mode, and decreases the expected operation cost. Furthermore, compared with fluctuation of the cooling and thermal load, fluctuation of net electrical load has a greater influence on the operating cost and conditions of the system.

The demand response can mitigate the variability of renewable resources and partial user demand by allowing user demand to be controllable. Thus, future research should be focus on combining the robust optimization method with demand response to address the uncertainties of the CCHP microgrid.

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Appendix A

See Table A1.

 Table A1
 Average probability of potential power falling into uncertainty set

Time	Cooling (σ_c)	Heat (σ_h)	Power (σ_l)	PV (σ_{pv})
1	2.33	0.59	2.13	0
2	2.21	0.28	2.01	0
3	1.98	0.11	1.98	0
4	1.85	0.32	2.09	0
5	1.79	0.96	2.13	0
6	2.38	1.97	2.76	0.10
7	2.57	1.87	3.28	0.67
8	3.56	1.63	3.63	1.11
9	4.53	1.54	4.03	1.72
10	4.67	1.91	4.36	2.23
11	5.95	1.27	4.55	2.57
12	9.13	1.52	4.59	2.69
13	9.27	1.70	4.61	3.01
14	10.46	1.58	4.60	2.89
15	10.01	1.61	4.70	1.89
16	9.81	1.79	4.65	1.72
17	9.23	1.95	4.83	1.12
18	8.92	2.30	4.76	0.82
19	9.02	3.04	4.66	0.27
20	8.67	3.63	4.24	0
21	5.68	3.77	3.83	0
22	3.06	3.20	3.86	0
23	2.78	2.04	2.61	0
24	3.02	0.90	2.33	0



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